

DATA-DRIVEN STRONG GRAVITATIONAL LENSING ANALYSIS IN THE ERA OF LARGE SKY SURVEYS

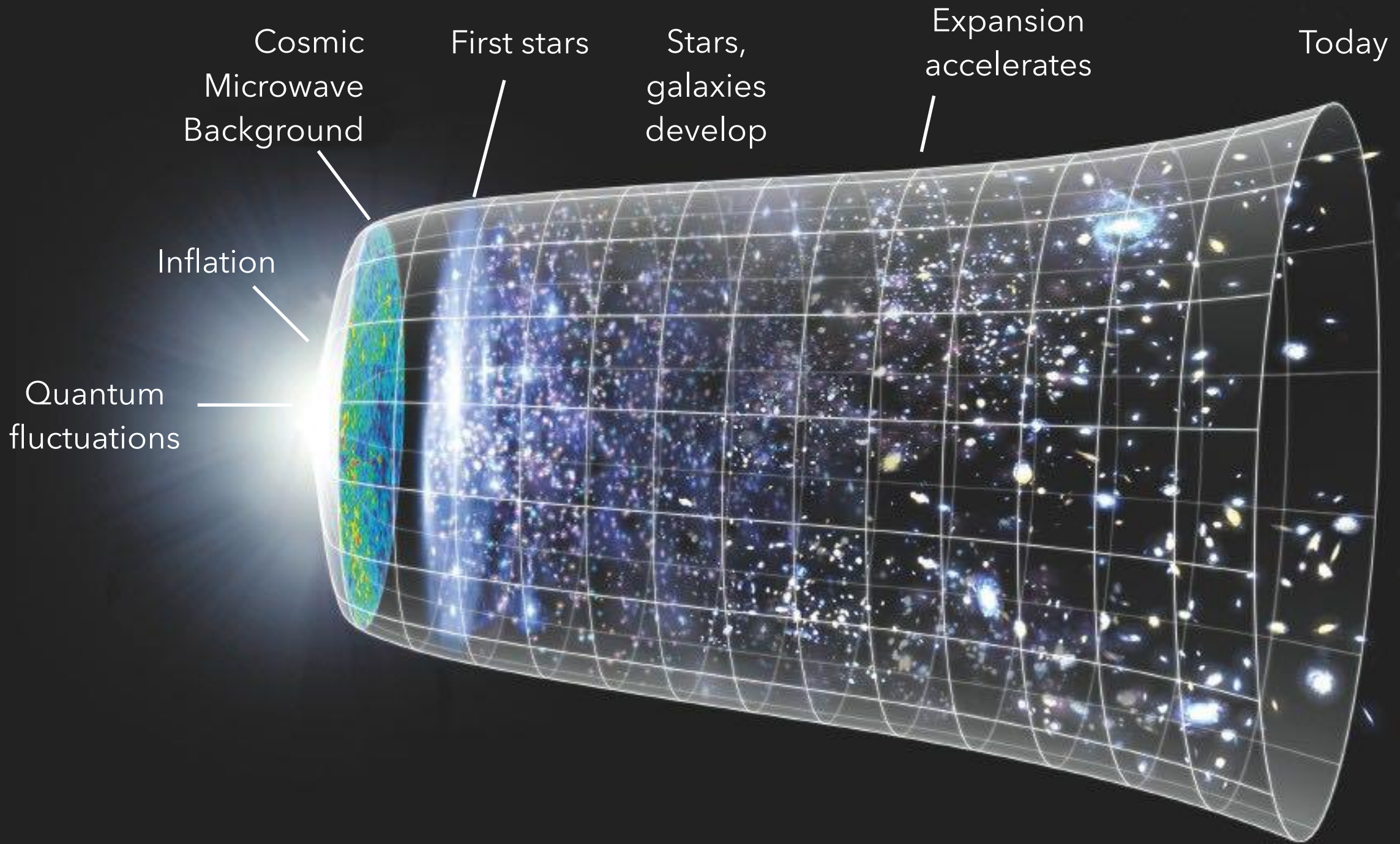
Laurence Perreault-Levasseur

Ciela Institute

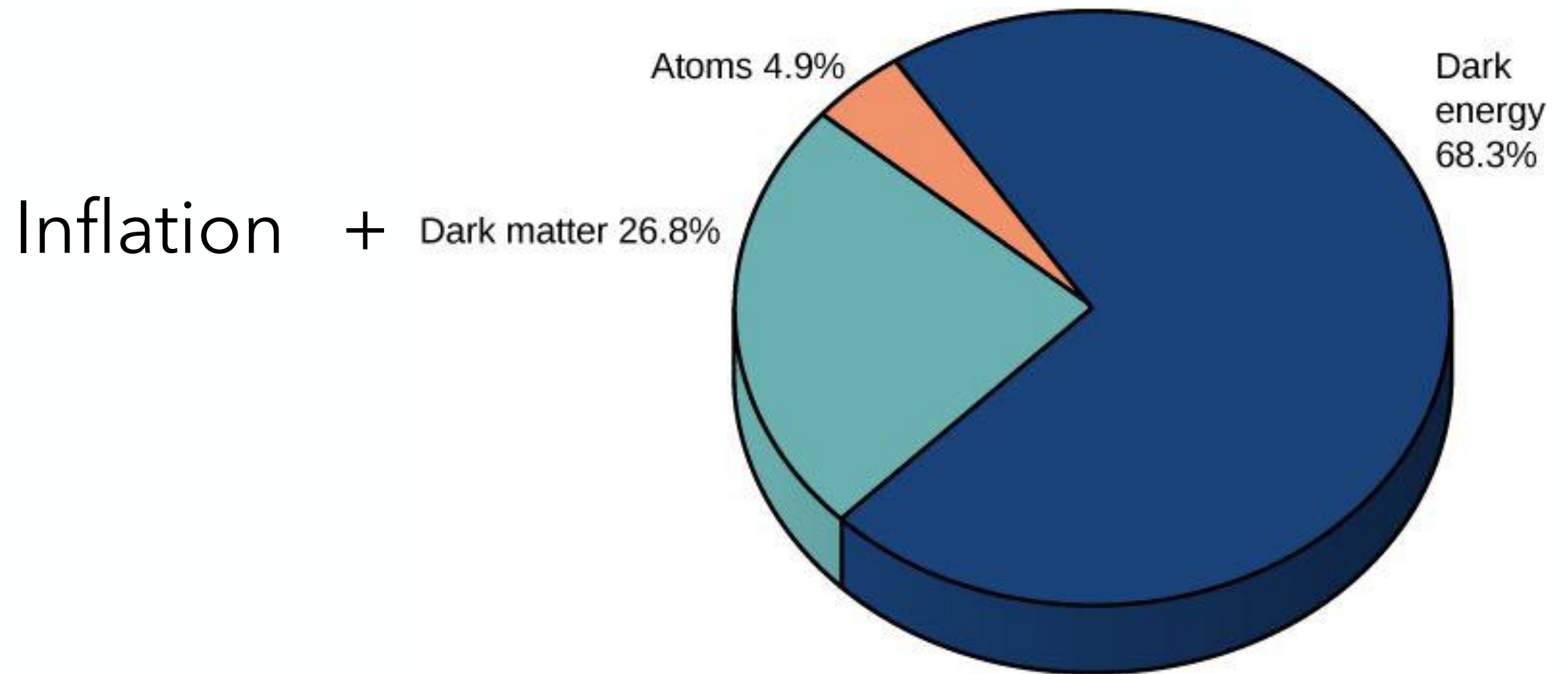
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Astrophysics



INFLATIONARY- Λ CDM

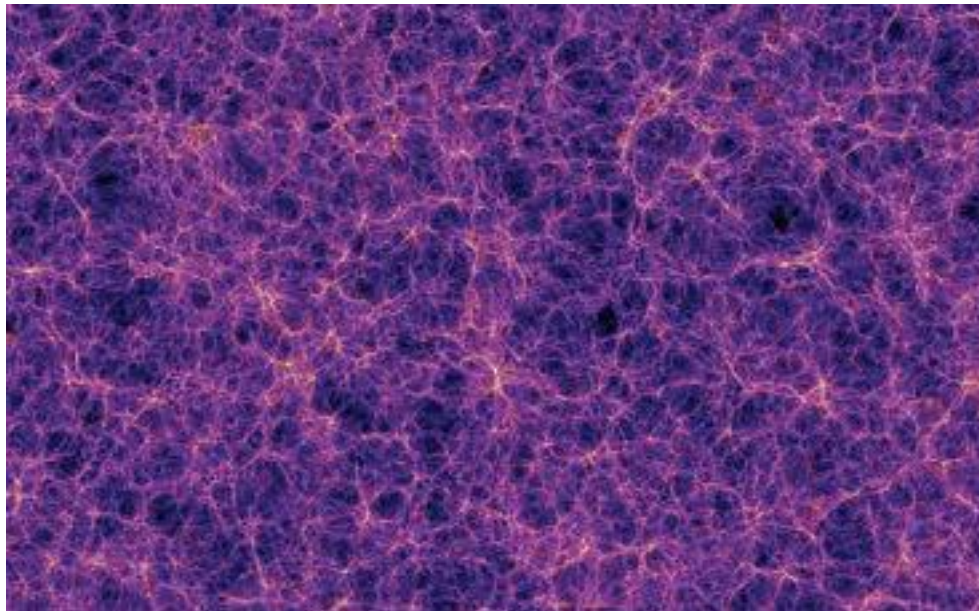
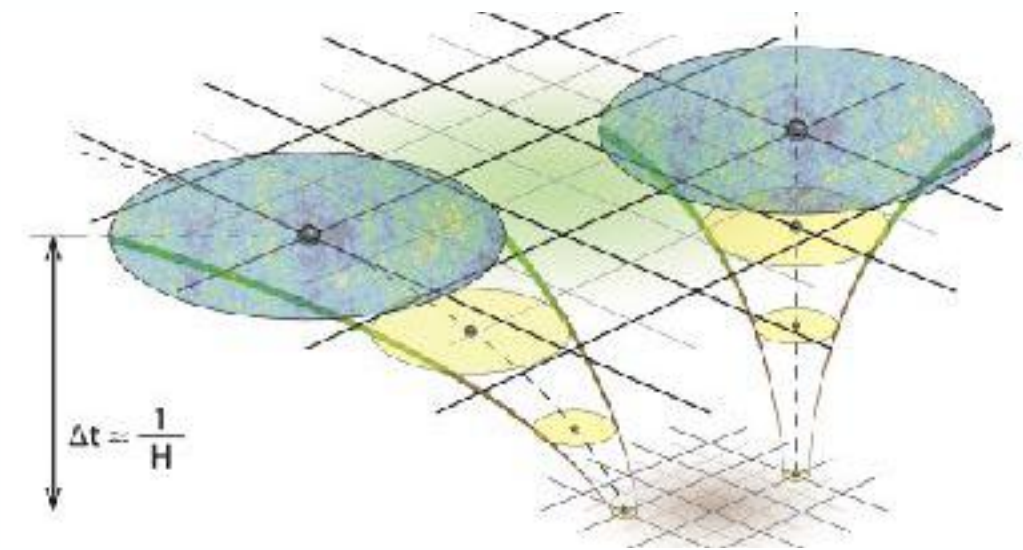


At this point,
are we done with cosmology?

Inflationary- Λ CDM

Inflation:

The nature, properties, or origin of the field causing inflation are completely unknown



Dark Matter:

What is known:
only that it exists and gravitates

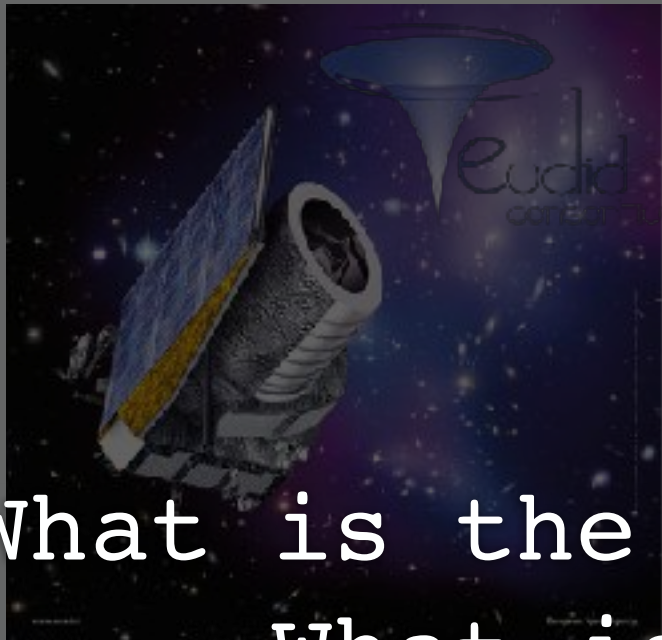
Dark Energy:

Is not even remotely understood.





MODERN COSMOLOGY



LSST: By the numbers

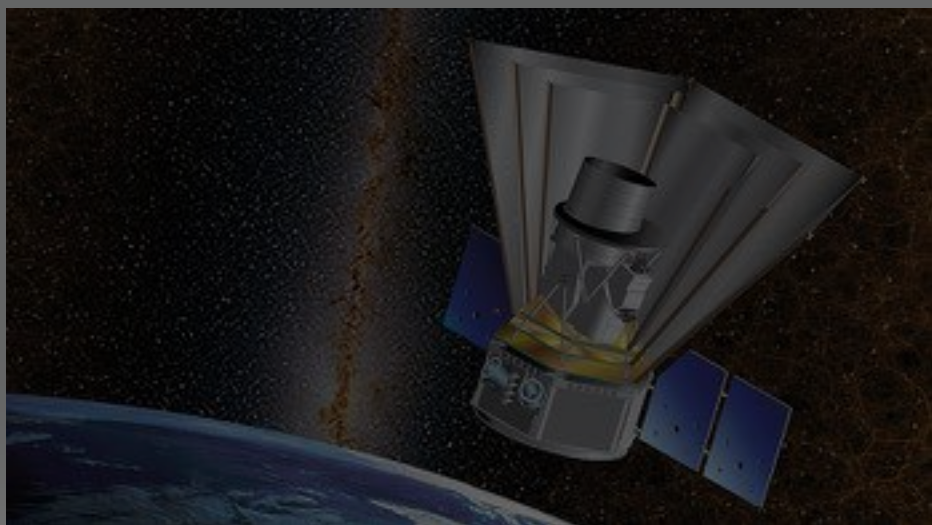
- 8 meter wide field survey telescope
- 3 billion pixel digital camera
- 3 mirror construction
- 30 terabytes of data per night

NSF's Large Synoptic Survey Telescope will image the entire visible sky a few times each week for 10 years and is expected to see first light in 2019.

NATIONAL SCIENCE FOUNDATION



What is the nature of inflation?
 What is "dark matter"?
 What is "dark energy"?





MODERN COSMOLOGY



LSST: By the numbers

8 meter wide field survey telescope

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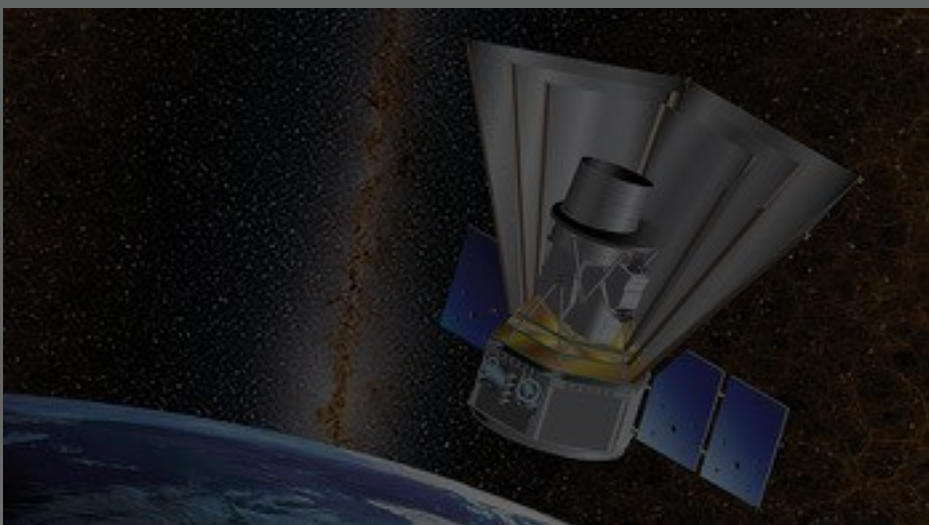
30 terabytes of cats per night

NSF's Large Synoptic Survey Telescope will image the entire visible sky a few times each week for 10 years and is expected to see first light in 2019.

NATIONAL SCIENCE FOUNDATION

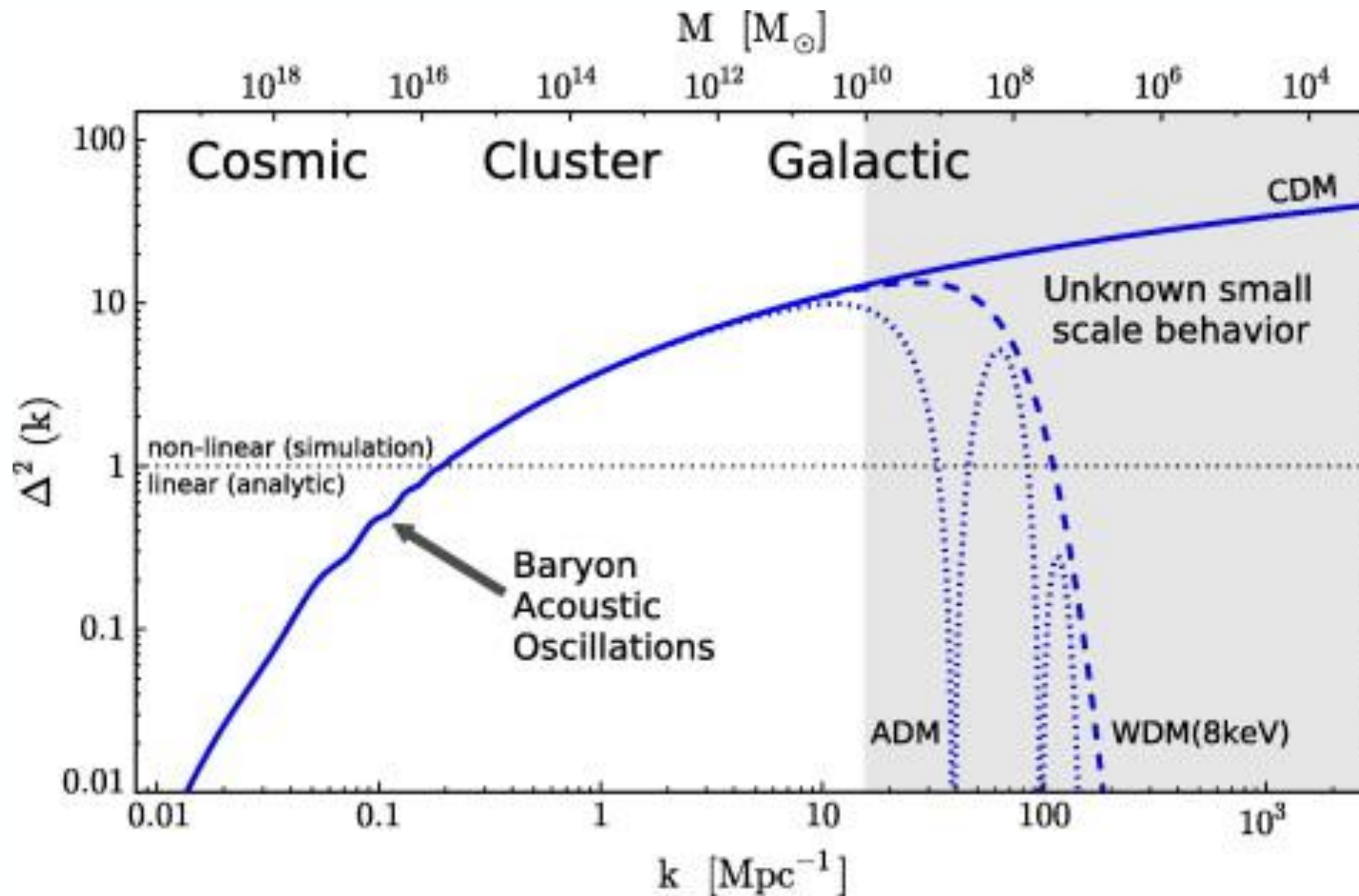


What is the nature of inflation?
 What is "dark matter"?
 What is "dark energy"?



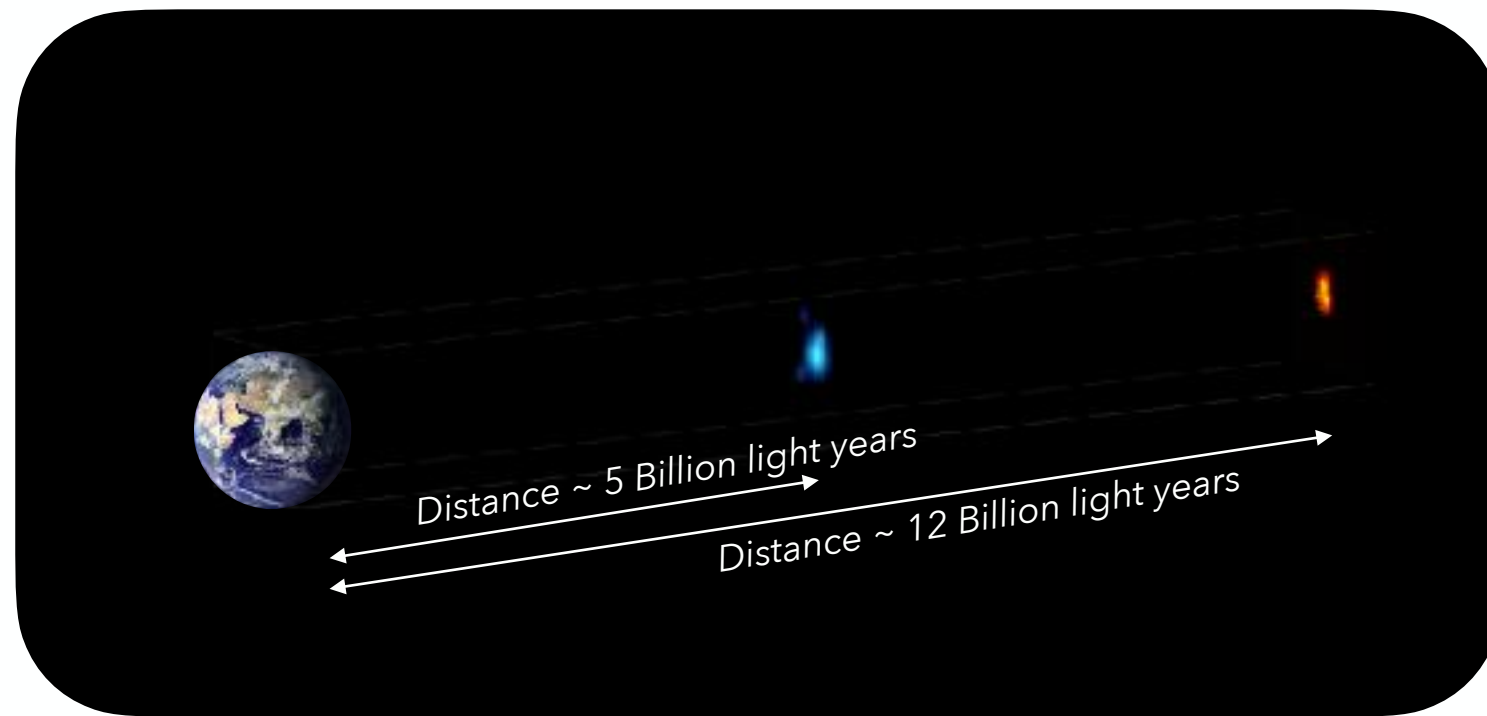


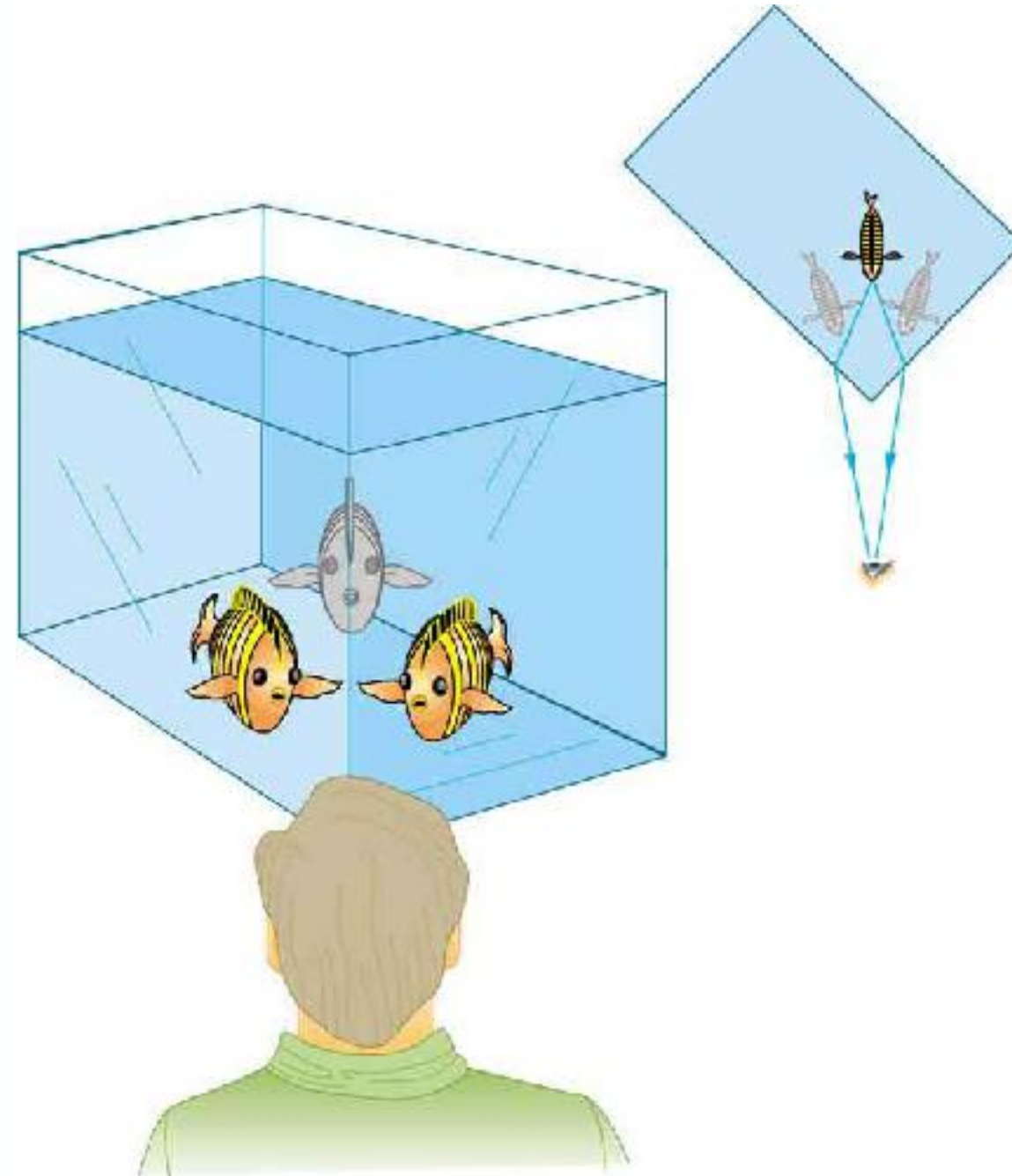
Matter power spectrum

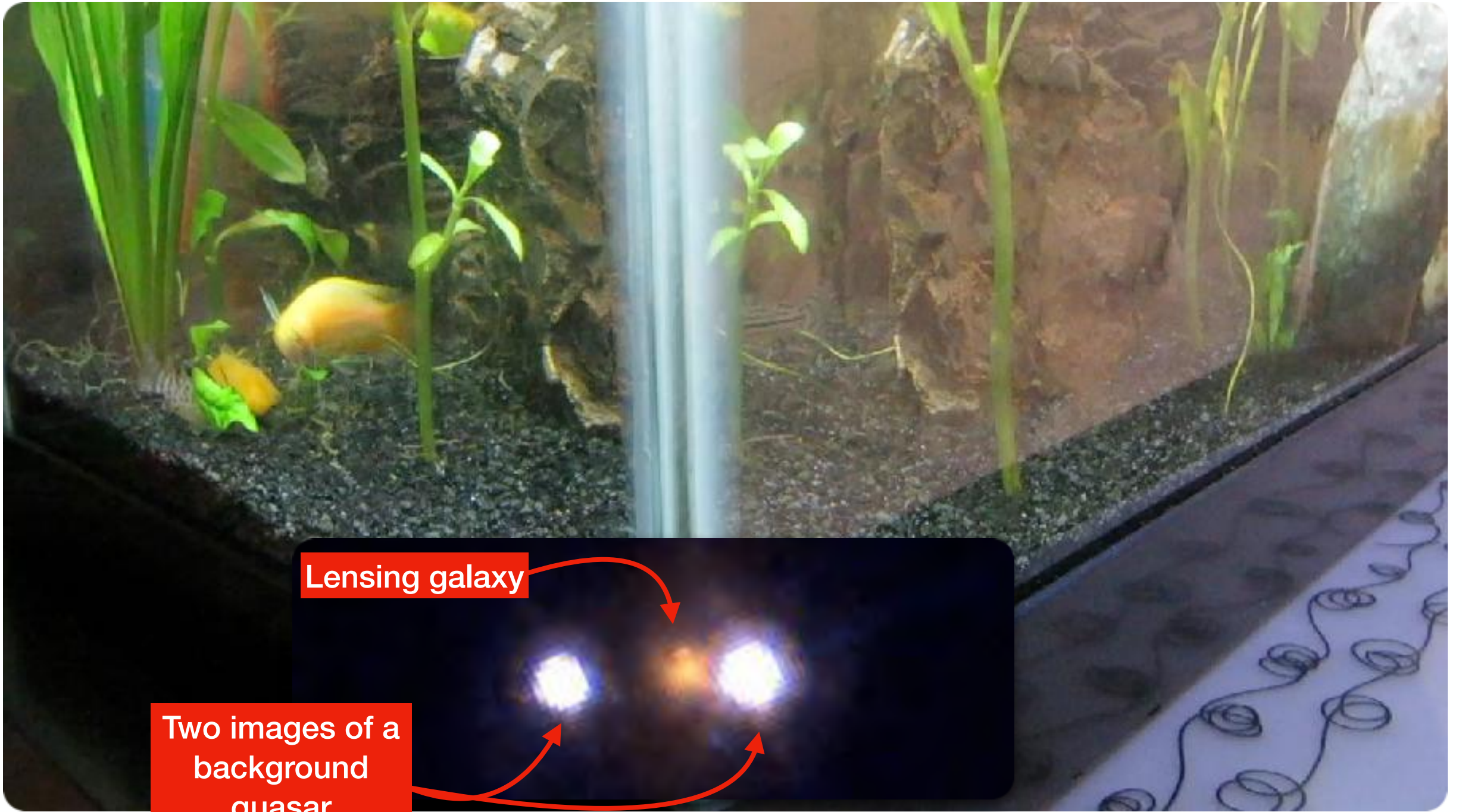


STRONG GRAVITATIONAL LENSING

Formation of **multiple images** of a single distant object due to the **deflection of its light** by the **gravity** of intervening structures.







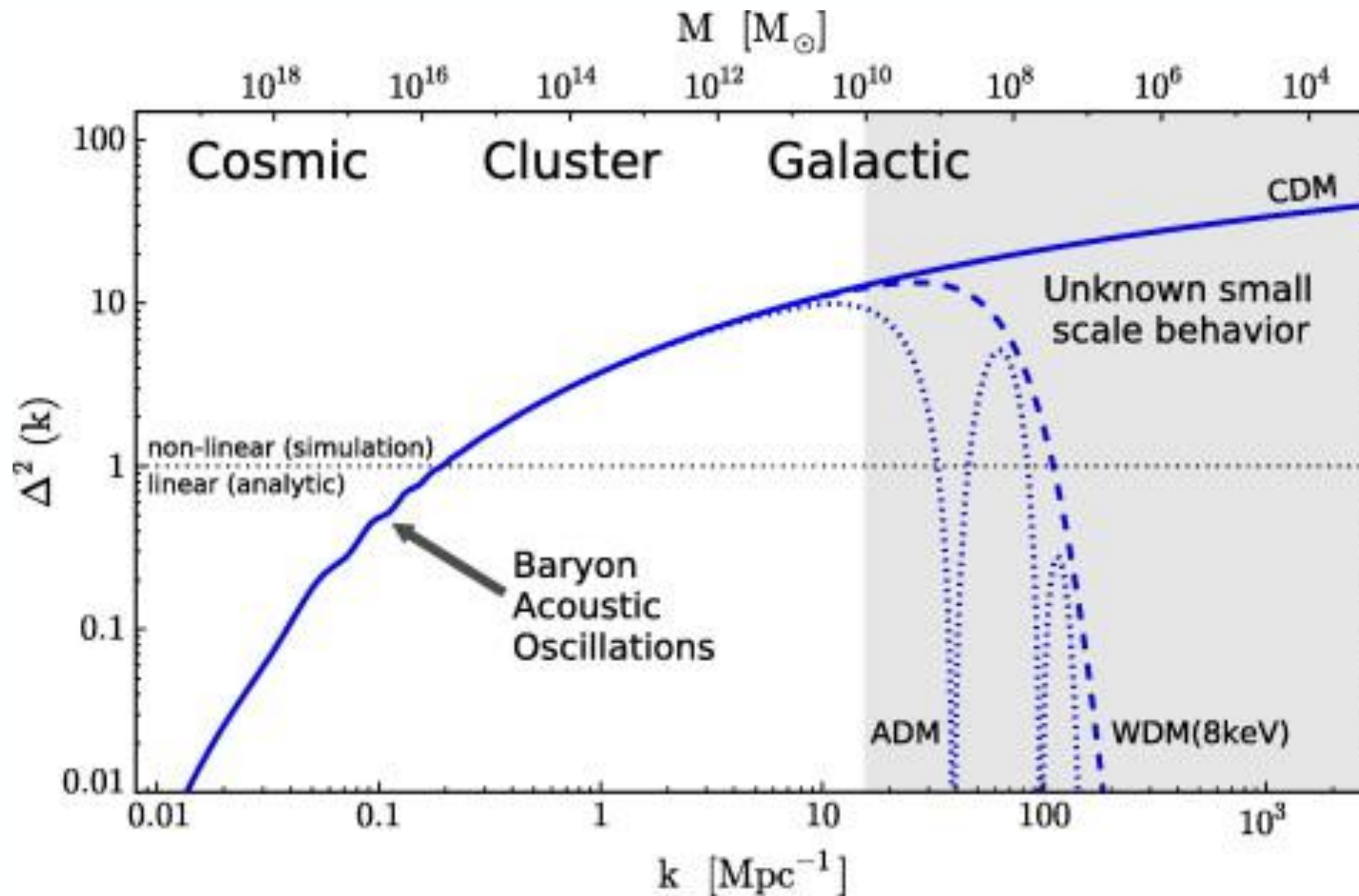
Lensing galaxy

Two images of a background quasar

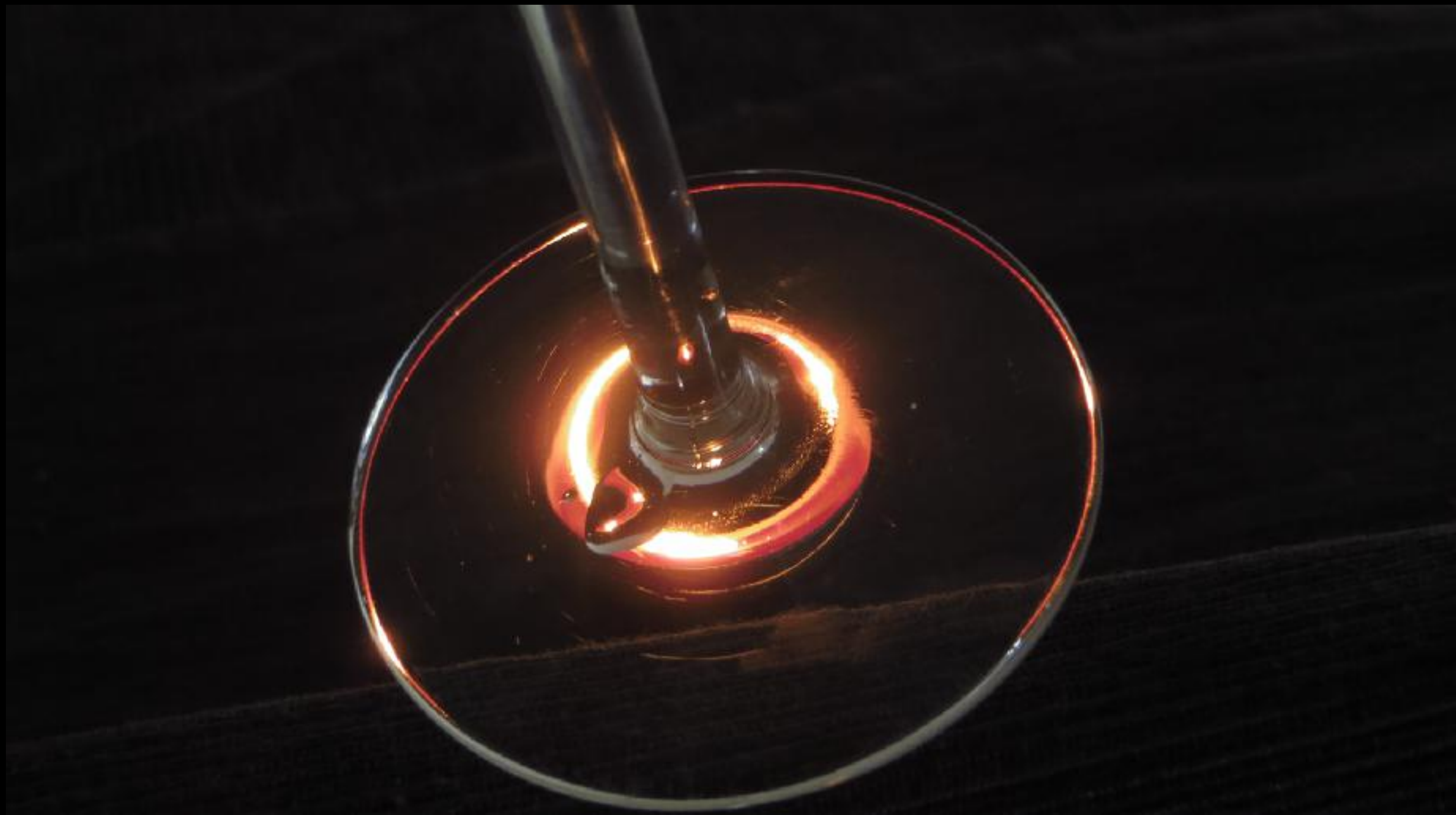




Matter power spectrum







SCIENCE MOTIVATIONS FOR STRONG LENSING

- **Foreground structure**

Use lensing to probe the **distribution of matter** in the lensing galaxies.

- **Background source**

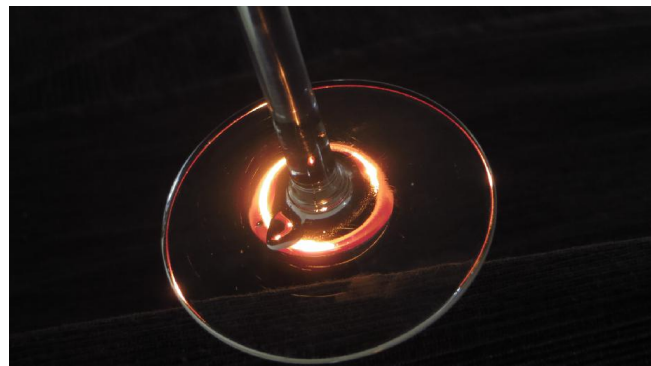
Use strong lensing as a **cosmic telescope**.

- **Cosmology**

Use lensing to probe the **cosmological parameters (H_0)**



LENSING ANALYSIS



Data



1: Morphology of the background source
(the true, undistorted image of the candle)



2: Matter distribution in the lens
(the shape of the wineglass)

Source Parameters (linear)

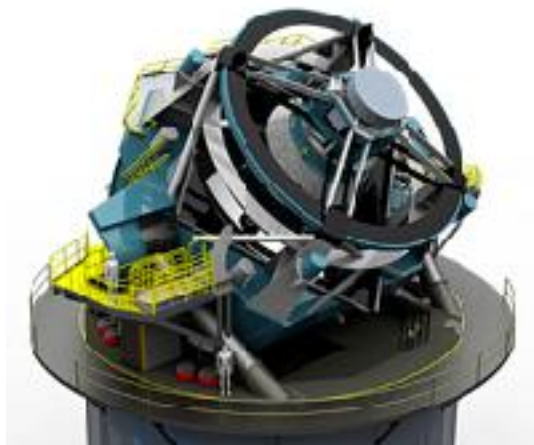
$$\text{Data} \longrightarrow y = L(p)x + n$$

Lens Parameters (non-linear)

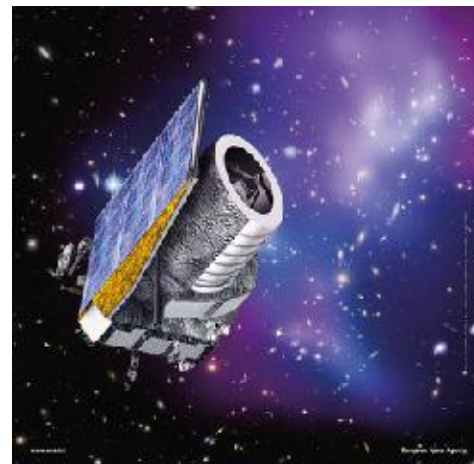
Noise

LOOKING INTO THE FUTURE

In the next few years, we're expecting to discover more than 170,000 new lenses.



LSST



euclid
consortium



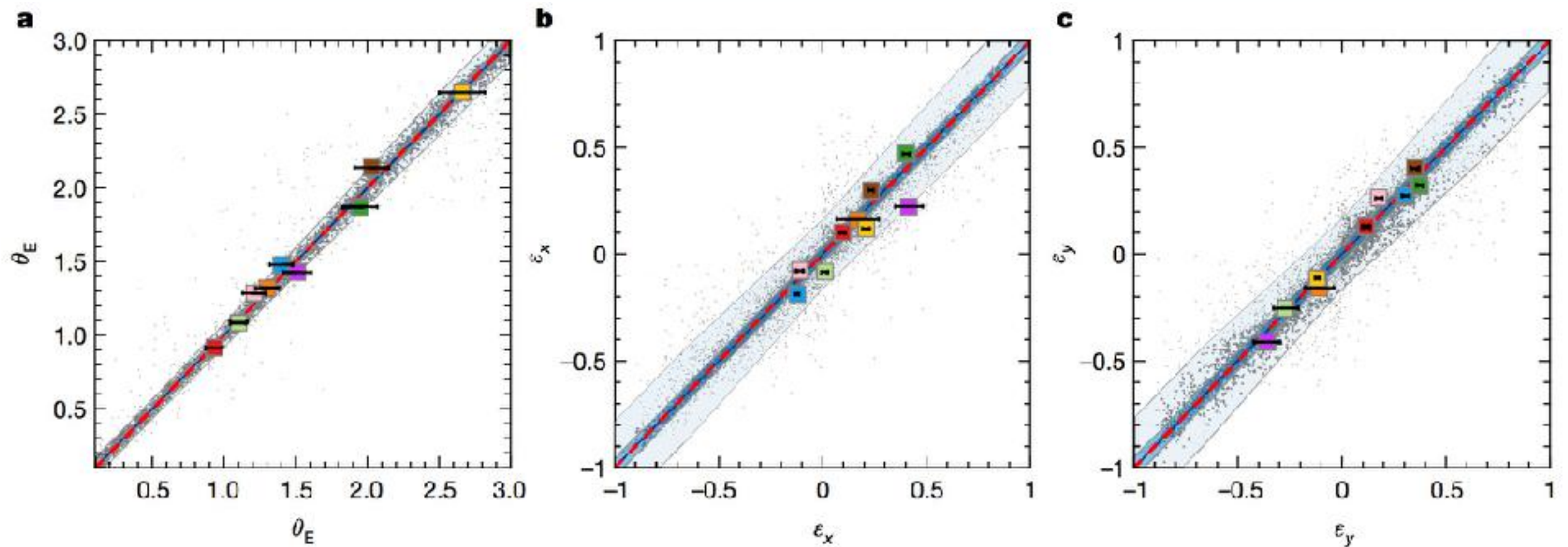
NANCY GRACE
ROMAN
SPACE TELESCOPE

Methods for the future:

How are we going to analyze 170,000 lenses?

- Lens modeling is **very slow**.
- Simple lens model takes ~3 days
=> **1,400 years !**

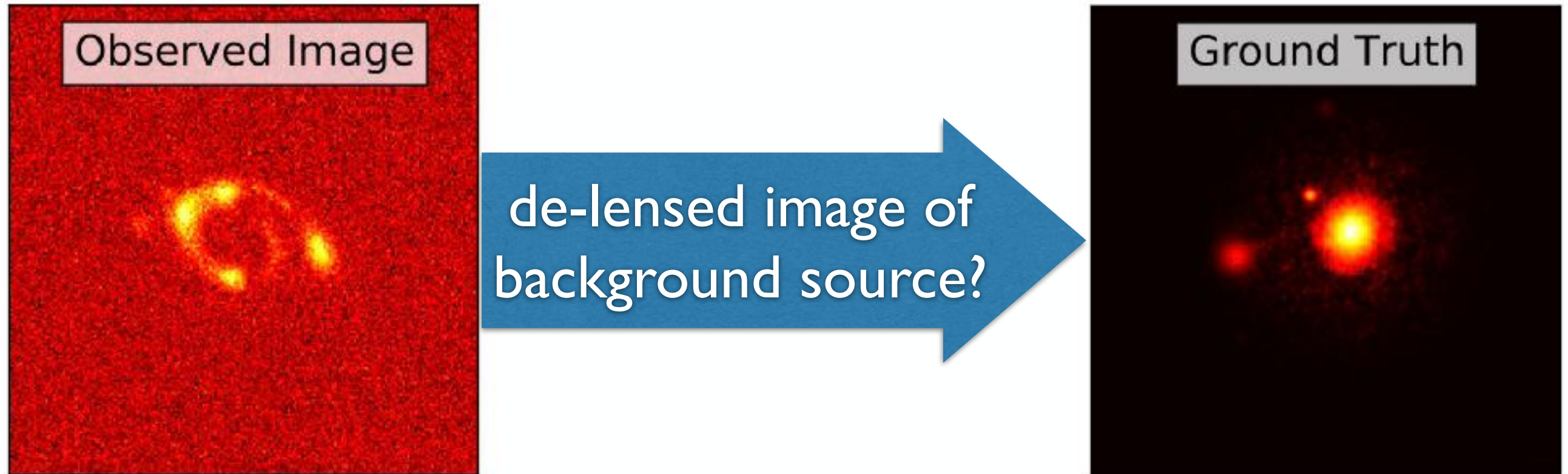
ESTIMATING THE MATTER DISTRIBUTION PARAMETERS WITH CNNs



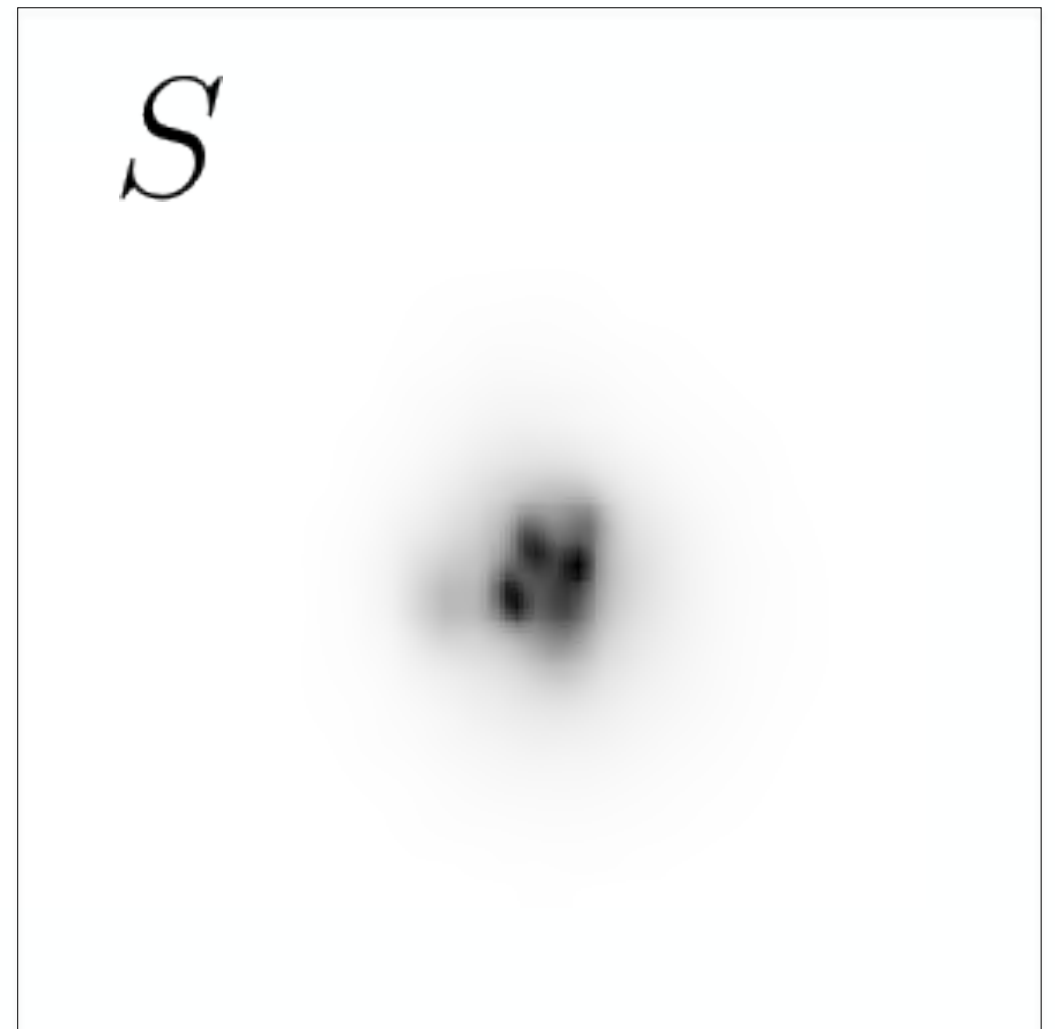
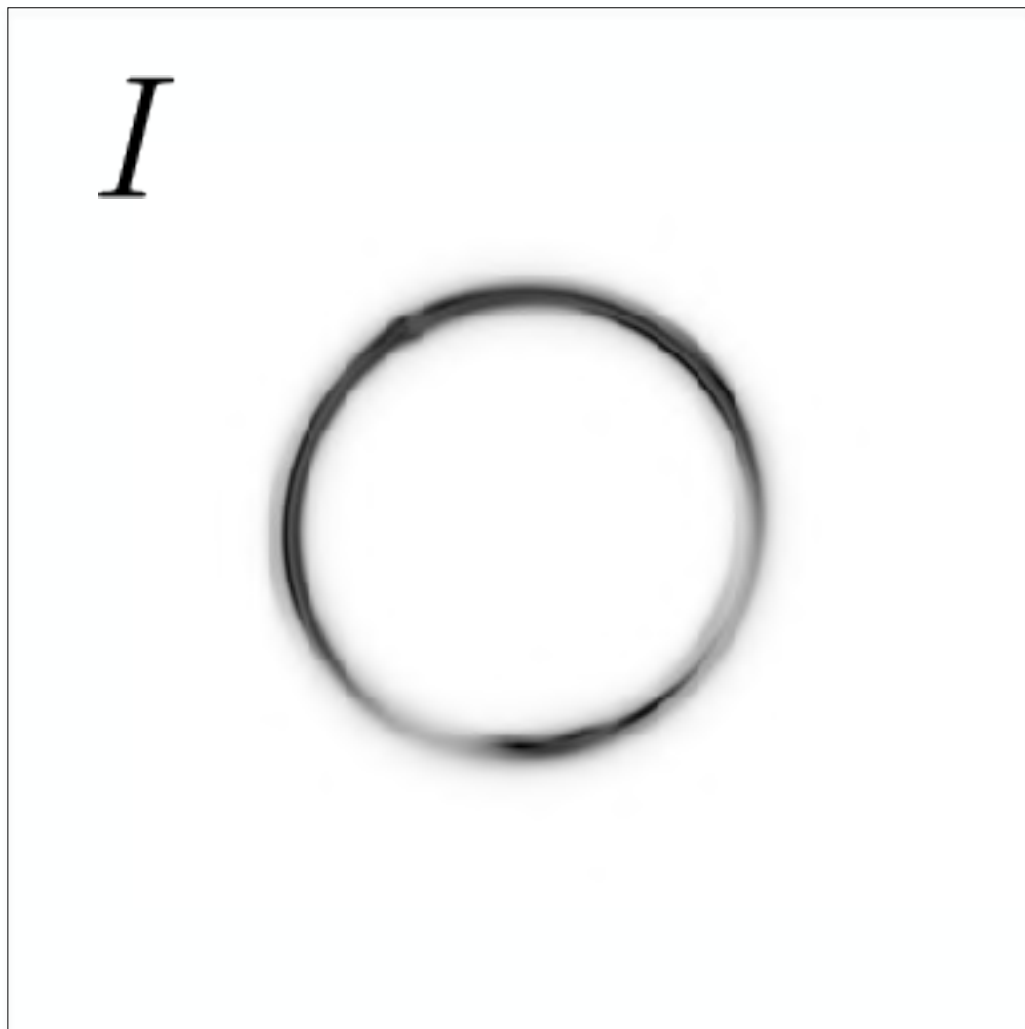
10 million times faster than traditional lens modeling.

0.01 seconds on a **single GPU**

UNDISTORTED IMAGE OF THE BACKGROUND SOURCE

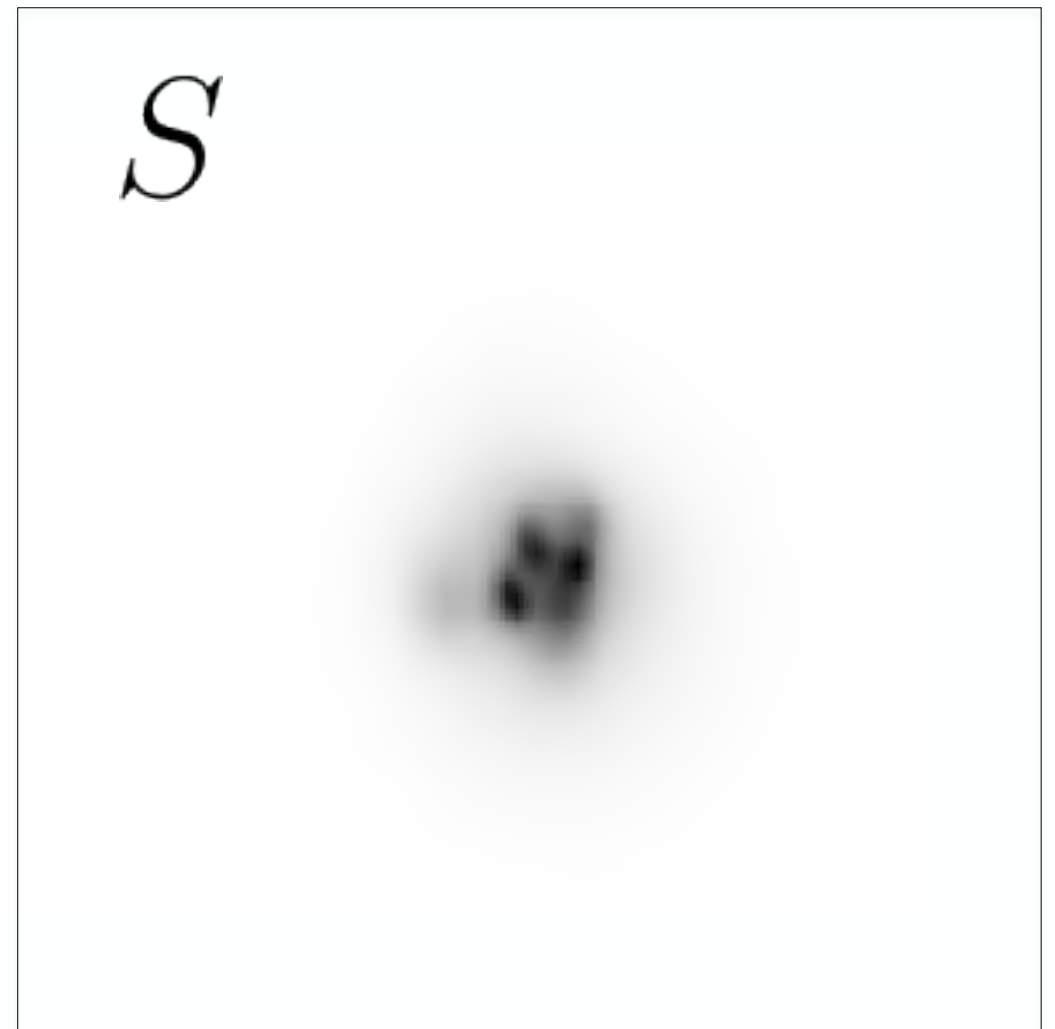
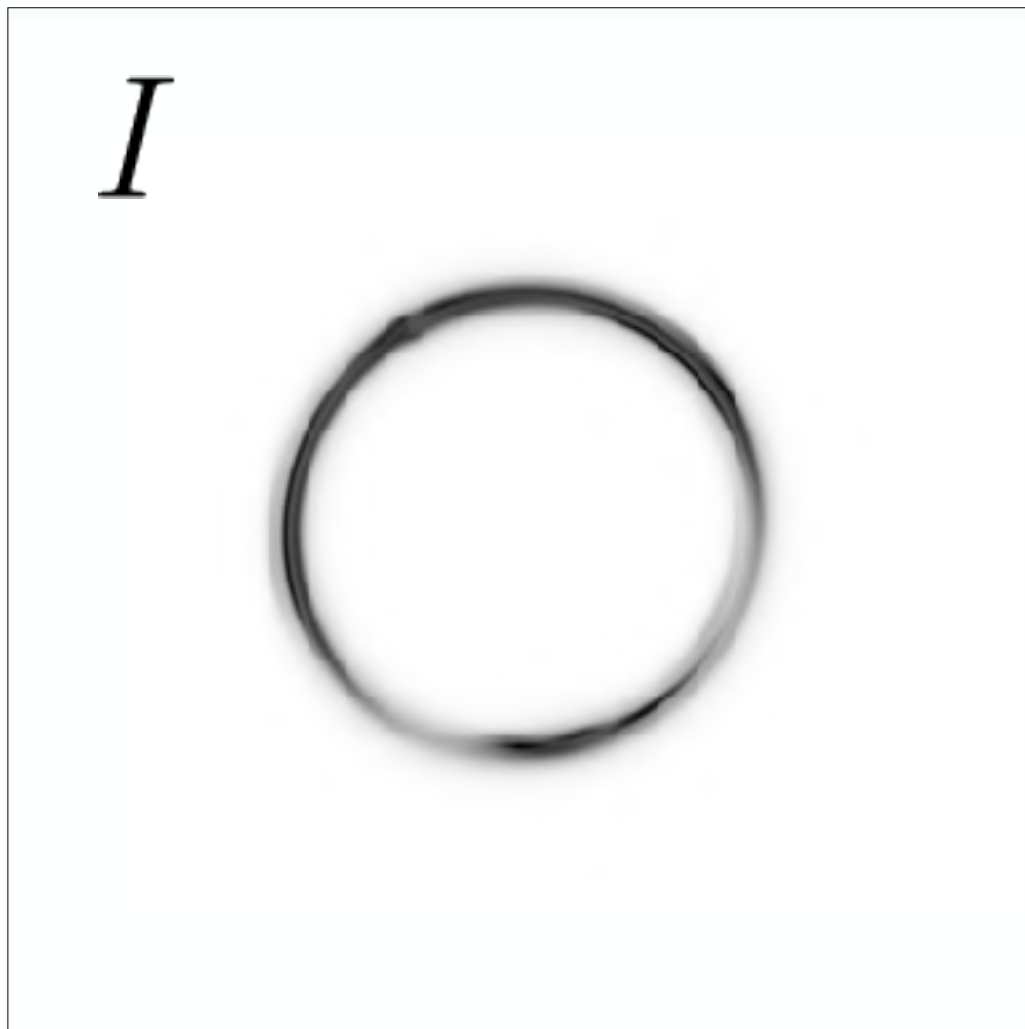


PIXEL VALUES OF THE BACKGROUND SOURCE ARE LINEAR
PARAMETERS



$$I = L(p)S$$

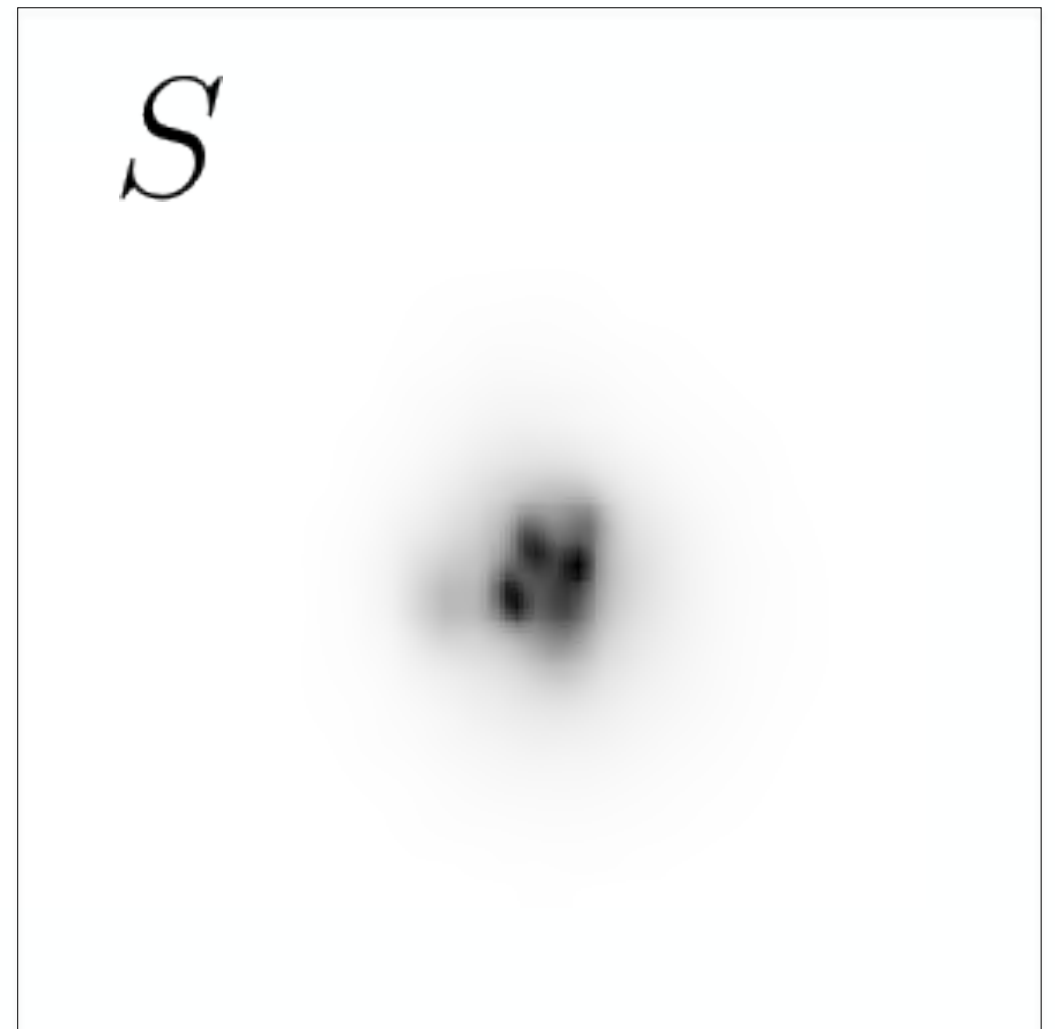
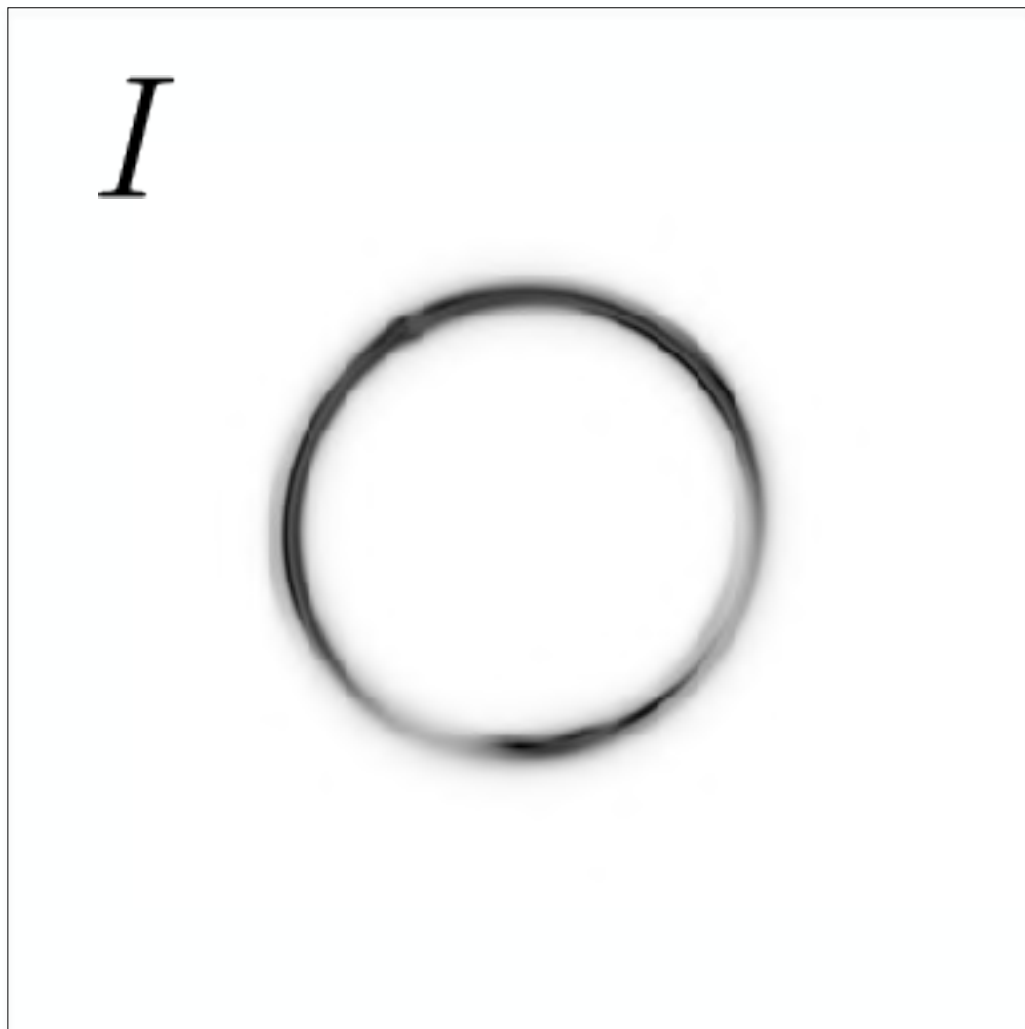
PIXEL VALUES OF THE BACKGROUND SOURCE ARE LINEAR
PARAMETERS



$$I = L(p)S$$

$$S = (L^T C_N^{-1} L)^{-1} L^T C_N^{-1} D$$

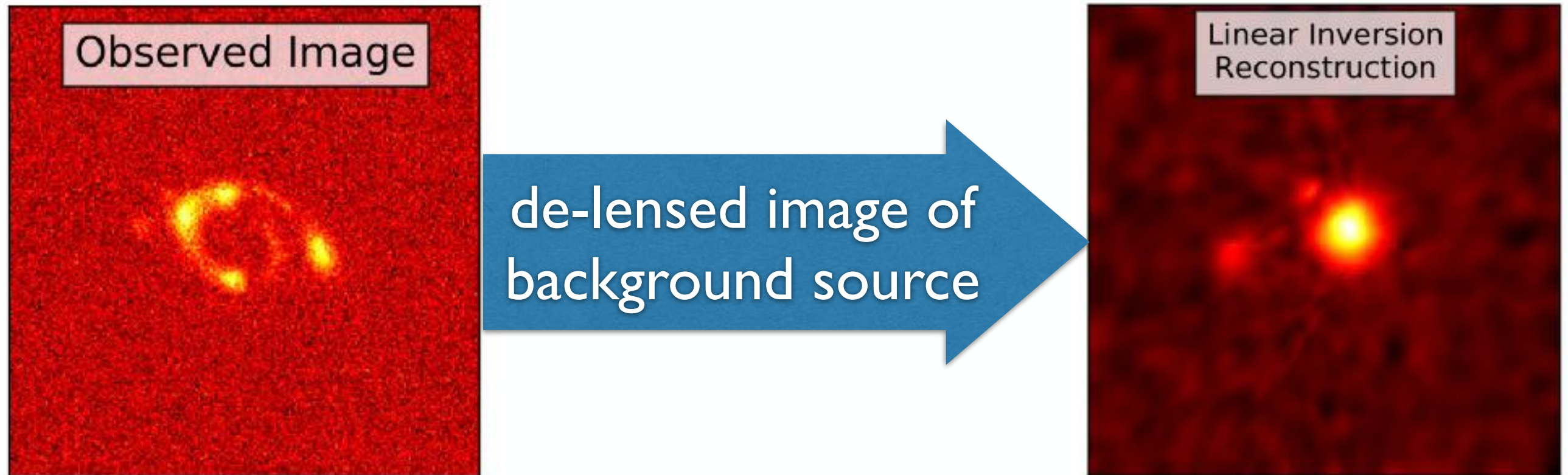
PIXEL VALUES OF THE BACKGROUND SOURCE ARE LINEAR
PARAMETERS



$$I = L(p)S$$

$$S = (L^T C_N^{-1} L + C_p^{-1})^{-1} L^T C_N^{-1} D$$

UNDISTORTED IMAGE OF THE BACKGROUND SOURCE



$$S = (L^T C_N^{-1} L + C_p^{-1})^{-1} L^T C_N^{-1} D$$

THE RECURRENT INFERENCE MACHINE

The RIM is designed to solve problems of the form:

$$\mathbf{y} = \mathbf{f}(\mathbf{x}) + \mathcal{N}$$

In this model, assuming the noise is Gaussian, the likelihood of \mathbf{y} given \mathbf{X} is:

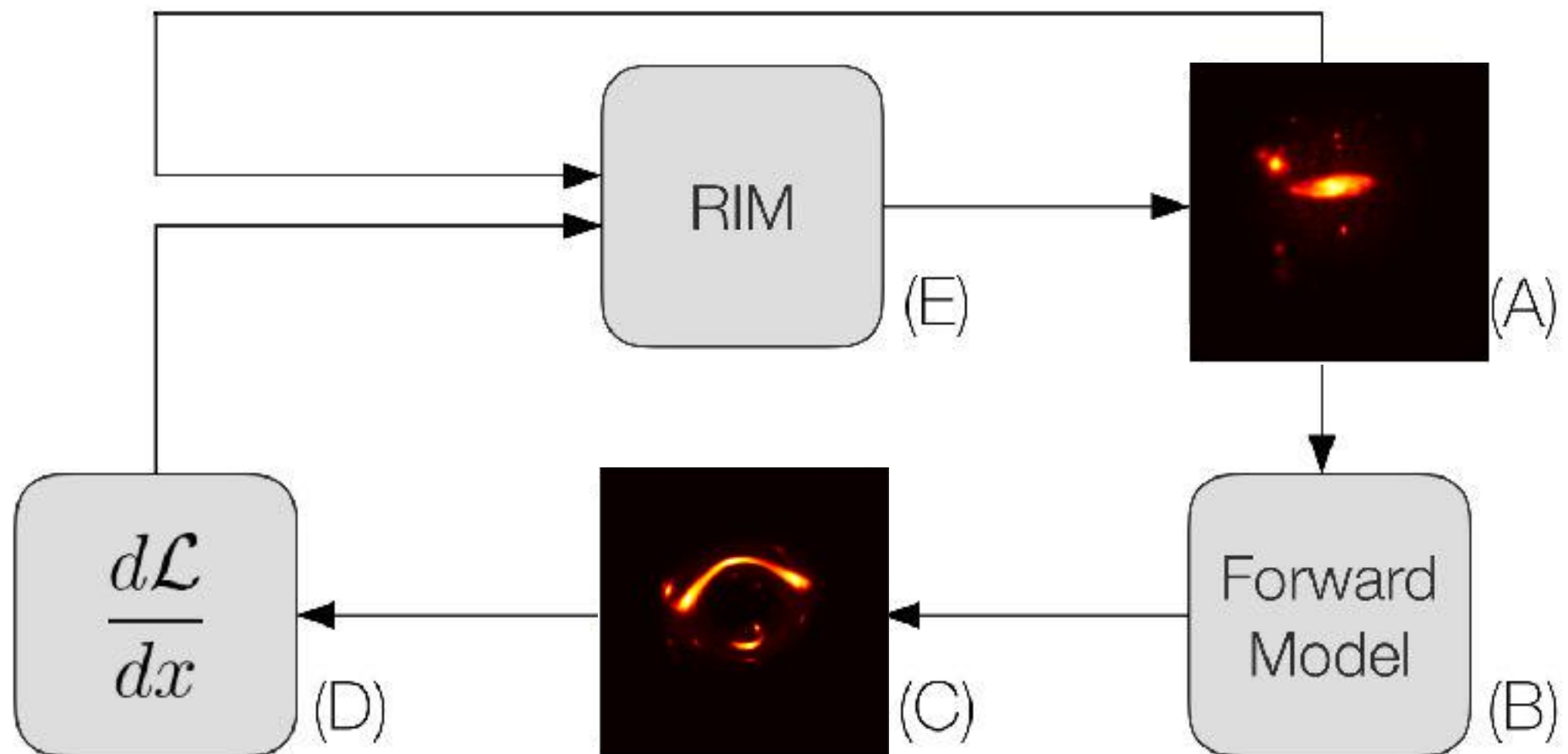
$$\mathcal{L}(\mathbf{y}|\mathbf{x}) \propto \exp \left[-\frac{1}{2} (\mathbf{y} - \mathbf{f}(\mathbf{x}))^T \mathbf{C}_{\mathcal{N}}^{-1} (\mathbf{y} - \mathbf{f}(\mathbf{x})) \right]$$

The RIM solves the above equation for \mathbf{X} recursively. At every time step, it takes its current estimate of \mathbf{X} , \mathbf{x}_t , and the gradient $\nabla_{\mathbf{x}} \mathcal{L}|_{\mathbf{x}_t}$ to output an update to the estimate $\Delta \mathbf{x}_t$ so that:

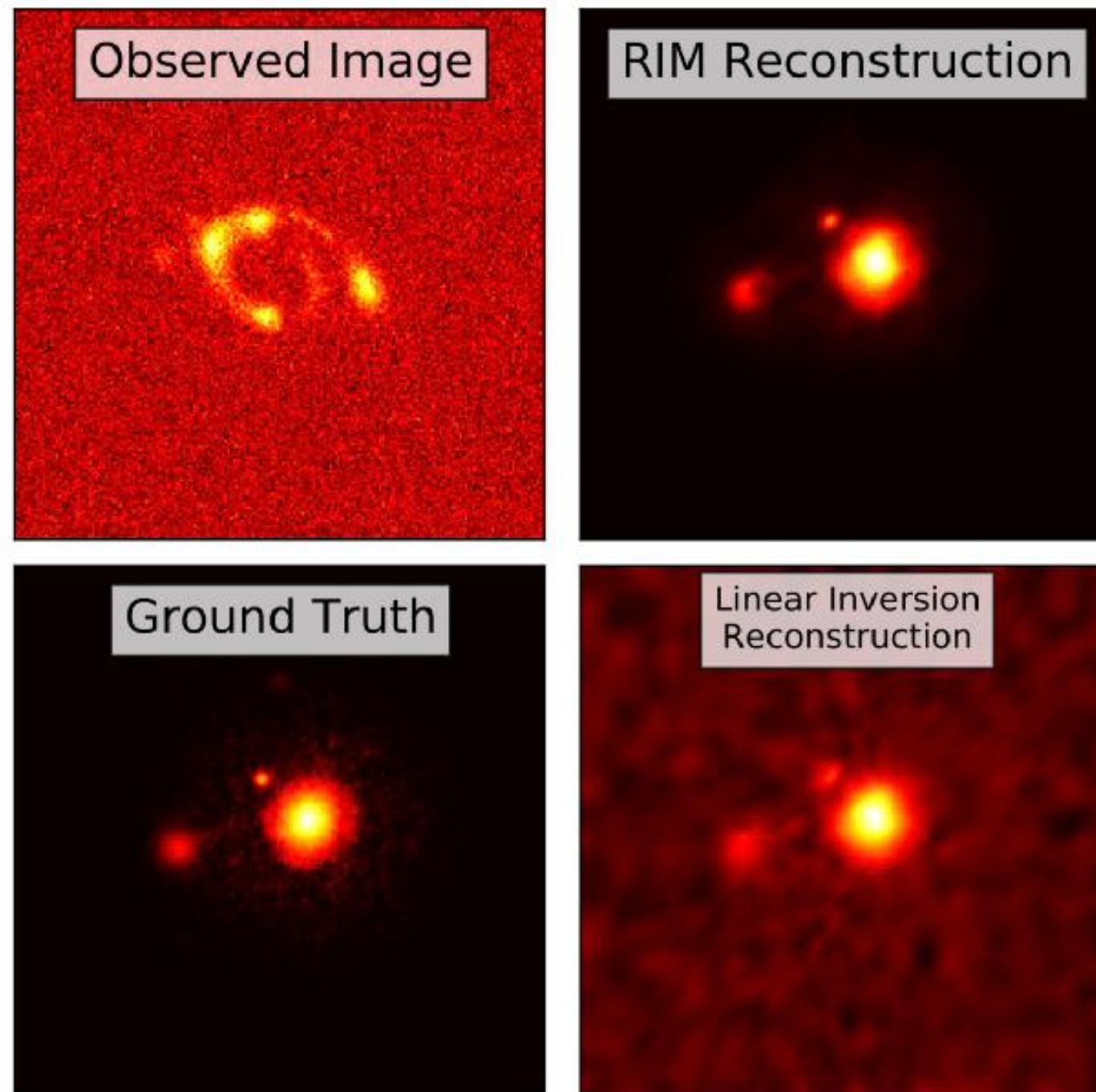
$$\mathbf{x}_{t+1} = \mathbf{x}_t + \Delta \mathbf{x}_t$$

=> very similar idea to what a downhill optimizer does

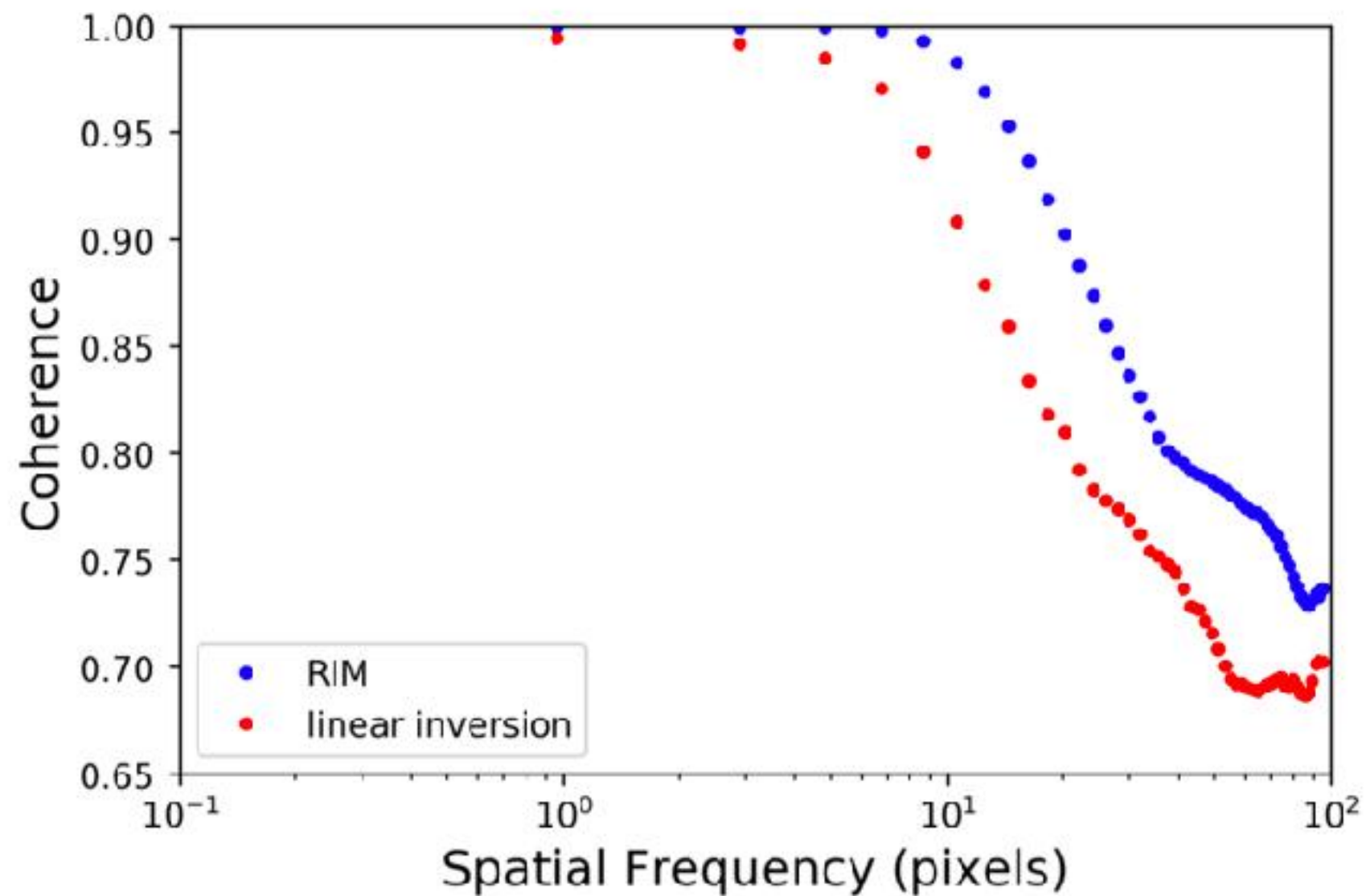
ESTIMATING THE BACKGROUND SOURCE IMAGES WITH THE RECURRENT INFERENCE MACHINE



UNDISTORTED IMAGE OF THE BACKGROUND SOURCE WITH THE RECURRENT INFERENCE MACHINE (RIM)

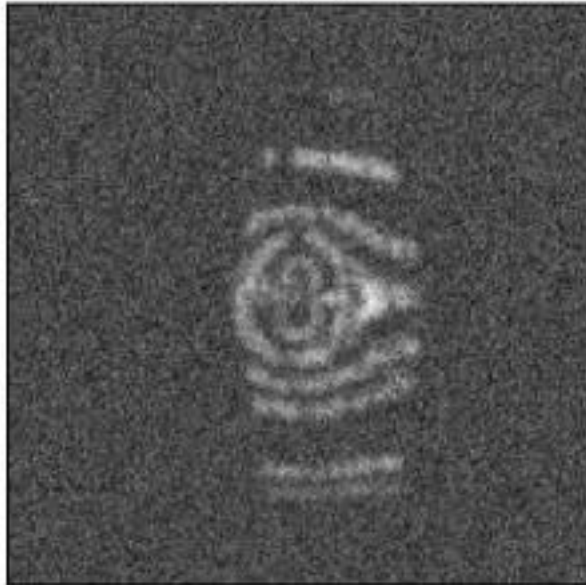


BACKGROUND SOURCE RECONSTRUCTION: COMPARISON TO MAXIMUM LIKELIHOOD METHODS

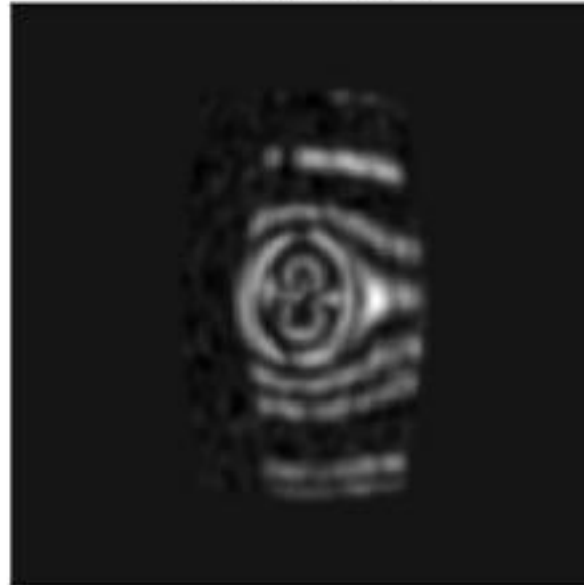


EXAMPLES OUTSIDE THE TRAINING DATA

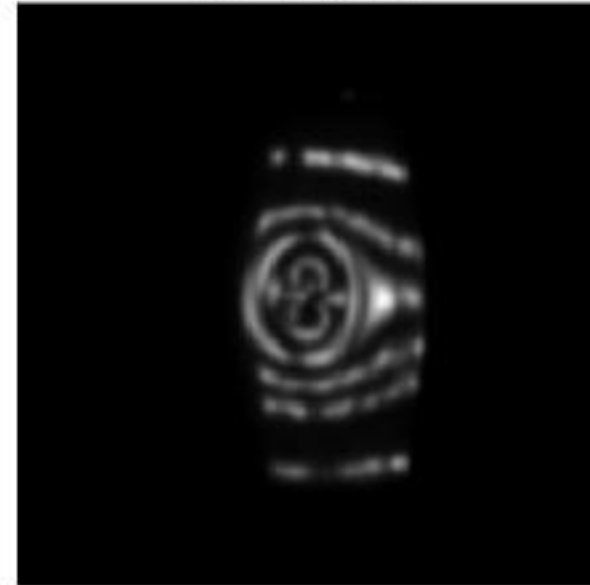
Data



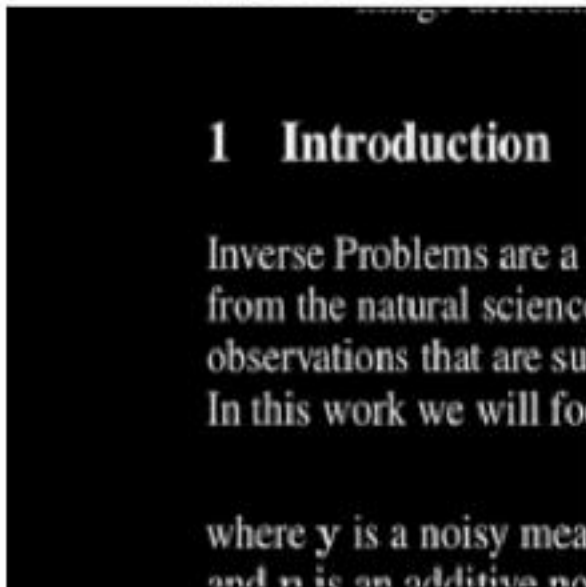
Linear Model



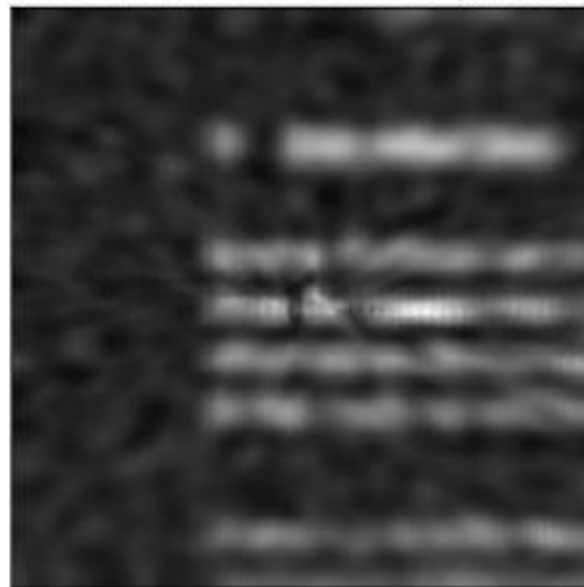
RIM Model



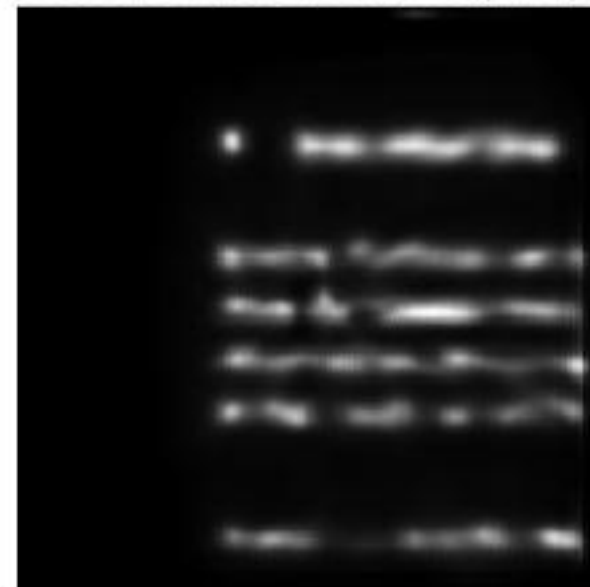
True Source

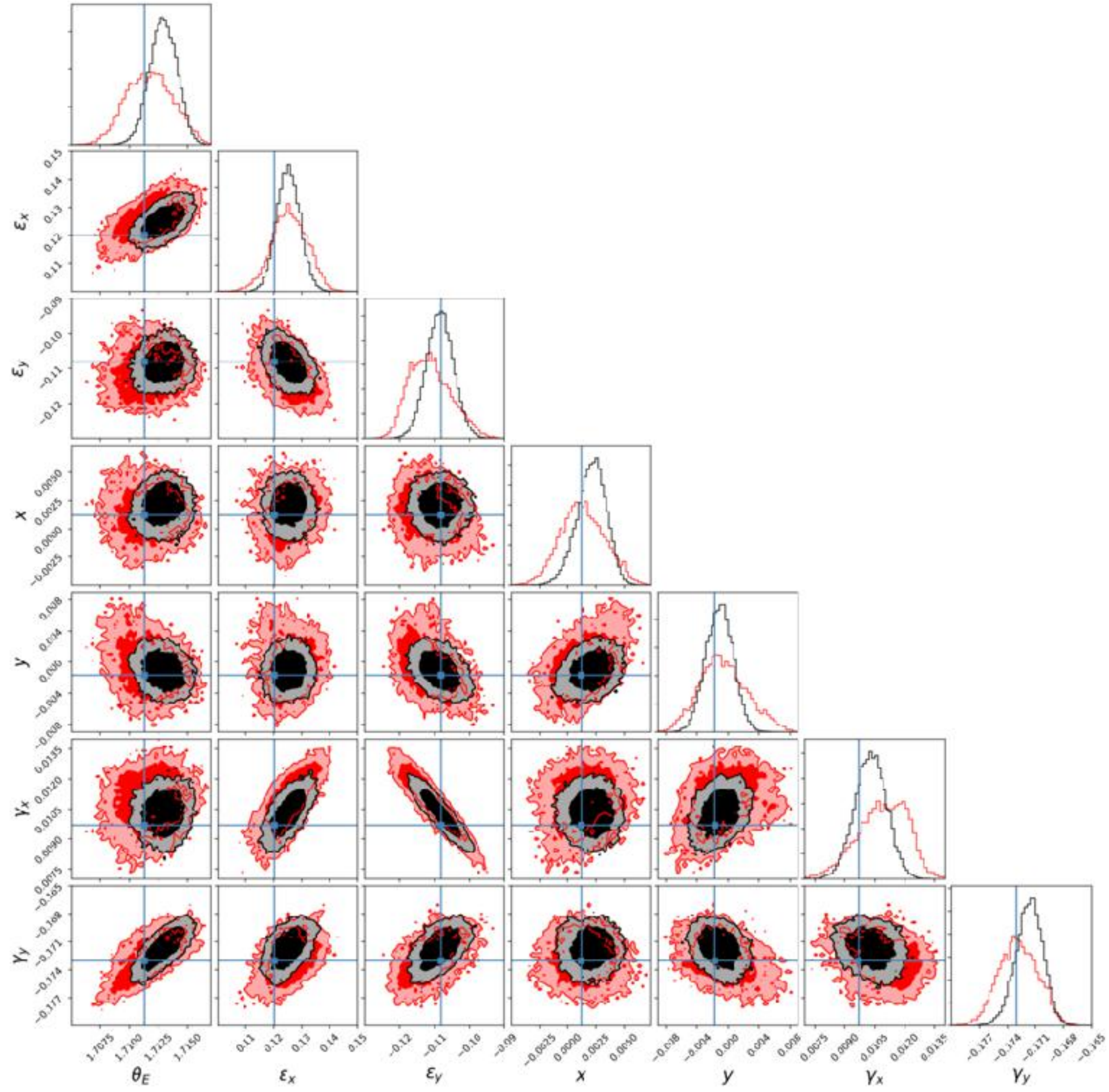


Reconstructed Source (Linear)



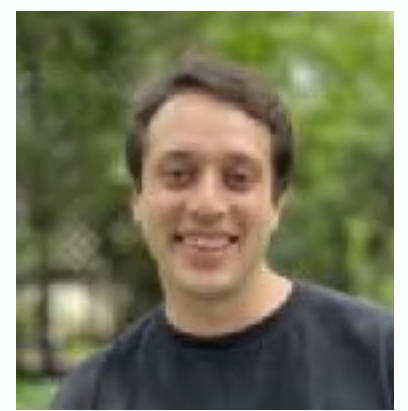
Reconstructed Source (RIM)



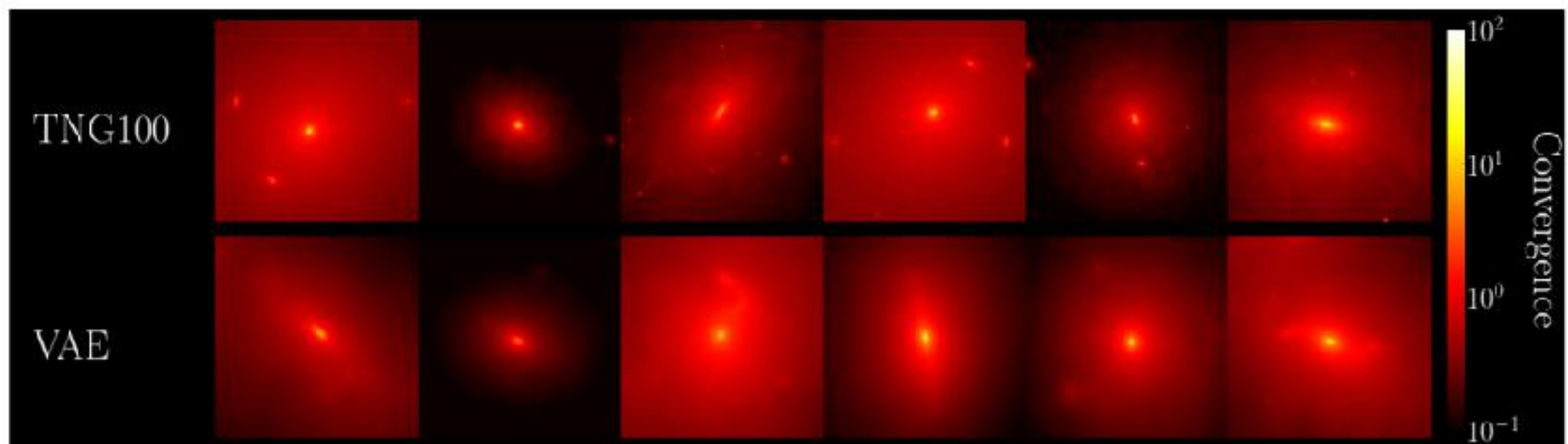




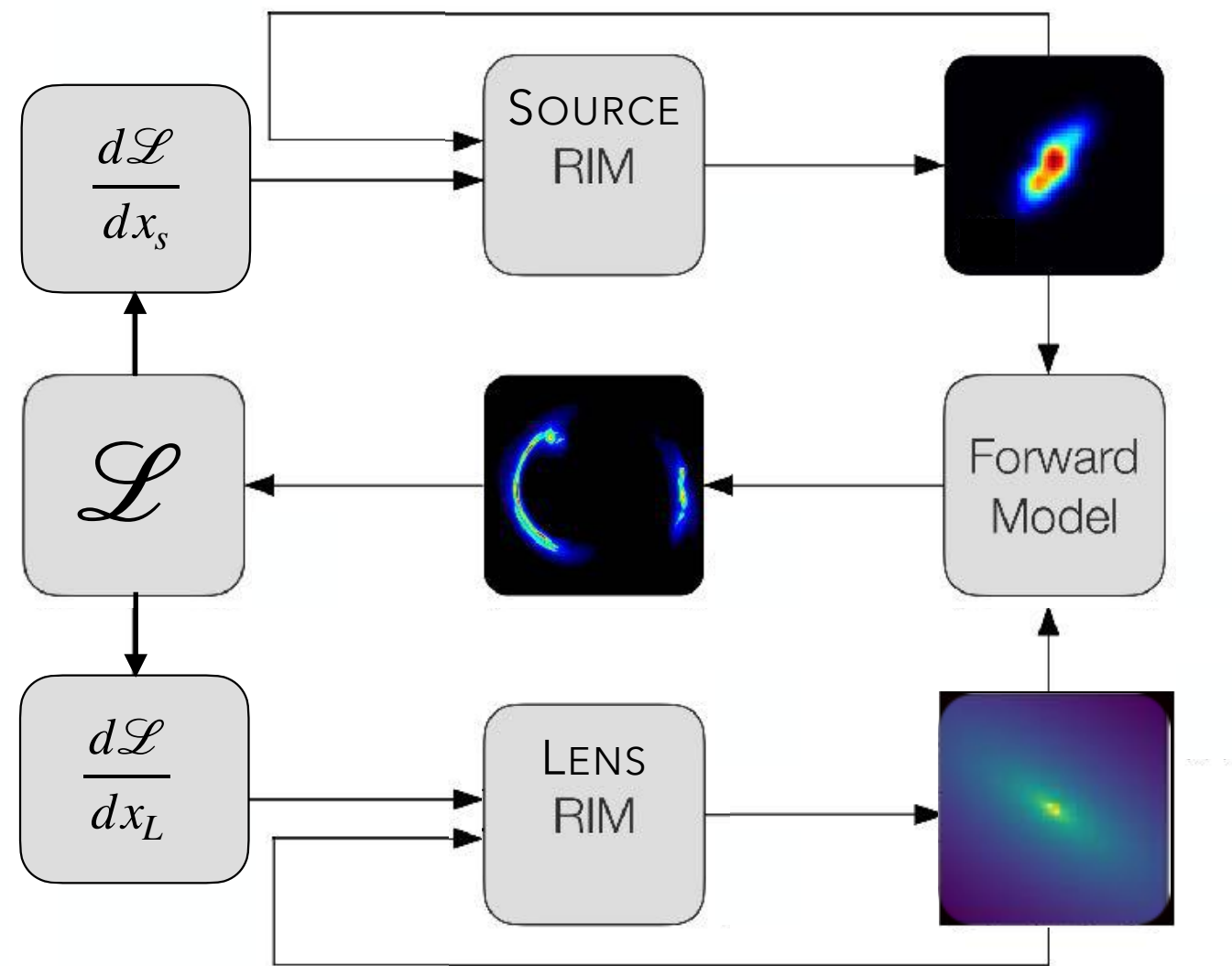
SIMULATED GALAXIES GENERATED WITH A VARIATIONAL AUTOENCODER



Alexandre Adam



SOLVING ENTIRE LENSING SYSTEMS WITH THE RECURRENT INFERENCE MACHINE



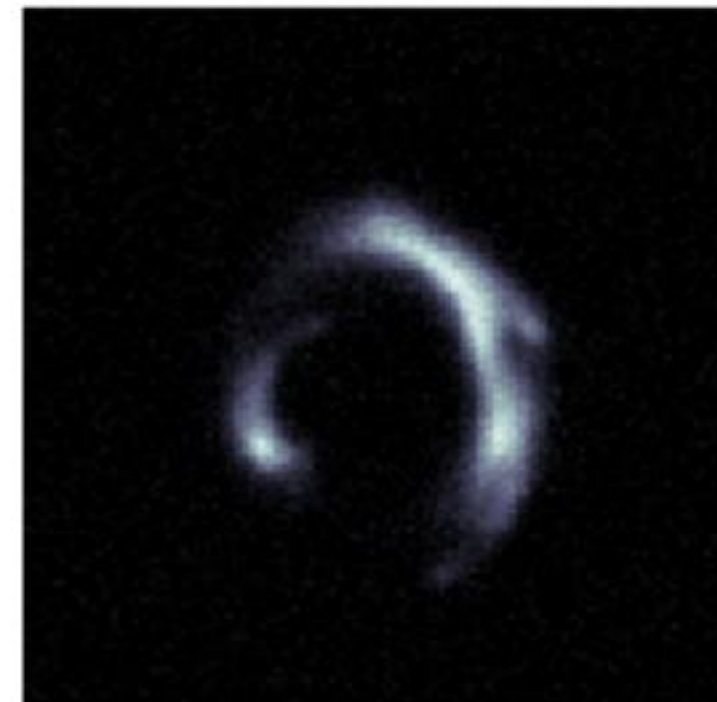
TRAINING ON HYDRODYNAMICAL SIMULATIONS

Background

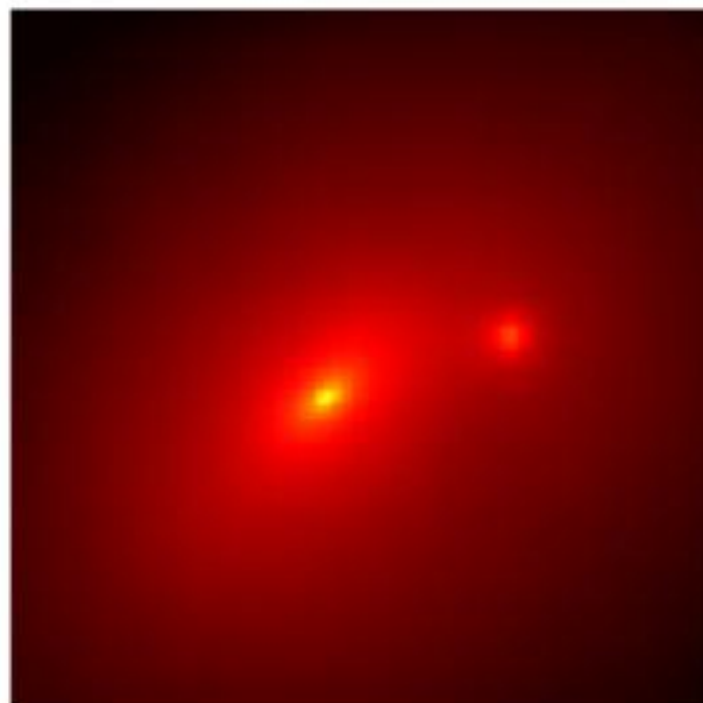
Foreground

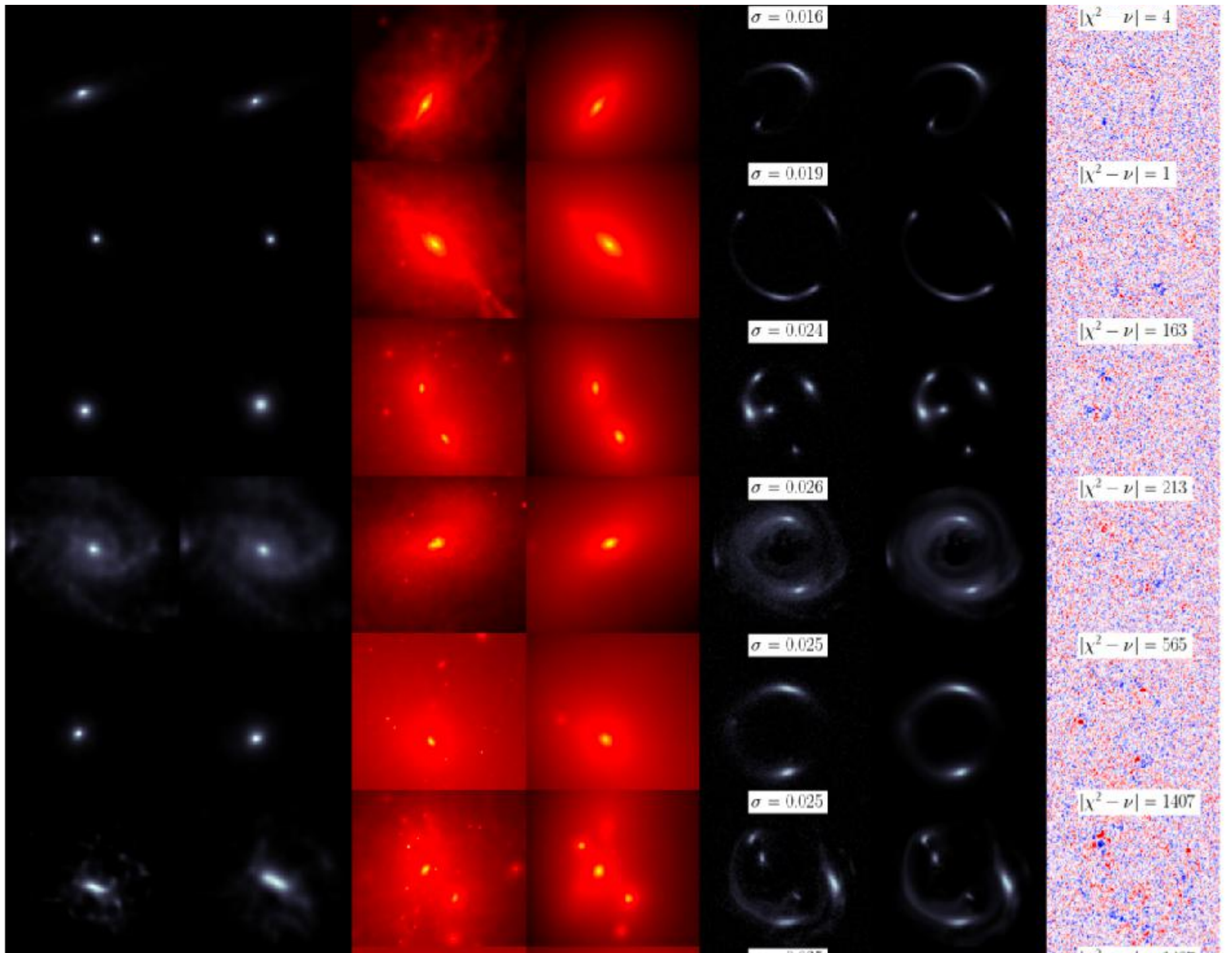
Lensed Image

Ground Truth

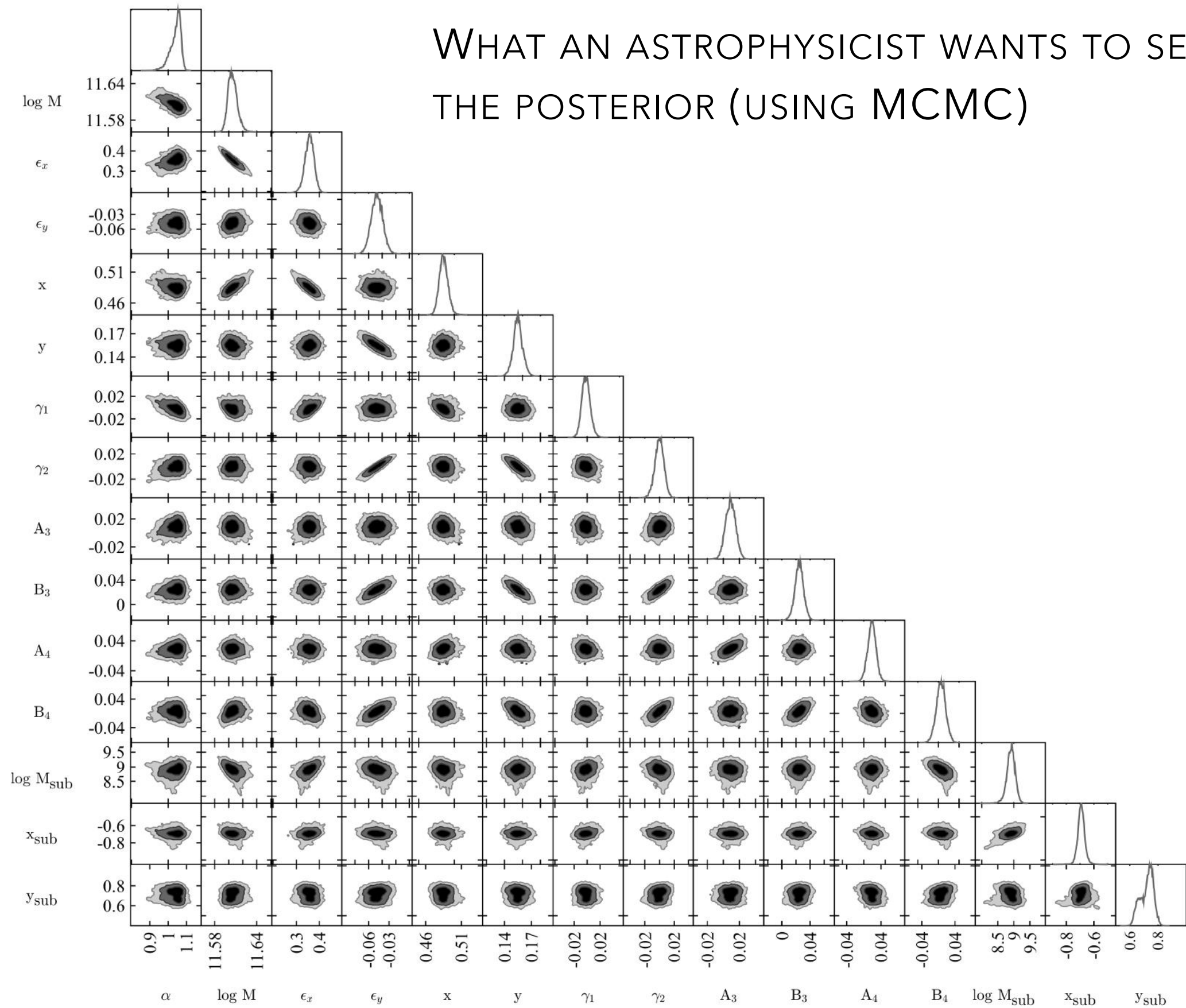


Prediction

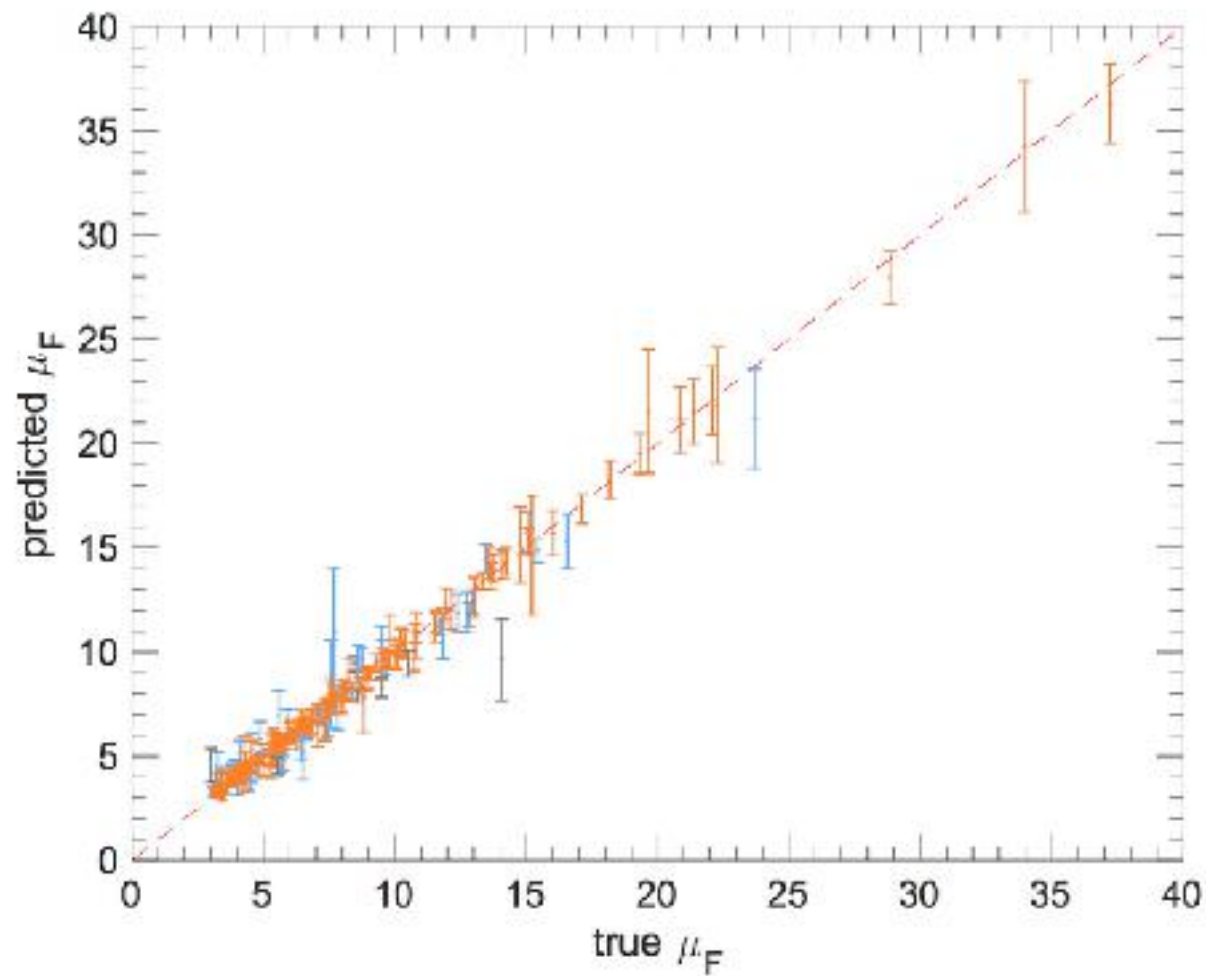




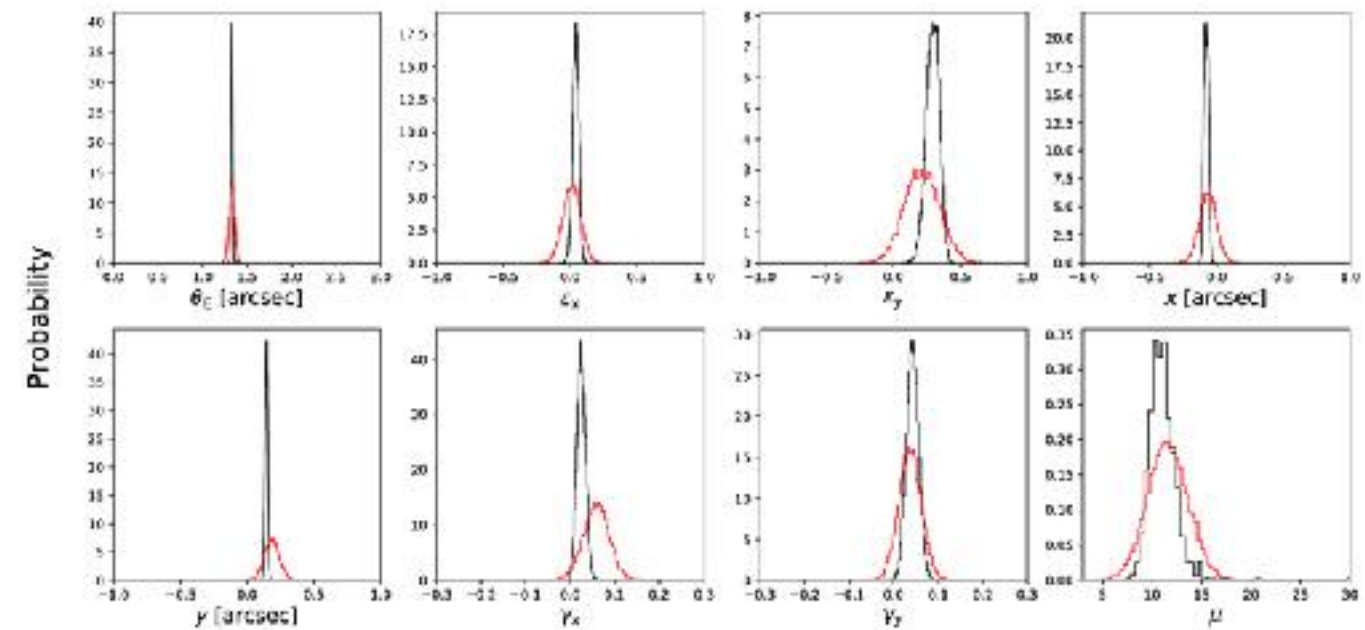
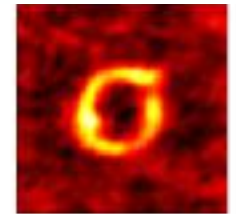
WHAT AN ASTROPHYSICIST WANTS TO SEE: THE POSTERIOR (USING MCMC)



UNCERTAINTY ESTIMATION WITH APPROXIMATE BAYESIAN NEURAL NETWORKS



Max-likelihood lens modeling (black)
Neural Networks (red)



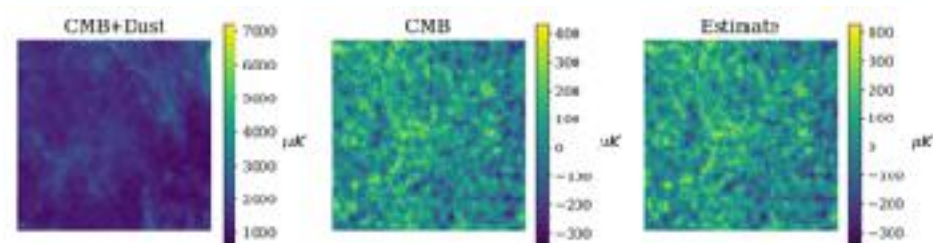
Variational Inference to Approximate Bayesian Neural Networks

Pros:

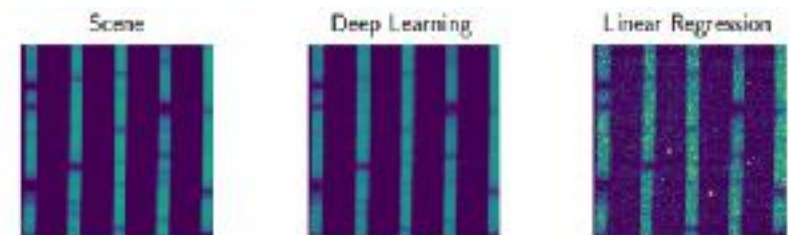
- ▶ Amortized.
- ▶ Requires few hundred forward passes at evaluation time (to collect samples). Still very fast.
- ▶ Marginalizes implicitly over parameters we do not wish to explicitly model.
- ▶ With good coverage probabilities, one can use importance sampling of the output distribution to get an unbiased posterior. (Provided one can actually write this posterior)

Caveats:

- ▶ The variational distributions (Bernoulli) are extremely simplistic, therefore even if we attempt to use them to approximate the true weight distributions, that approximation could be bad and yield inaccurate uncertainties.



CMB Cleaning



IR Spectrometer De-noising

Same problem remains regardless of the variational distribution used: there is no way of quantifying how well we approximate the true weight distributions

Simulation-Based inference

Ground truth latent variable



$$P(\theta | \hat{\theta}_x)$$



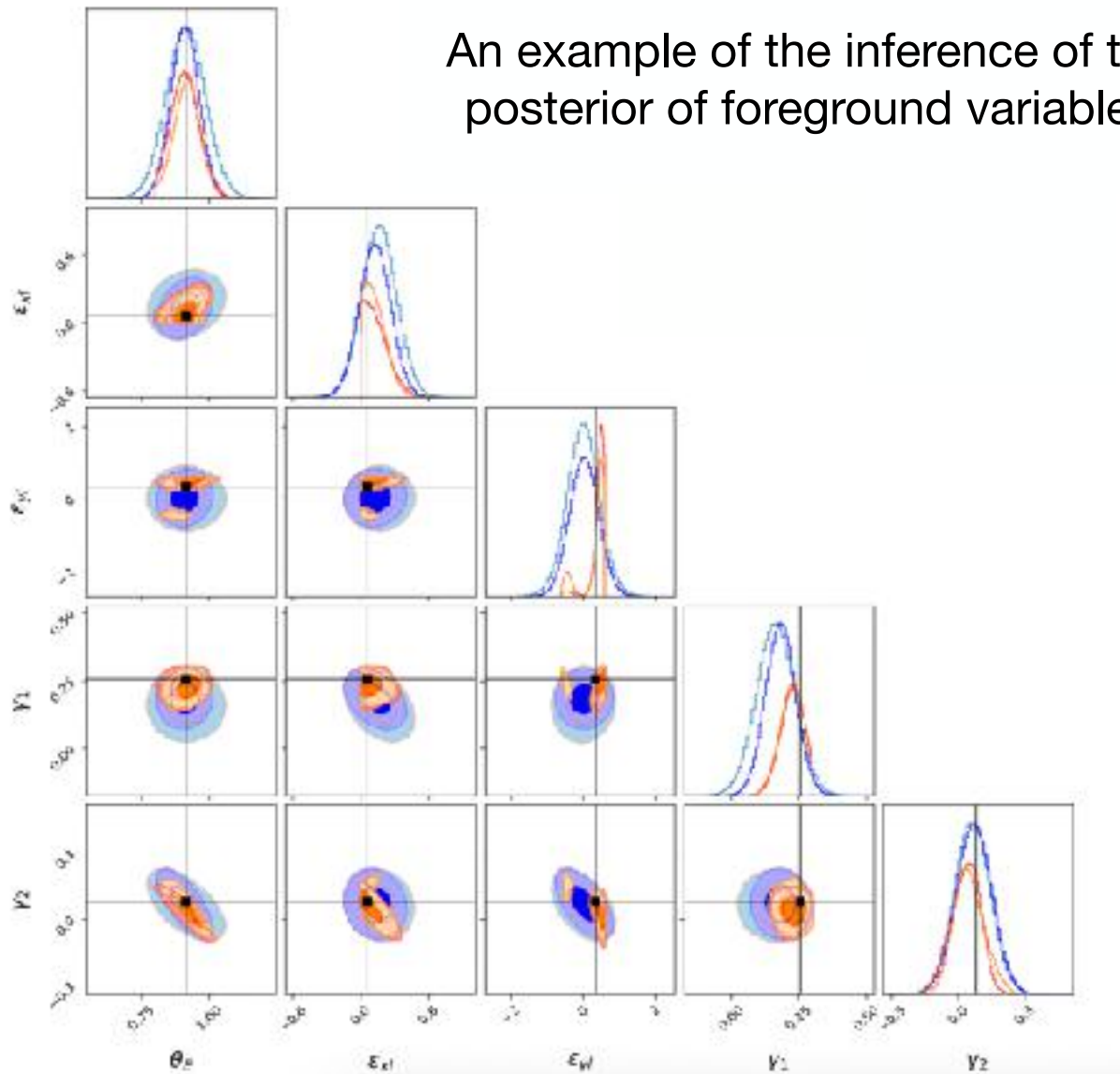
Ronan
Legin

UNCERTAINTY ESTIMATION WITH SIMULATION-BASED INFERENCE METHODS

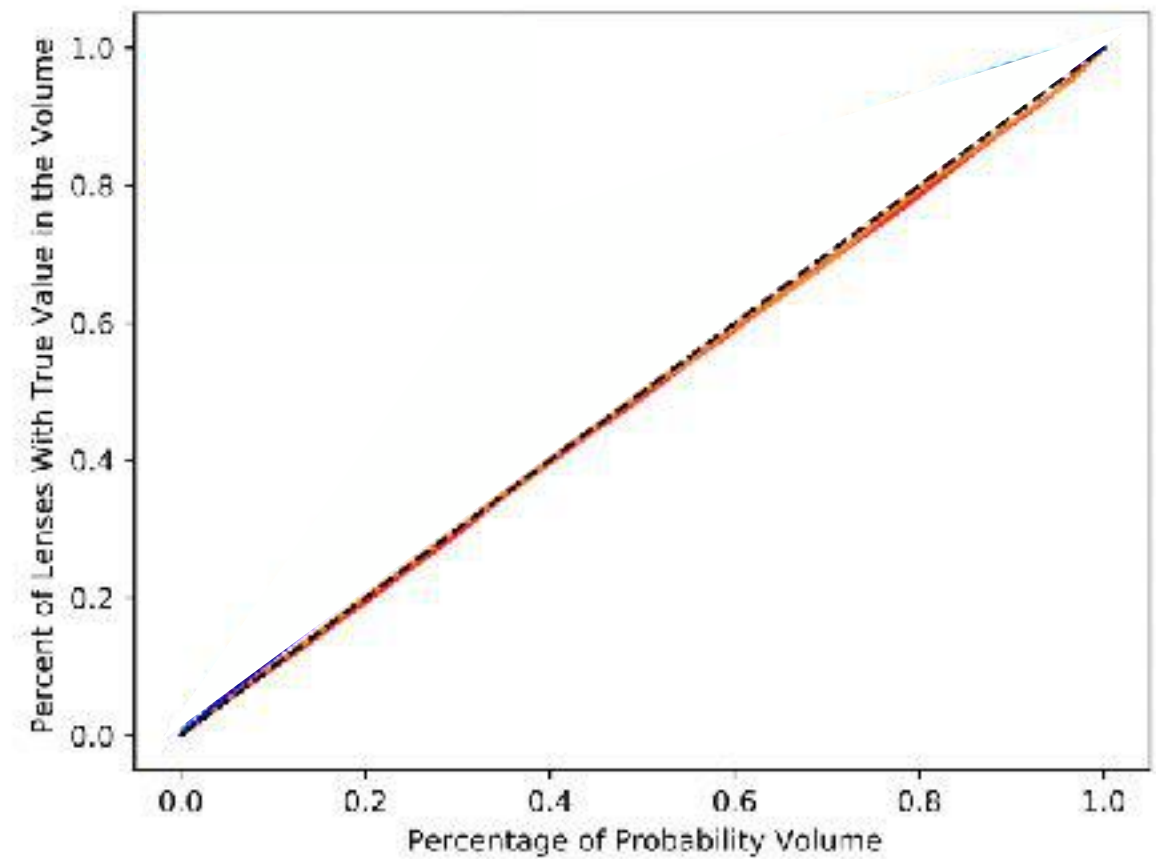


Ronan Legin

An example of the inference of the posterior of foreground variables



Coverage probabilities



UNCERTAINTY ESTIMATION WITH SIMULATION-BASED INFERENCE METHODS

Pros:

- ▶ Use the **power of ML to find a compress statics**, and even if it is biased, we can get unbiased error estimate, the only drawback would be sub-optimal precision. (Provided the simulation pipeline is accurate!)
- ▶ A well-defined statistical framework that can: be relatively **fast**, deal with **complex distributions**, model **joint posteriors**.
- ▶ Use a neural density estimator to get the joint distribution $p(\text{data}, \text{parameter})$, no need for the epsilon parameter in ABC.
- ▶ Can **change the prior** from data point to data point without retraining the ML compressor.
- ▶ Once we have the posterior, can **generate samples** that are consistent with data (this is really important for 'interrogating the black box')

Caveats:

- ▶ Hard to marginalize implicitly over parameters, we need to **explicitly** model them.
- ▶ We don't model the uncertainty of the density estimator itself. (But it's a fairly simple ML model, and except for very pathological problems it's reasonable to expect that we are in interpolation mode).
- ▶ Limited to **low-dimensional posteriors** (10s maximum).
- ▶ Requires an **accurate simulation pipeline**.

Hierarchical Bayesian inference

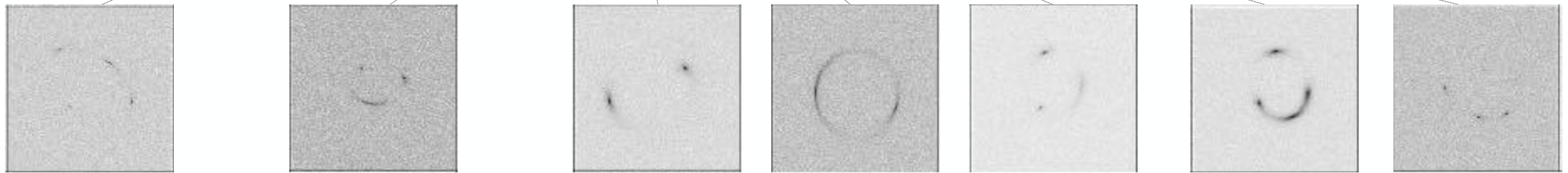
$$p(\lambda|\{x_i\}) = \frac{p(\lambda) \prod_i p(x_i|\lambda)}{\int d\lambda' p(\lambda') \prod_i p(x_i|\lambda')}$$

$$p(x_i|\lambda) = \int p(x_i|\theta)p(\theta|\lambda)d\theta$$

Posterior of individual measurements

We are interested in the parameters of the hyper distribution,

Latent variable



Hierarchical Bayesian inference

$$p(\lambda|\{x_i\}) = \frac{p(\lambda) \prod_i p(x_i|\lambda)}{\int d\lambda' p(\lambda') \prod_i p(x_i|\lambda')}$$

~~$$p(x_i|\lambda) = \int p(x_i|\theta)p(\theta|\lambda)d\theta$$~~

$$p(x_i|\lambda) = \frac{\int p(x_i|\theta)p(\theta|\lambda)d\theta}{\alpha(\lambda)},$$

$$\alpha(\lambda) = \int p_{\det}(\theta)p(\theta|\lambda)d\theta$$

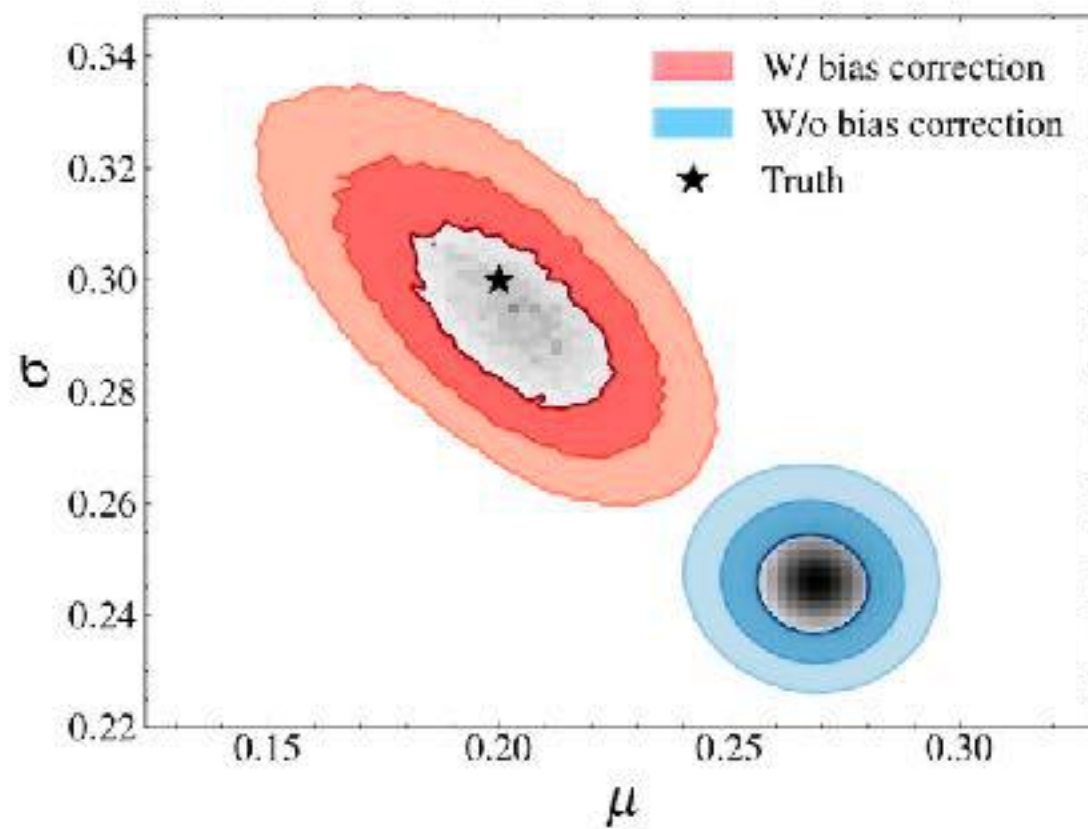
We are interested in the parameters of the hyper distribution,

Latent variable

$$p(\lambda|\{x_i\}) = \left[\int d\lambda' \frac{p(\lambda')}{p(\lambda)} \prod_i \frac{\mathbb{E}_{p(\theta|x_i)} \left[\frac{p(\theta|\lambda')}{p(\theta)\alpha(\lambda')} \right]}{\mathbb{E}_{p(\theta|x_i)} \left[\frac{p(\theta|\lambda)}{p(\theta)\alpha(\lambda)} \right]} \right]^{-1}$$



Hierarchical Bayesian inference



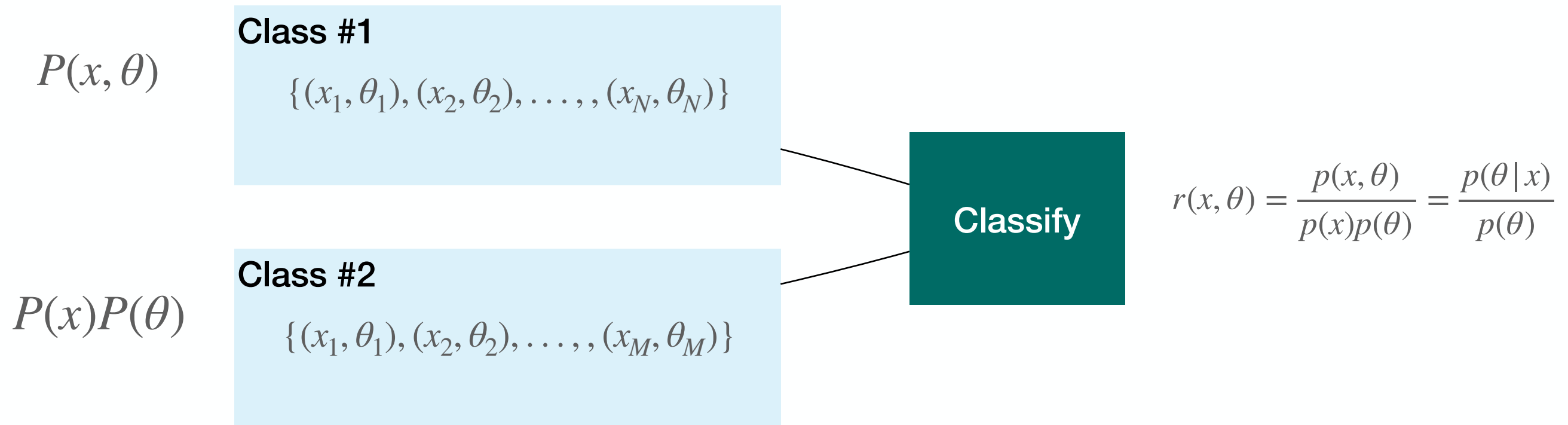
Ronan
Legin



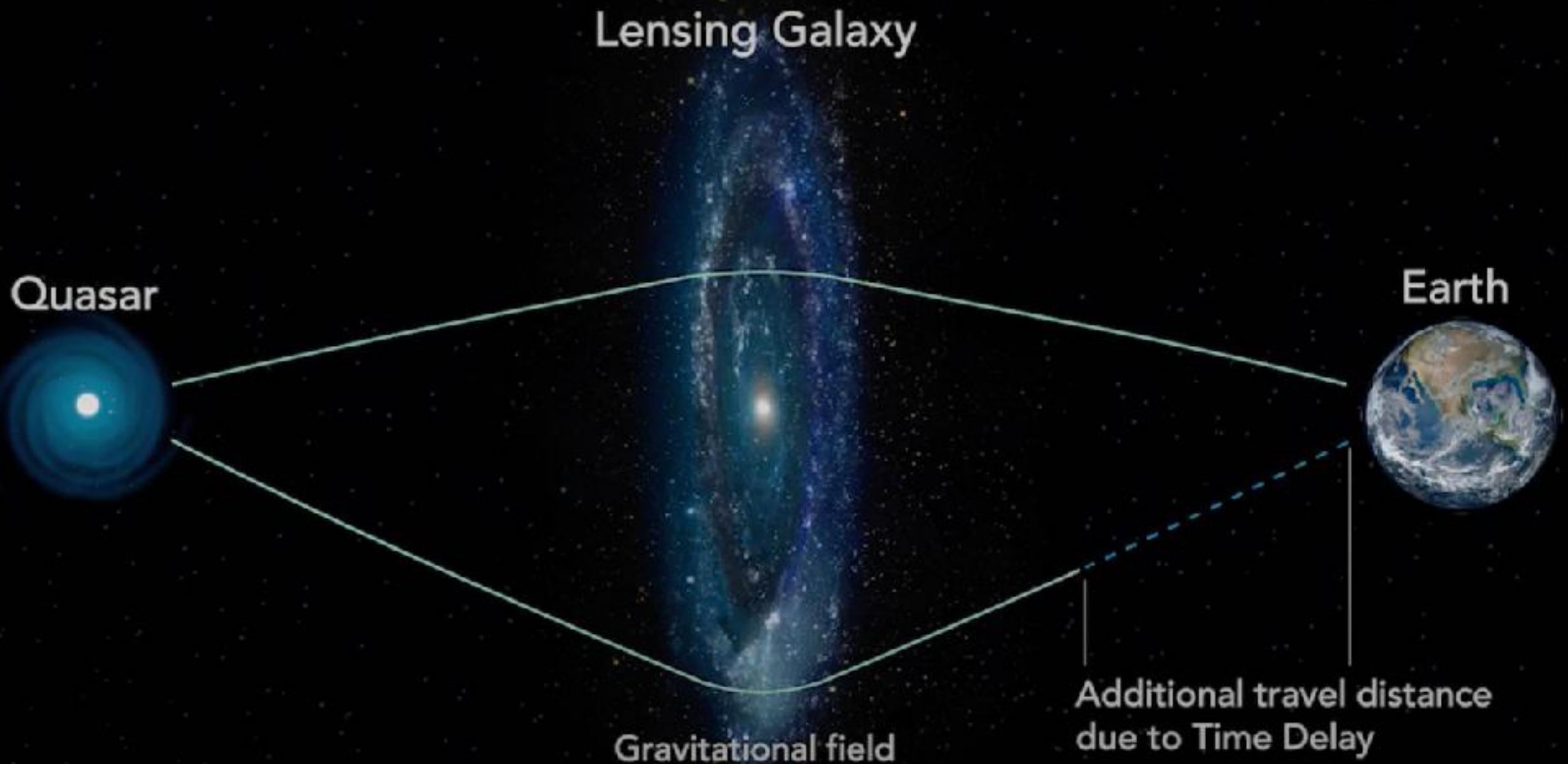
Connor
Stone

Legin, Stone, Hezaveh, Perreault Levasseur,
ICML 2022 - Machine Learning for
Astrophysics Workshop

Neural Ratio Estimators

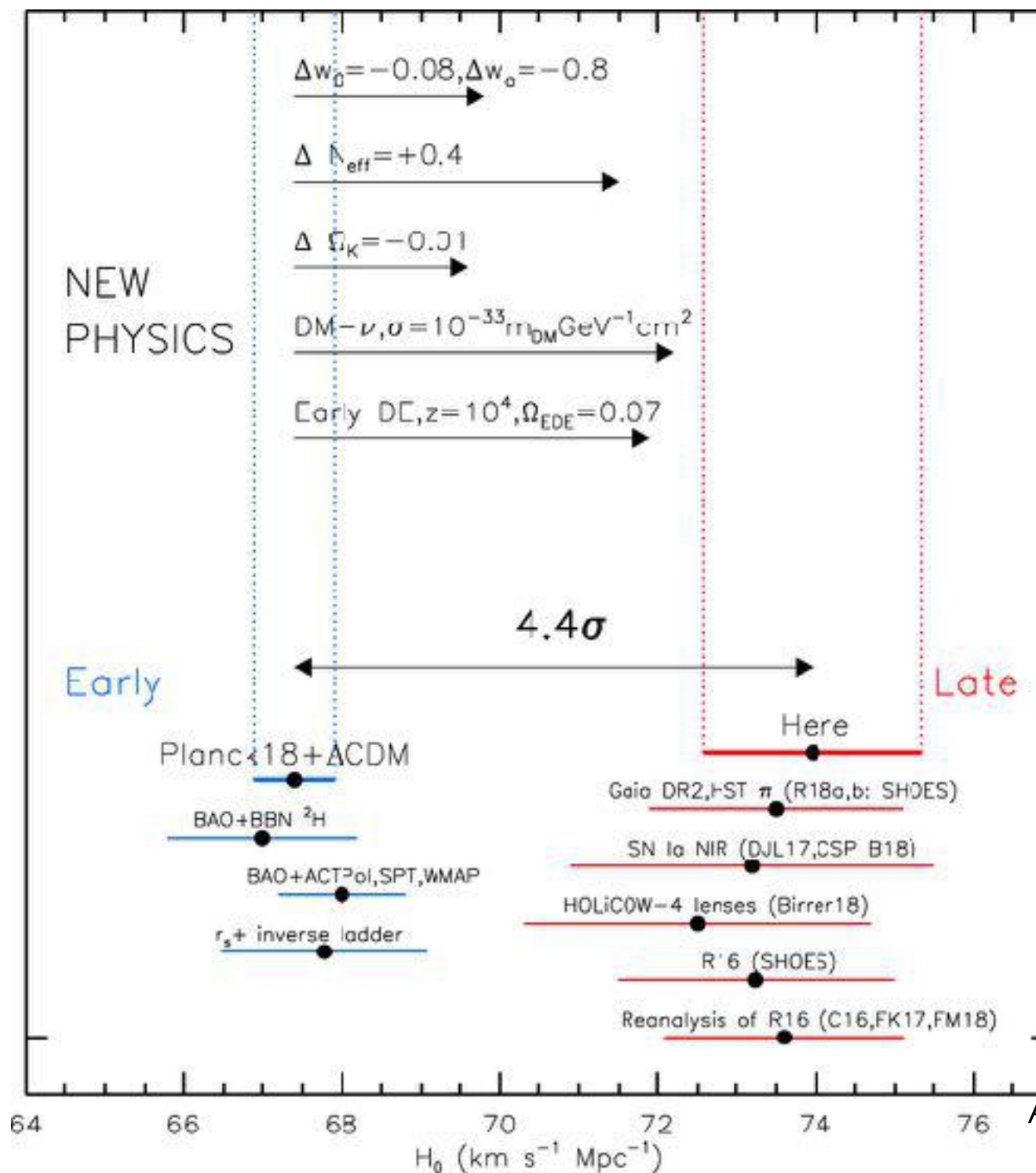


H0 INFERENCE WITH TIME DELAY COSMOGRAPHY



THE HUBBLE CONSTANT

DISCREPANCY BETWEEN MEASUREMENTS

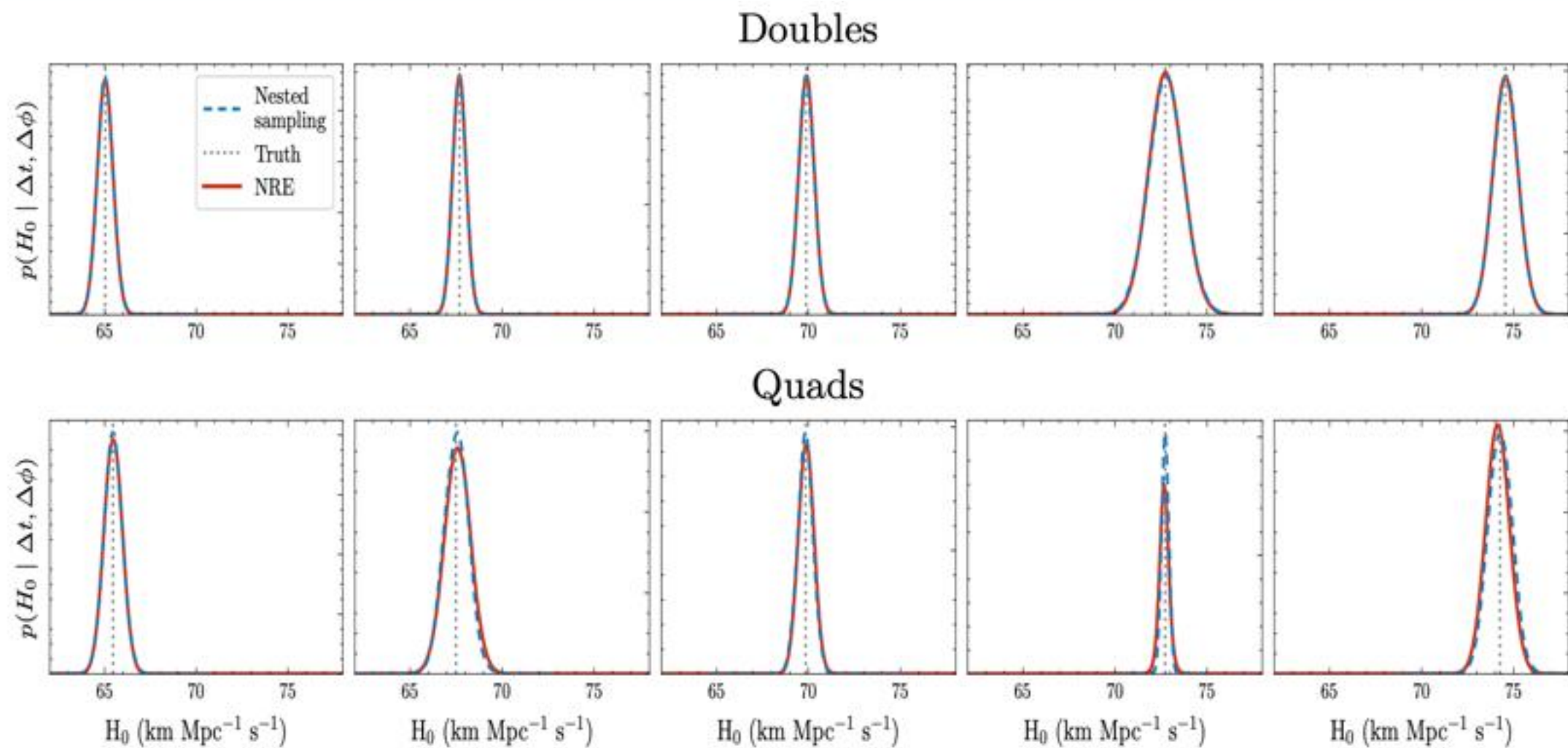


Adam G. Riess *et al* 2019
ApJ **876** 85

H0 INFERENCE WITH NEURAL RATIO ESTIMATORS



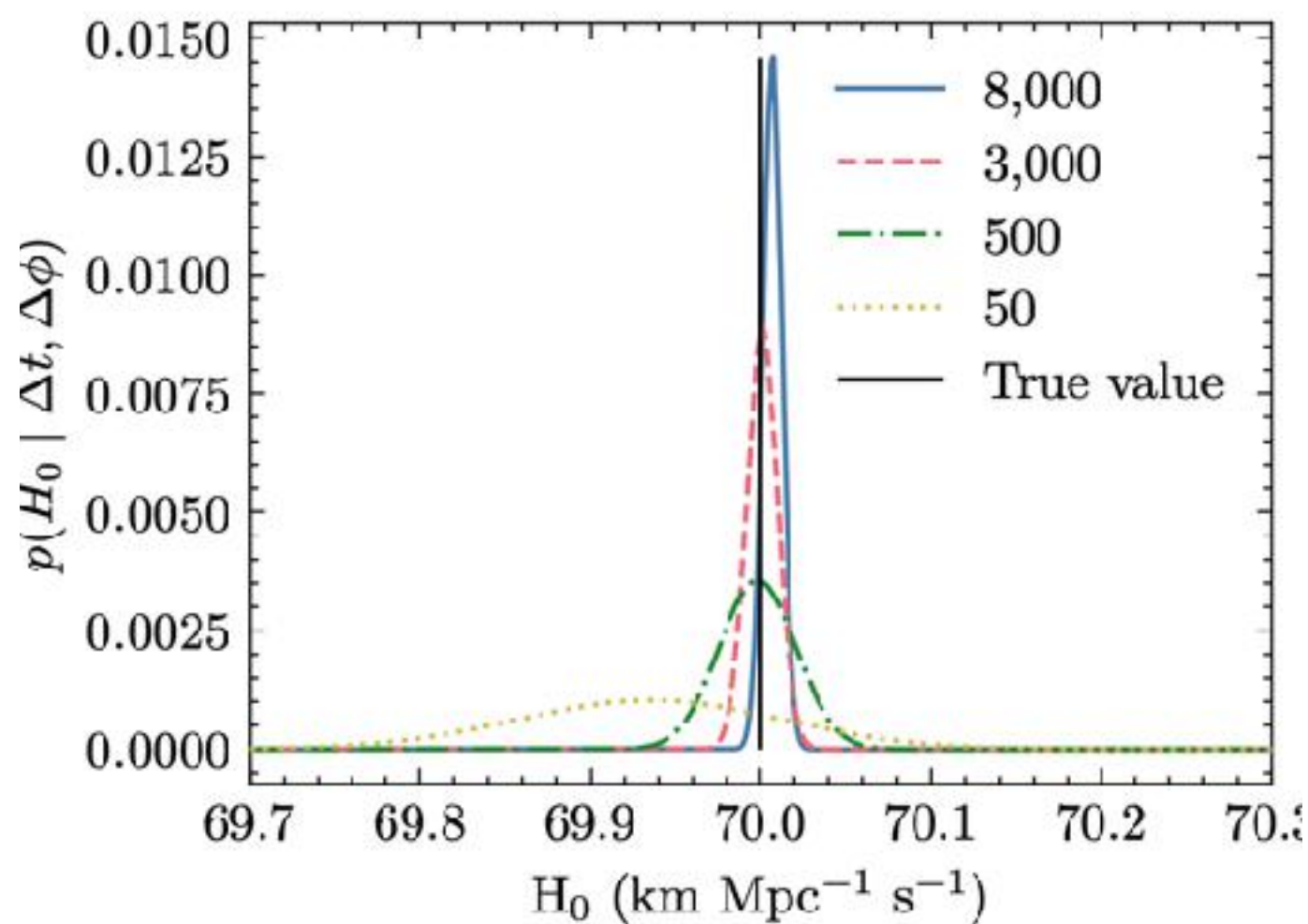
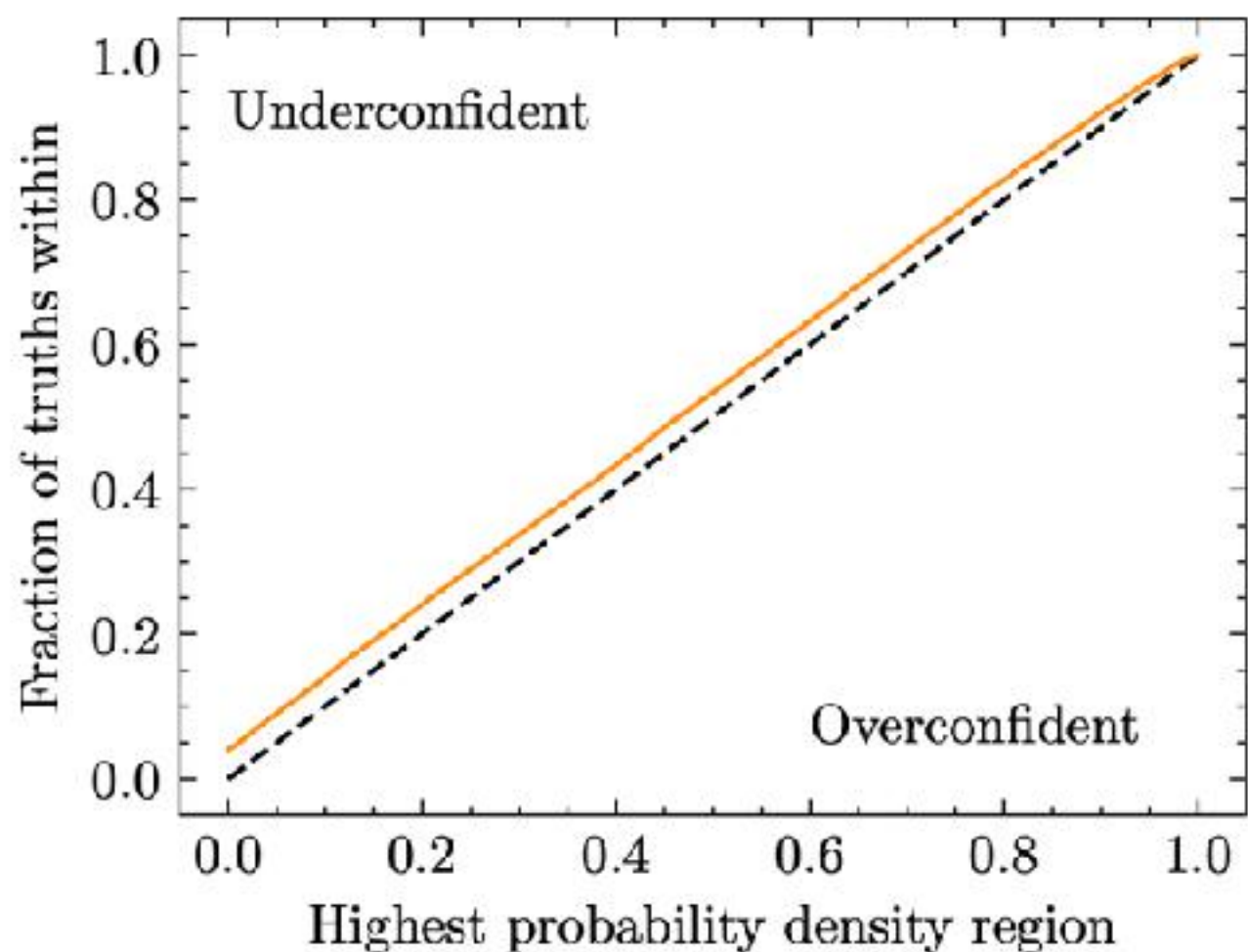
Ève Campeau-Poirier



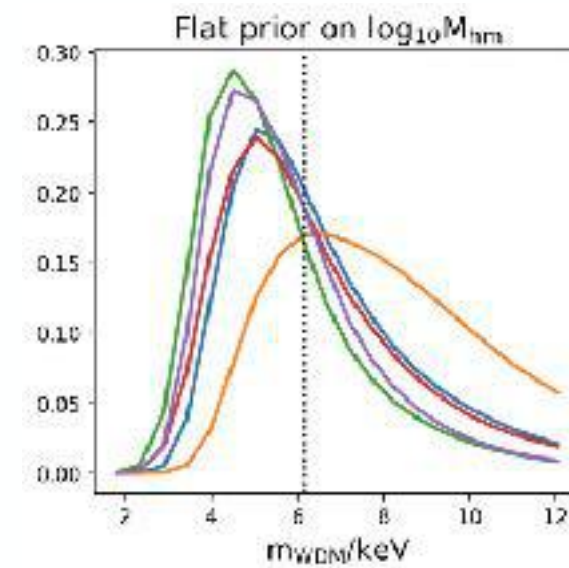
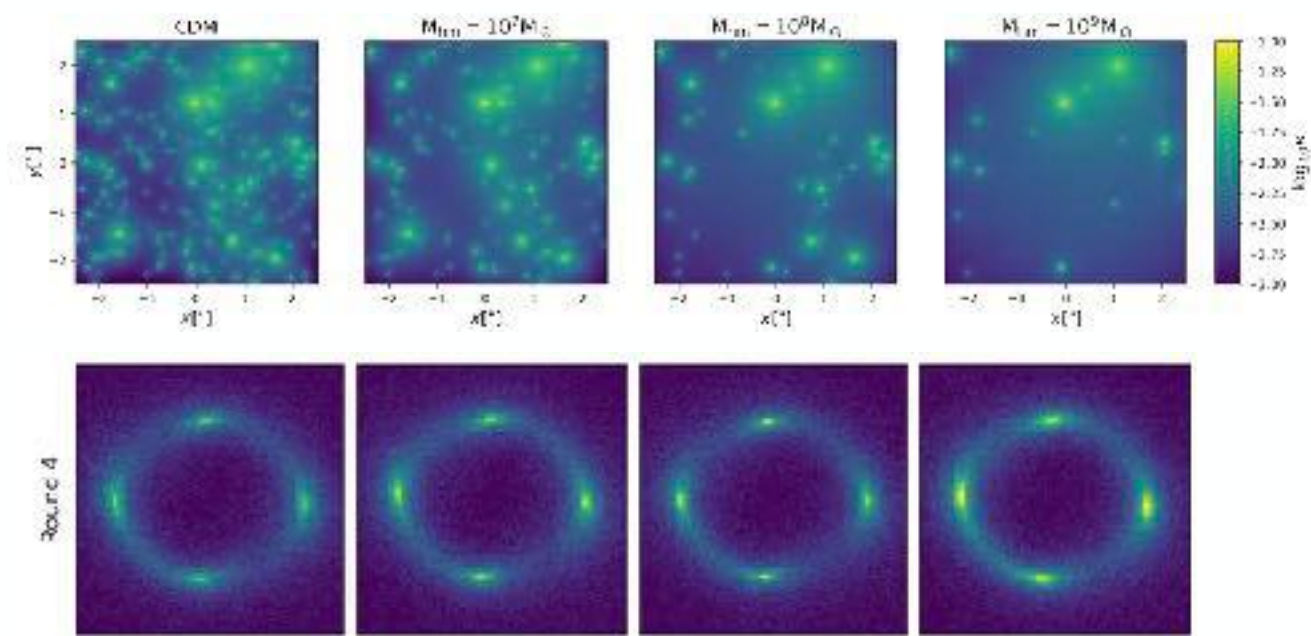
H0 INFERENCE WITH NEURAL RATIO ESTIMATORS



Ève Campeau-Poirier



Estimating the dark matter particle temperature with Neural Ratio Estimators



Adam
Coogan

Anau Montel, Coogan et al. 2022

Coogan et al. , NeurIPS 2020 ML4PS Workshop

RATIO ESTIMATION METHODS

Pros:

- ▶ Can marginalize implicitly over large number of nuisance parameters

Caveats:

- ▶ Because we have marginalized, we've lost the capability to generate samples consistent with the observations.
- ▶ So far: no real way of quantifying the uncertainty of the ratio estimator itself. All the guarantees are in terms of convergence to a specific ratio in the limit of perfect training. Is this always realistic?

TACKLING AN UNSOLVED PROBLEM: HIGH DIMENSIONAL INFERENCE

A previously unsolved problem in all of astrophysics (and other sciences):

How do we infer the posteriors of high-dimensional parameters (e.g., an image or spectra)?

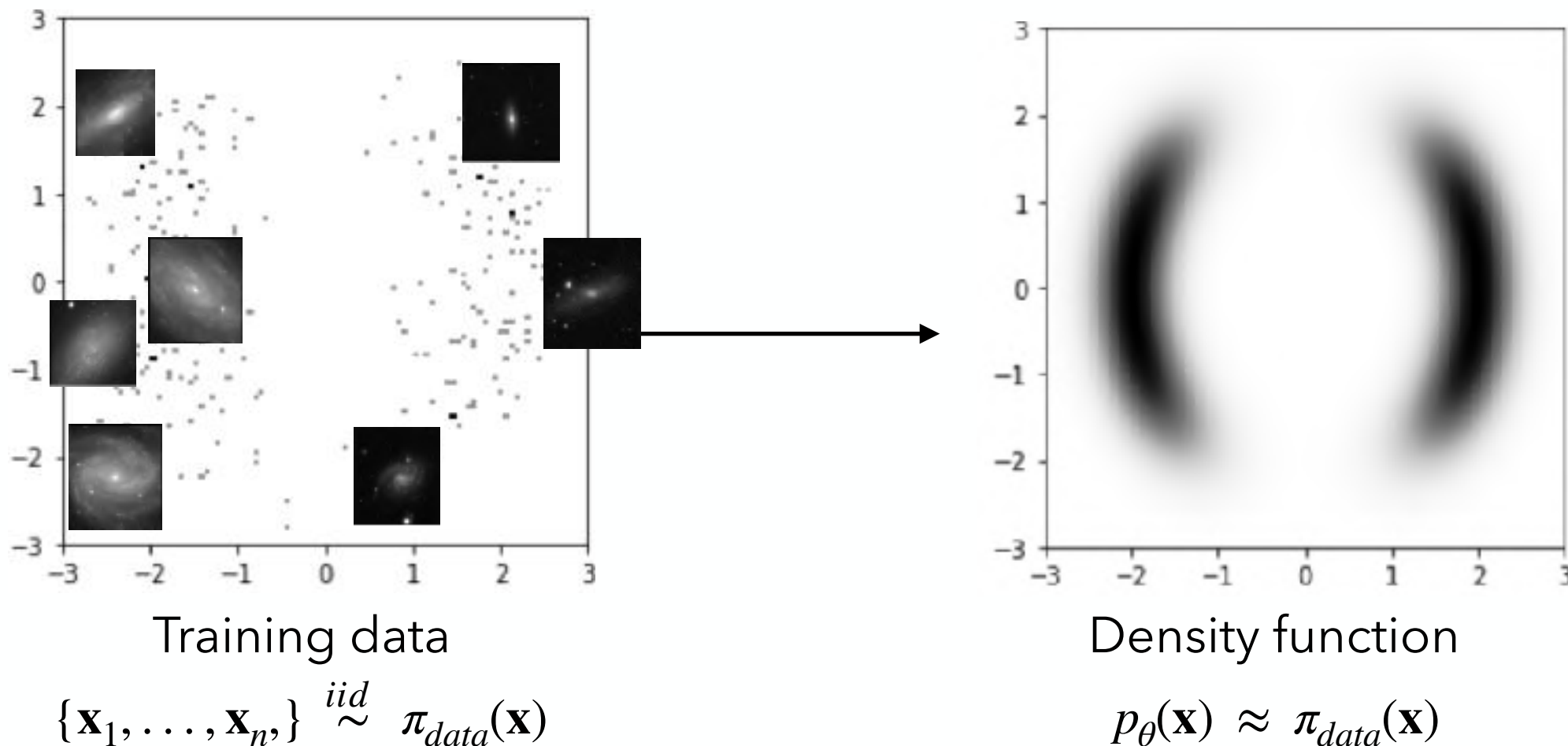
Obstacles:

- 1) How do we encode complex priors
- 2) How we sample such high-dimensional posteriors (even if we could compute them)

LEARNING THE PRIOR EXPLICITLY

Can we learn our high-dimensional prior explicitly from data?
i.e. can we learn a generative model that will produce samples from that distribution?

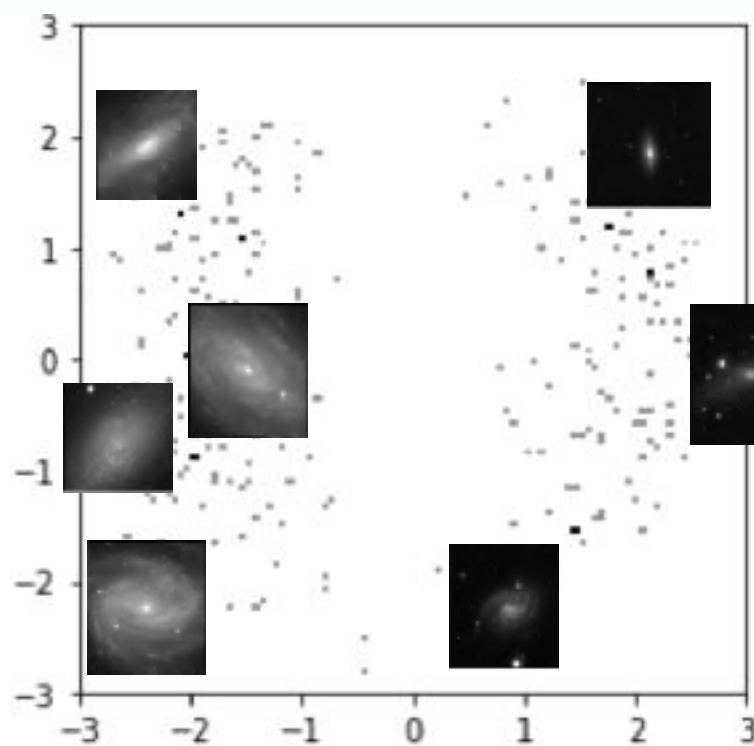
How can we do this from samples (e.g. data)? Modeling the density?



SCORE MODELING

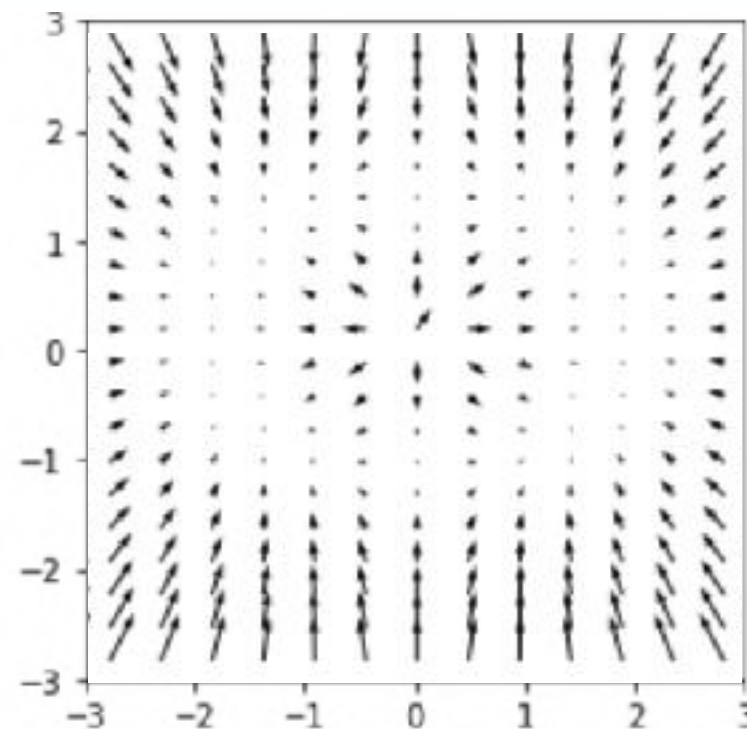
Turns out that if I want to sample a distribution, the only thing I need to learn is its **score**, which does not include the normalization constant and only uses local information

$$\mathbf{s}(\mathbf{x}) = \nabla_{\mathbf{x}} \log(\pi(\mathbf{x}))$$



Training data

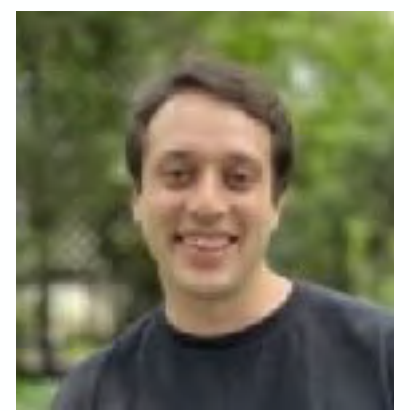
$$\{\mathbf{x}_1, \dots, \mathbf{x}_n\} \stackrel{iid}{\sim} \pi_{data}(\mathbf{x})$$



Score function

$$\mathbf{s}_{\theta}(\mathbf{x}) \approx \nabla \log(\pi(\mathbf{x}))$$

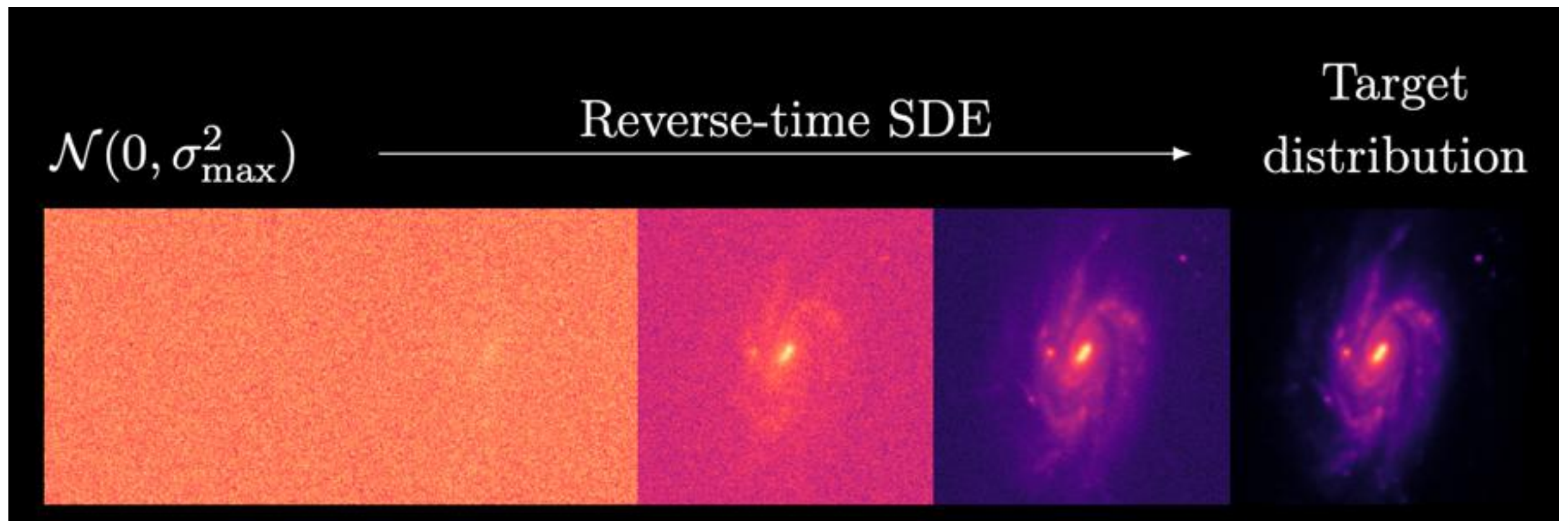
SCORE-BASED MODELING

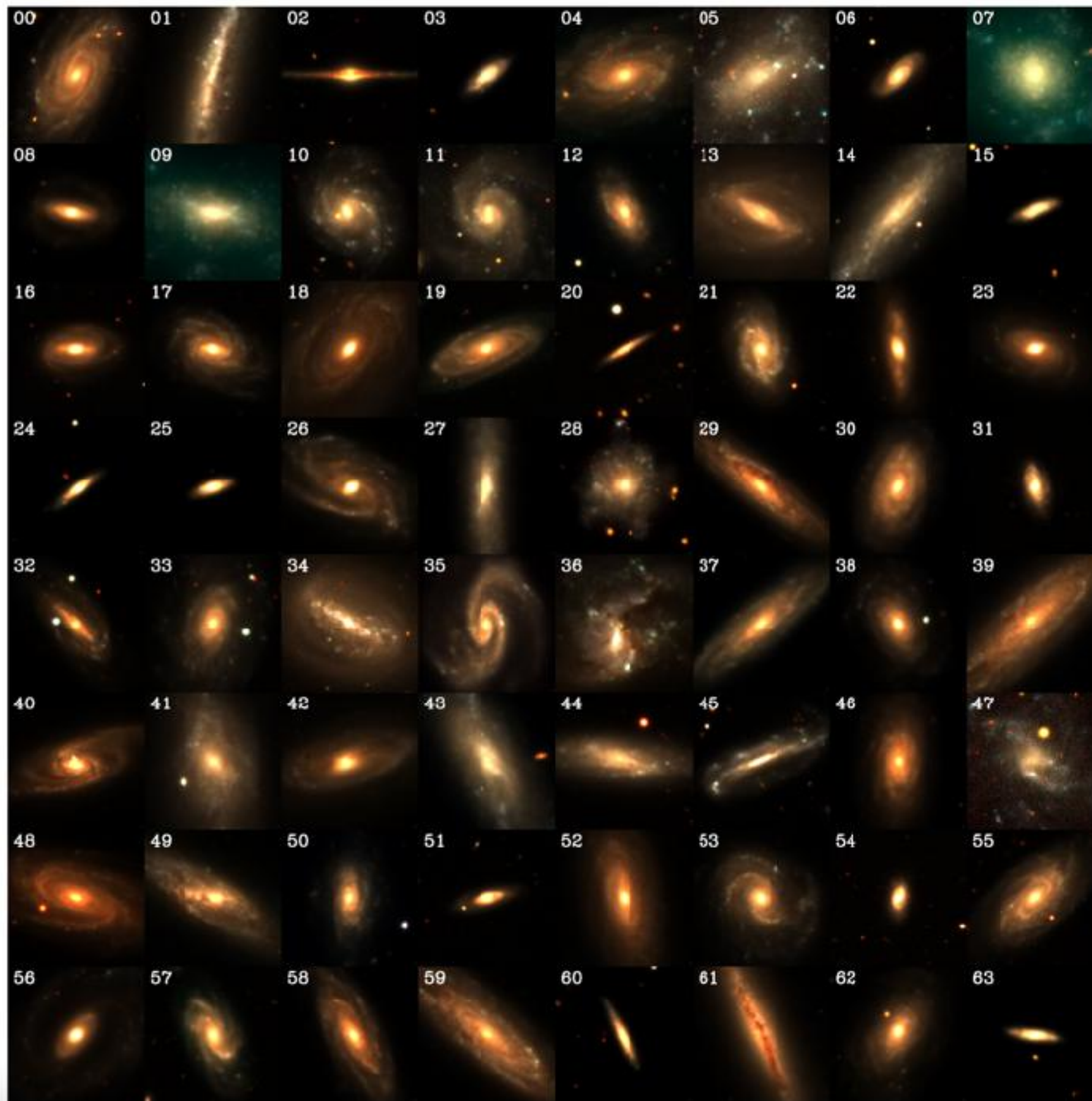


Alexandre Adam

We model the score of the prior

$$s_{\theta}(x) \equiv \nabla_x \log p_{\theta}(x)$$





Connor
Stone

<http://www.mjjsmith.com/thisisnotagalaxy/>

SCORE-BASED MODELING



Alexandre Adam

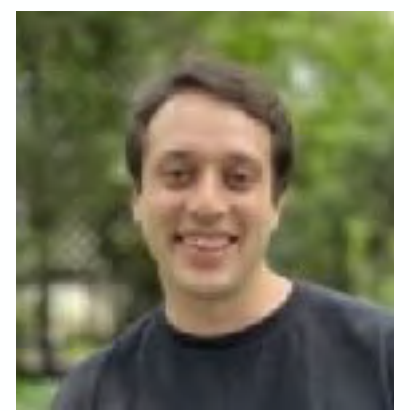
To sample from the posterior, the score of the likelihood is all that we need:

$$\nabla_x \log p(x|y) = \nabla_x \log p(y|x) + \nabla_x \log p_\theta(x)$$

We can calculate the likelihood score analytically if we assume it's Gaussian.

This is the prior score we learnt from the training data

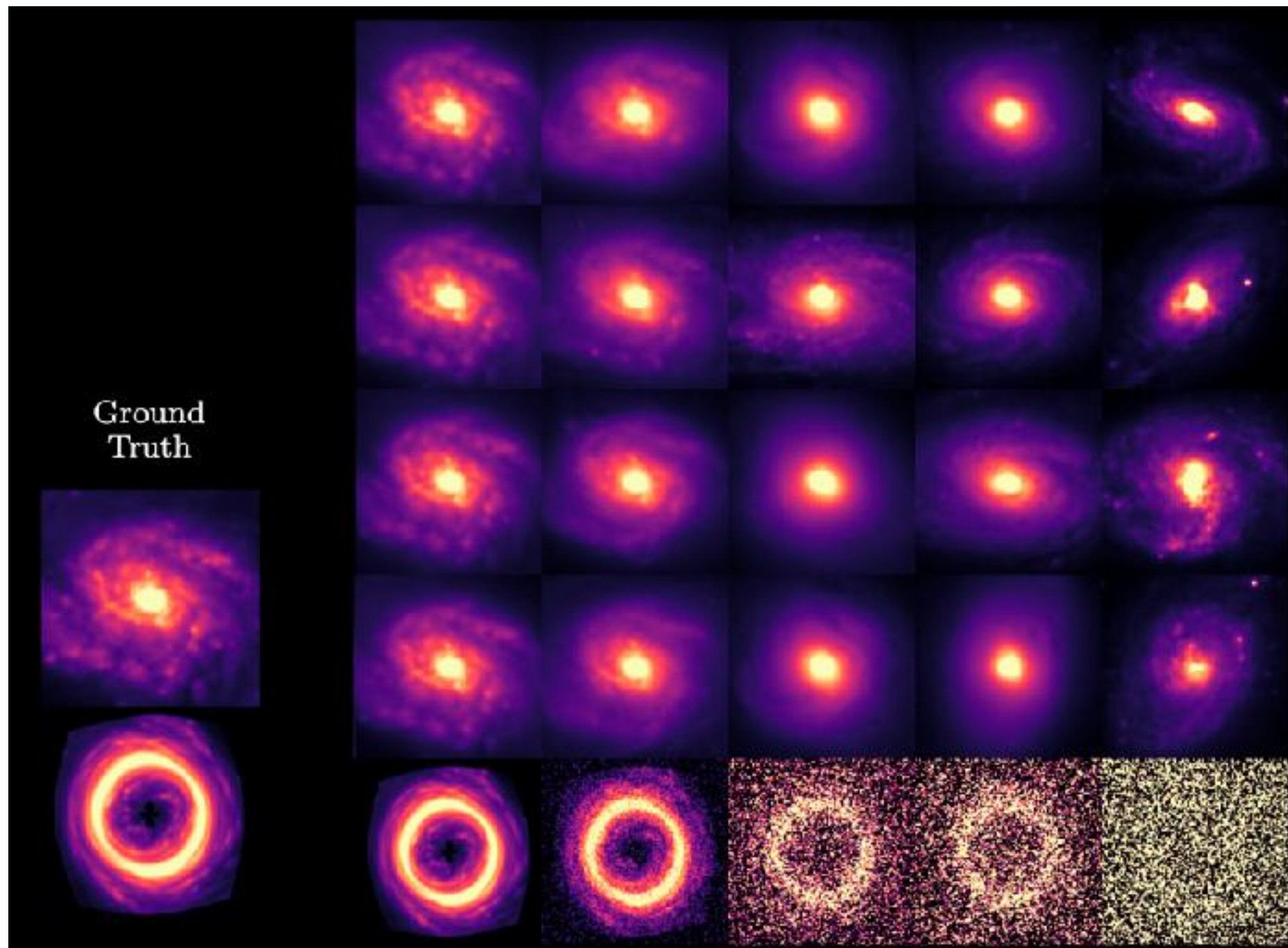
SCORE-BASED MODELING



Alexandre Adam

To sample from the posterior, the score of the likelihood is all that we need:

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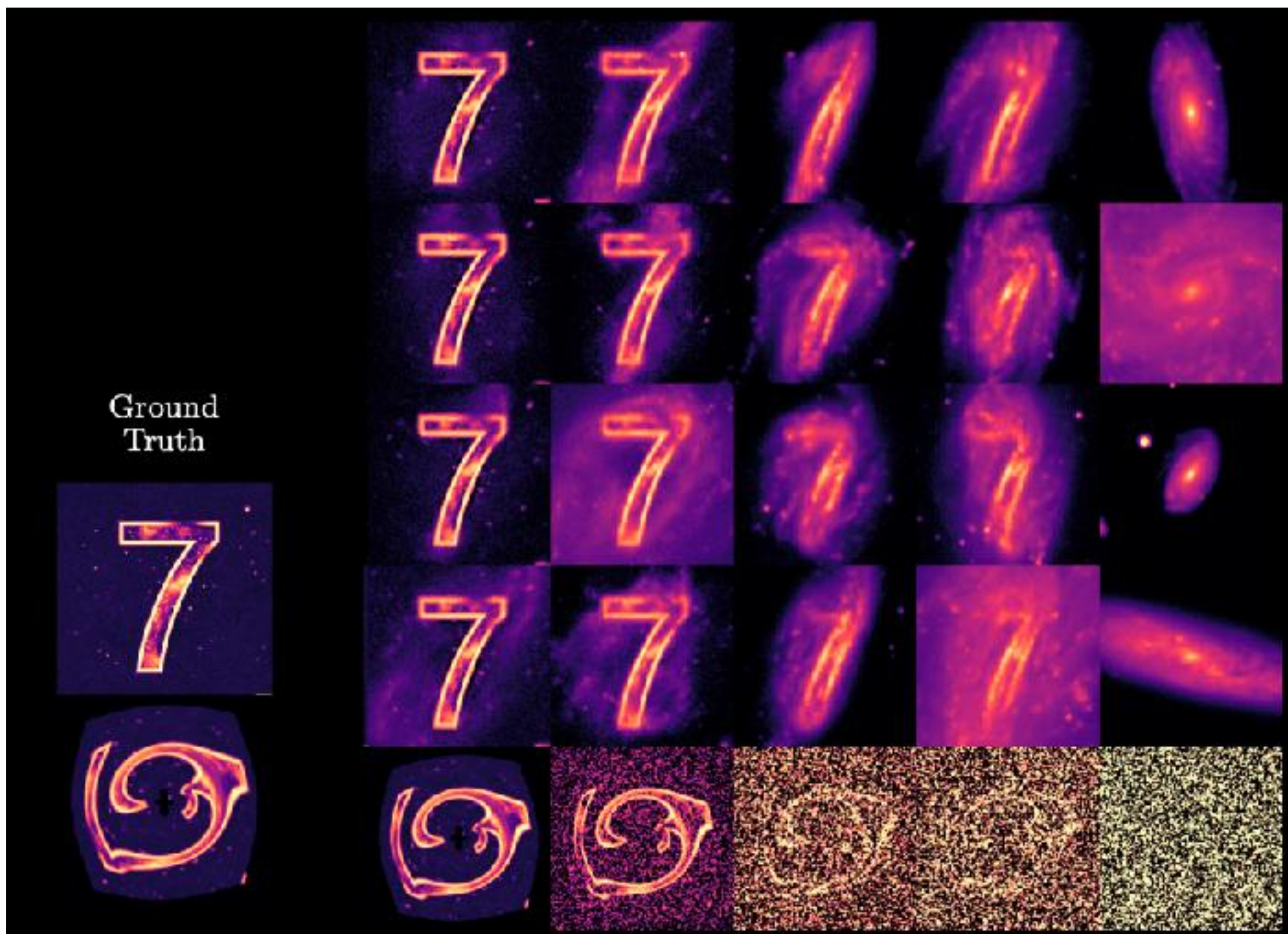
OUT OF DISTRIBUTION TESTS



Alexandre Adam

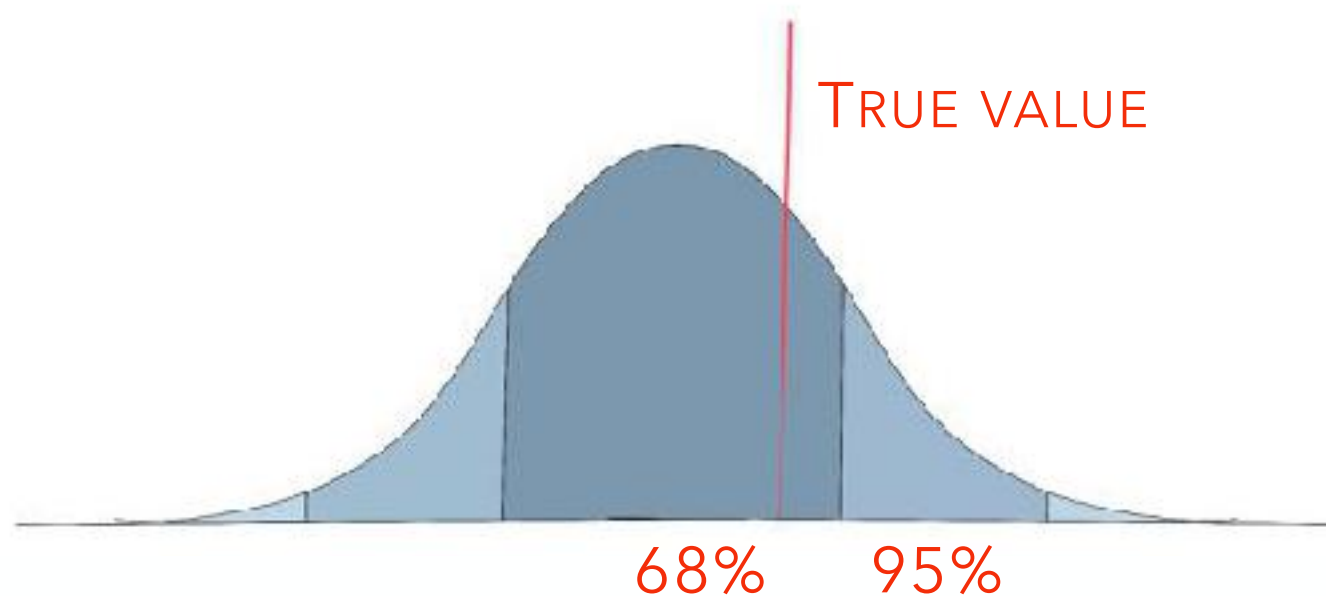
To sample from the posterior, the score of the likelihood is all that we need:

$$\nabla_x \log p(x|y) = \nabla_x \log p(y|x) + \nabla_x \log p_\theta(x)$$



ARE THESE UNCERTAINTIES ACCURATE?

COVERAGE PROBABILITY OF A CONFIDENCE INTERVAL IS THE PROPORTION OF THE TIME THAT THE INTERVAL CONTAINS THE TRUE VALUE OF INTEREST.

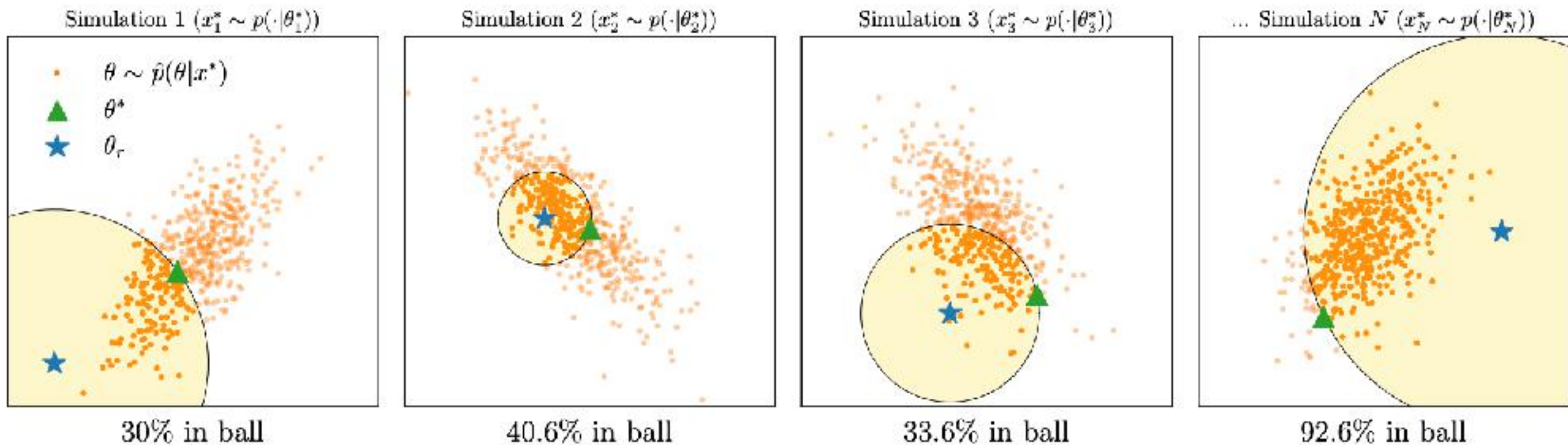


FOR AN ACCURATE INTERVAL ESTIMATOR, THE COVERAGE PROBABILITY IS EQUAL TO ITS CONFIDENCE LEVEL

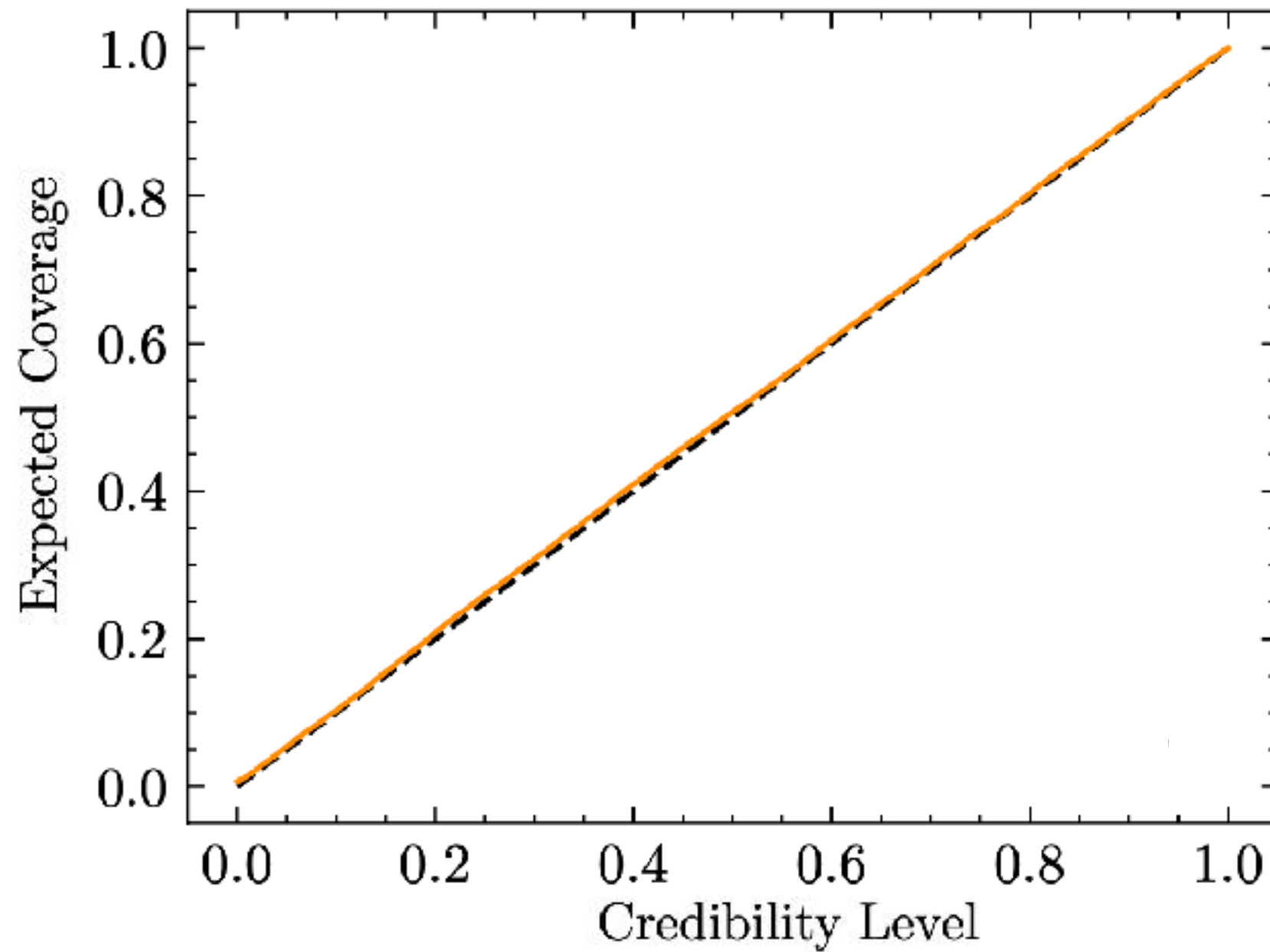
COVERAGE TEST FOR ACCURACY



Pablo Lemos



COVERAGE TEST FOR ACCURACY



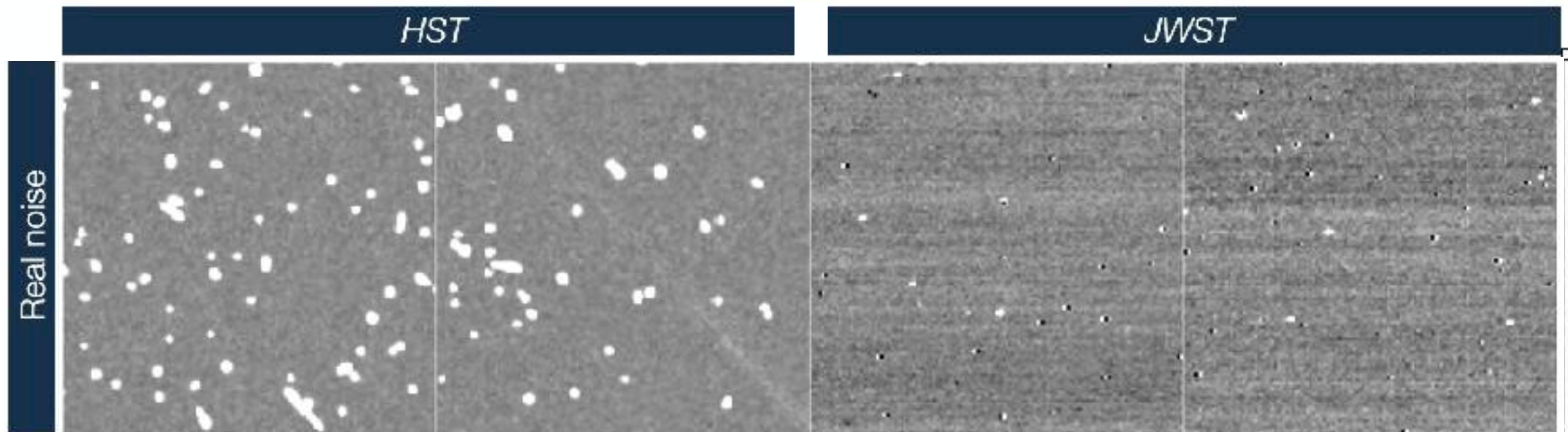
DEALING WITH REALISTIC NOISE: BEYOND GAUSSIANITY



Alexandre Adam



Ronan Legin

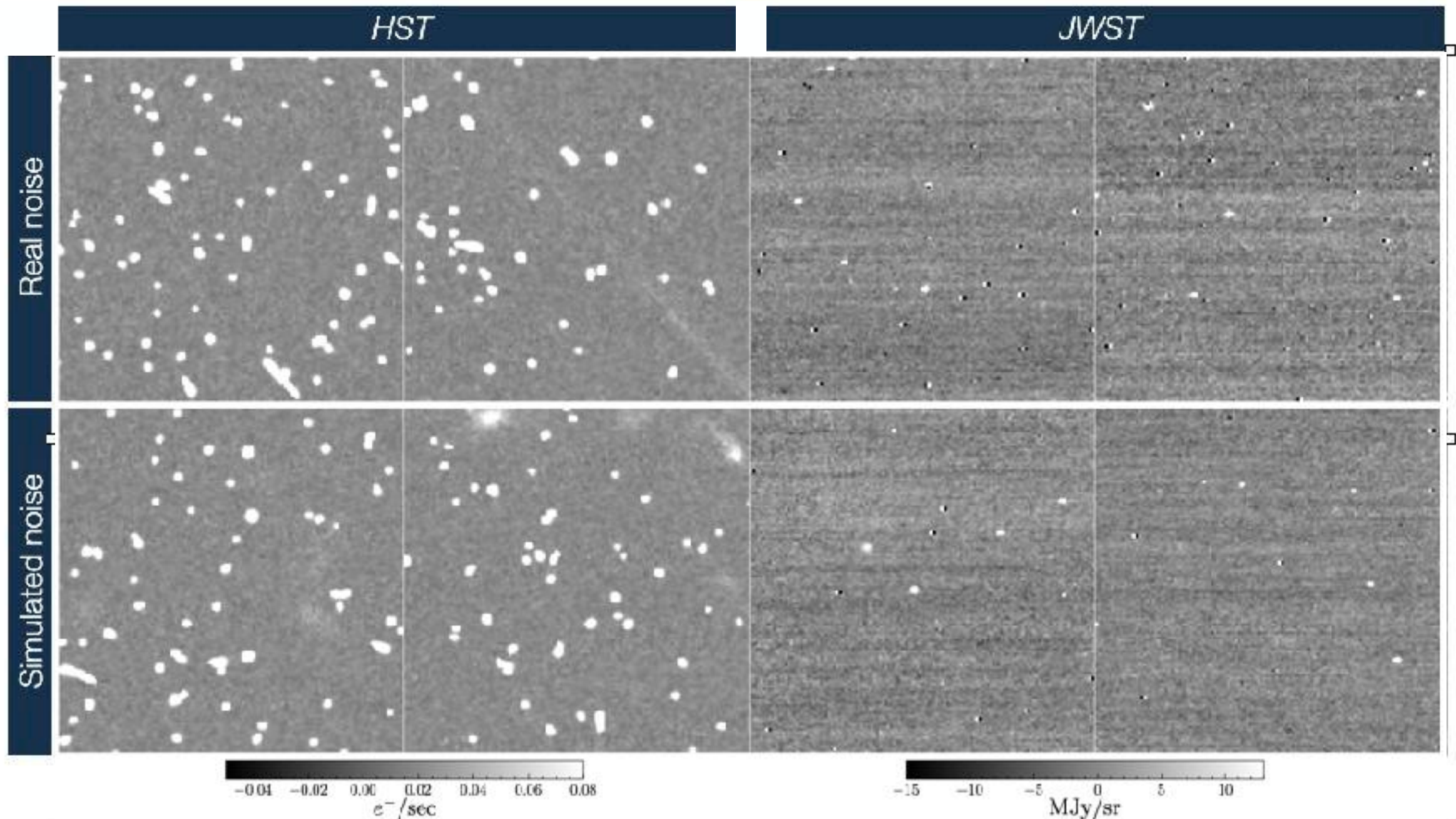


DEALING WITH REALISTIC NOISE: BEYOND GAUSSIANITY

SLIC: SCORE-BASED LIKELIHOOD CHARACTERIZATION

Since we have learnt a generative model of the additive noise, it can now be used in a simulation pipeline to get new, independent realizations of noise:

$$P(\mathbf{x}_O|\eta) = Q(\mathbf{x}_O - \mathbf{M}(\eta))$$



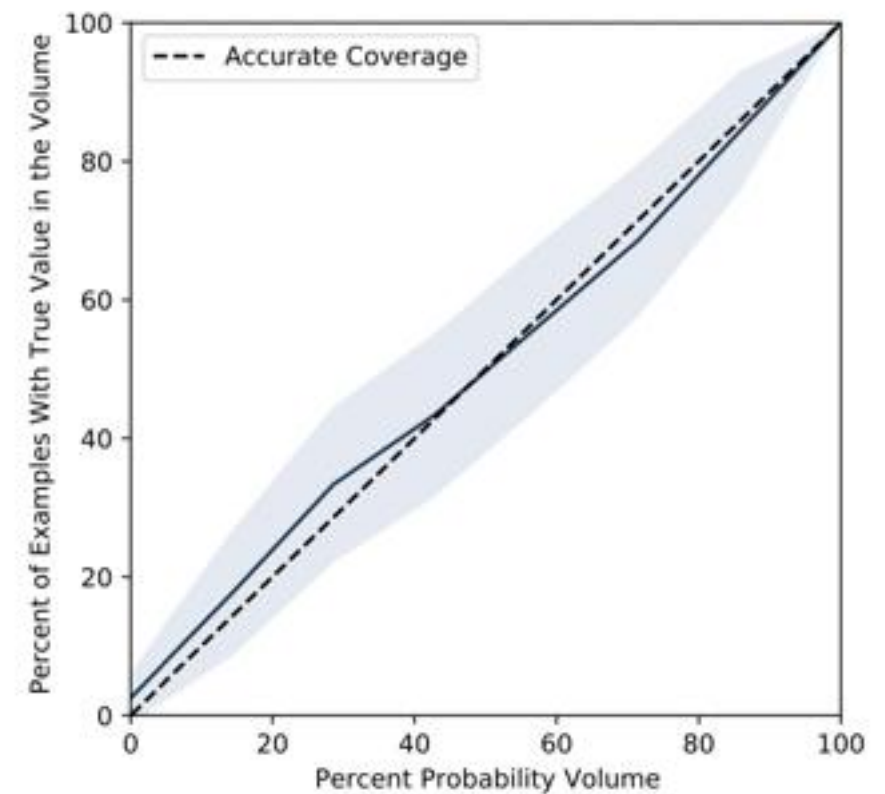
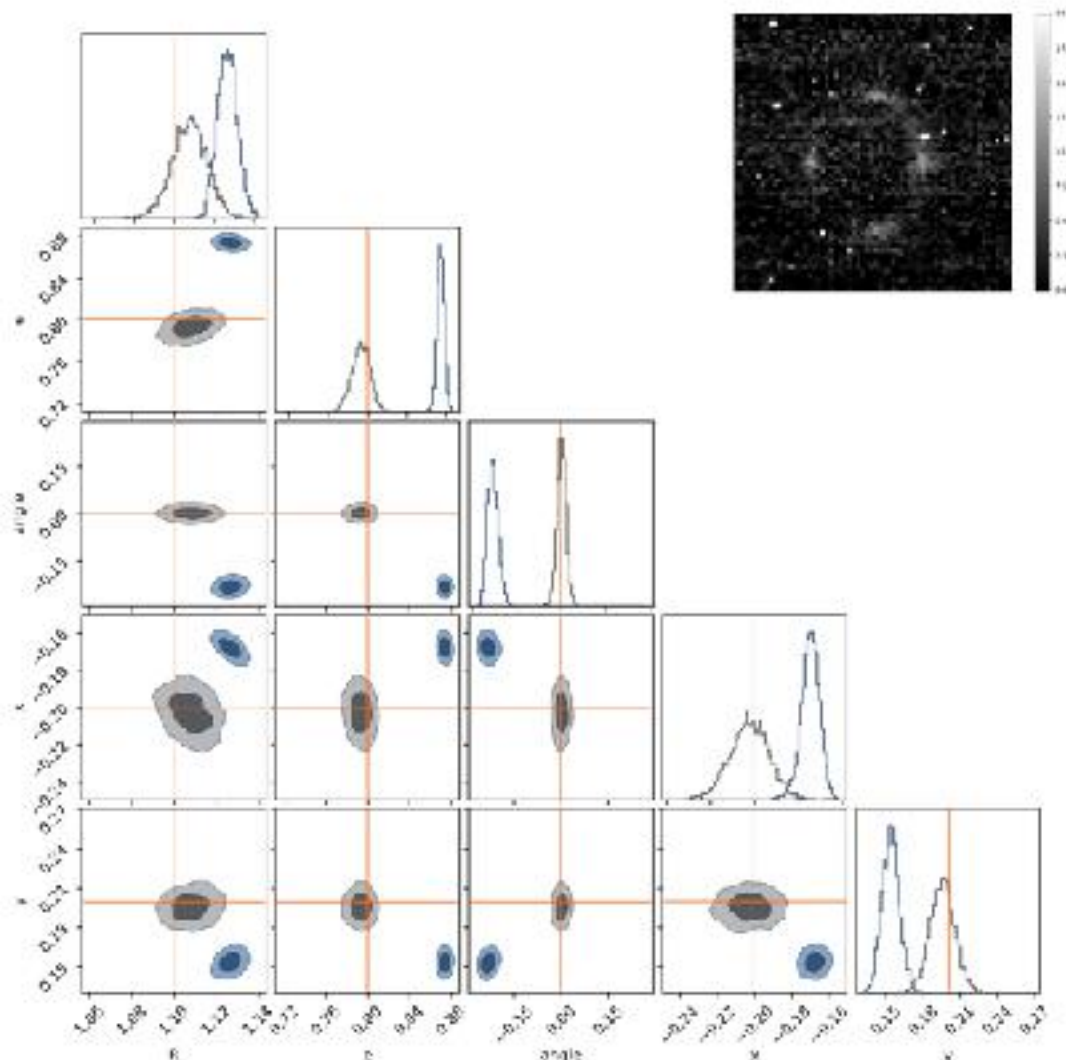
DEALING WITH REALISTIC NOISE: BEYOND GAUSSIANITY

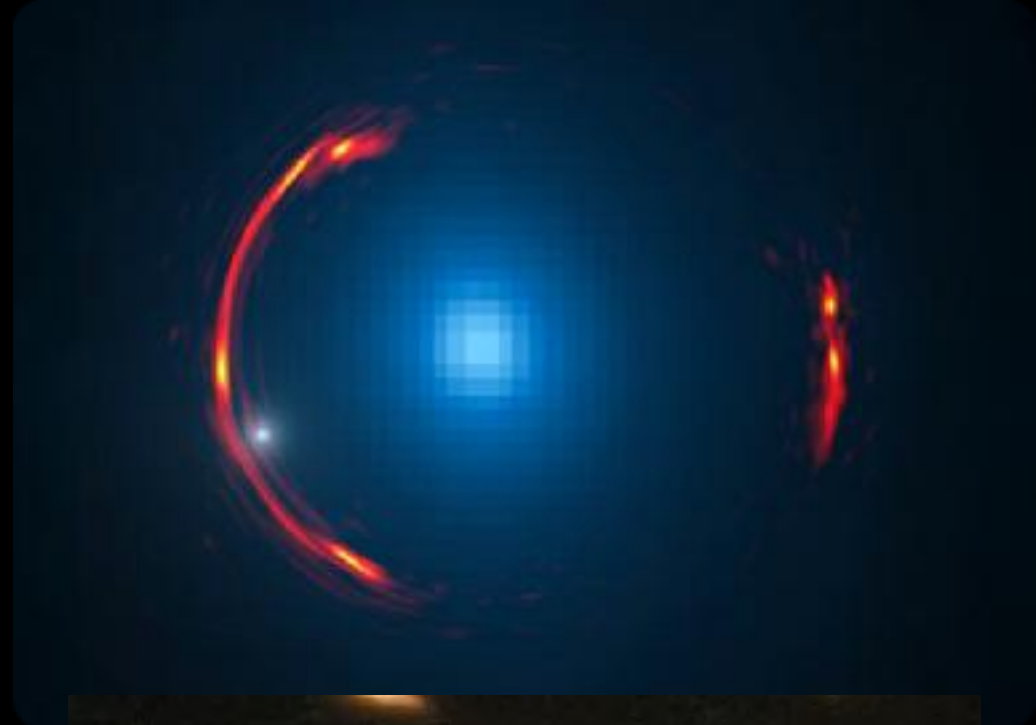
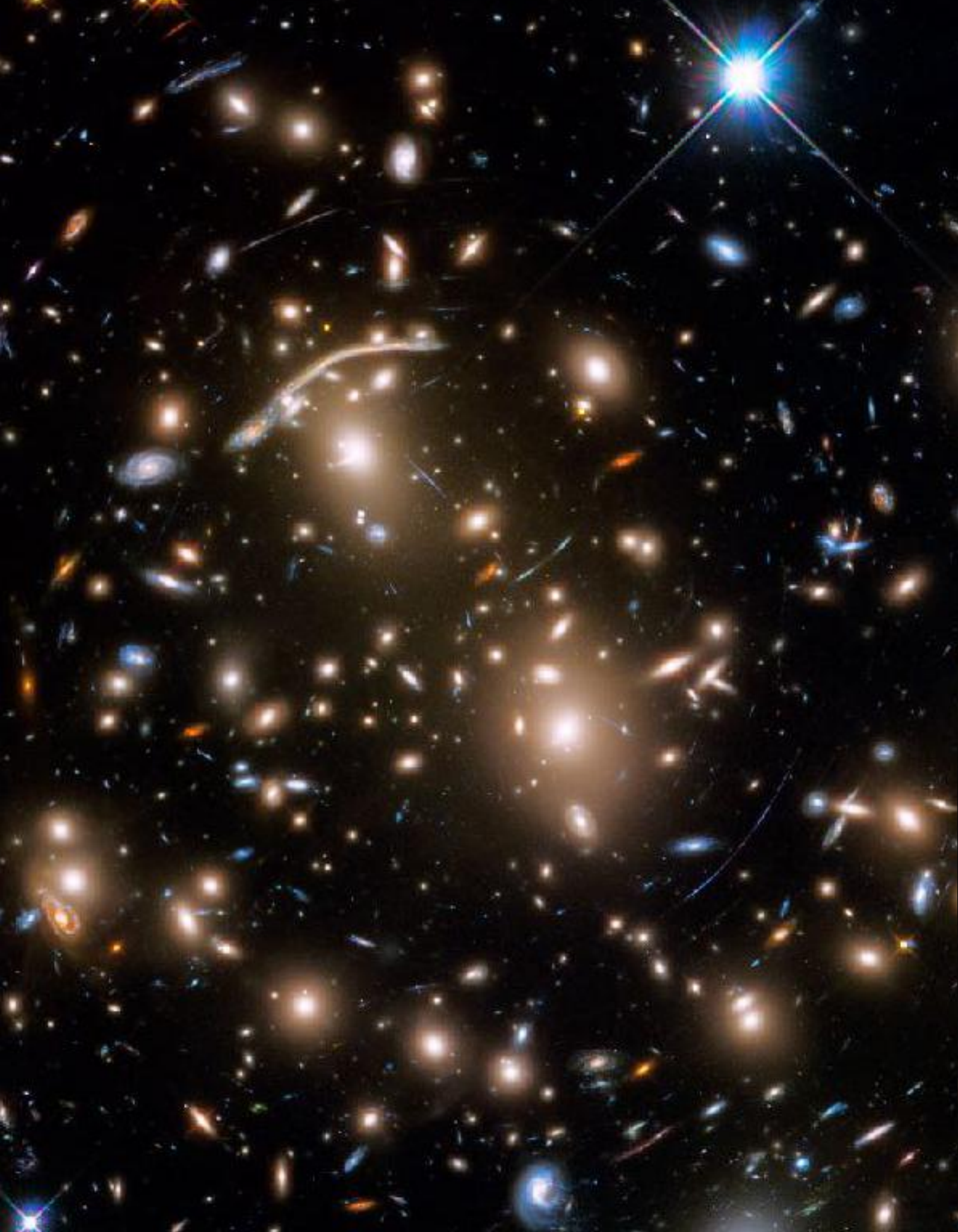
SLIC: SCORE-BASED LIKELIHOOD CHARACTERIZATION

$$\mathbf{s}(\mathbf{x}_0) = \partial \log Q(\mathbf{x}_0) / \partial \mathbf{x}$$

$$P(\mathbf{x}_0 | \eta) = Q(\mathbf{x}_0 - \mathbf{M}(\eta))$$

$$\eta_{i+1} = \eta_i + \tau \nabla_{\mathbf{x}} \log Q(\mathbf{x}_0 - \mathbf{M}(\eta)) \nabla_{\eta} \mathbf{M}(\eta_i) + \sqrt{2\tau} \xi$$







Explore Algorithmically

Montreal Institute for Astrophysics and Machine Learning

Cielà is a research institute associated with the Université de Montréal, with the mission to contribute to breakthrough discoveries in astrophysics by developing new computational data analysis methods. It supports a unique interdisciplinary community of world-leading researchers in astrophysics and machine learning. Read about our [research](#).



Ciela Institute

The institute's mission is to contribute to breakthrough discoveries in astrophysics and cosmology by developing innovative data analysis and machine learning methods. It also aims to use unsolved and challenging data analysis problems in astrophysics to push the boundaries of machine learning and to make significant advances that can contribute to the successful and widespread use of machine learning in other fields of science.



Laurence Perreault-Levasseur
Faculty Member

Laurence Perreault-Levasseur is an assistant professor at the University of Montreal and an Associate Member of Mila.



Pierre-Luc Bacon
Faculty Member

P'm an assistant professor at University of Montreal's DIRO, a member of Mila and the Institute for Data Valorisation (IVADO).



Yashar Hezaveh
Faculty Member

Yashar Hezaveh is the Director of Ciela Institute and an Assistant Professor in the Department of Physics.



Yoshua Bengio
Faculty member

Acknowledged as one of the founding figures of machine learning, Yoshua Bengio was the recipient of the Turing Award for his groundbreaking contributions to deep learning.



Julie Hlavacek-Larrondo
Faculty Member

Dr. Julie Hlavacek-Larrondo is a world leading expert in the astrophysics of black holes.



Adrian Liu
Faculty Member

Adrian Liu is an Assistant Professor in the Department of Physics and the Trotter Space Institute at McGill University.



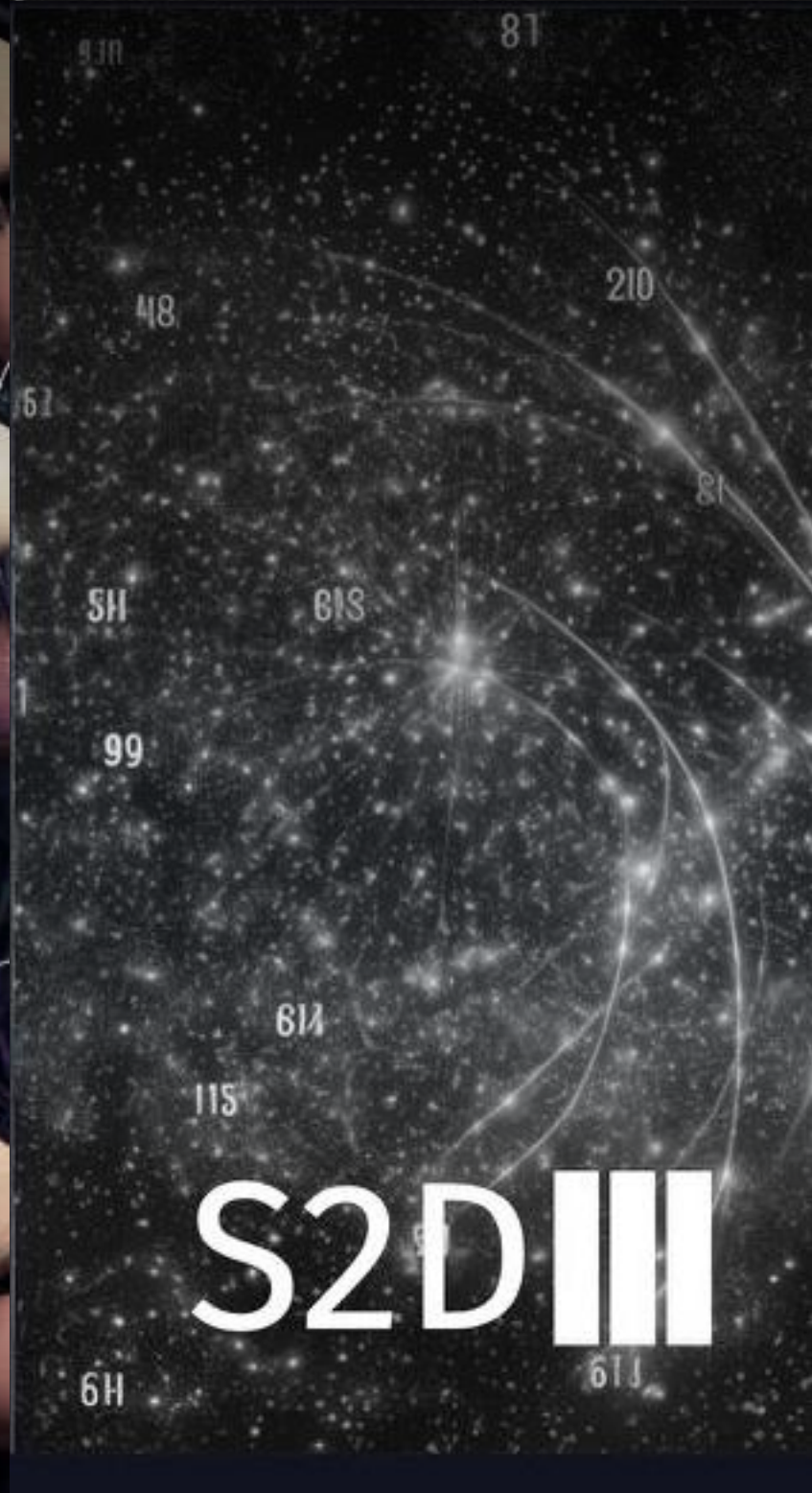
Stephanie Luna
Manager

Stephanie Luna has more than 5 years of experience in research administration.



Siamak Ravanbakhsh
Faculty Member

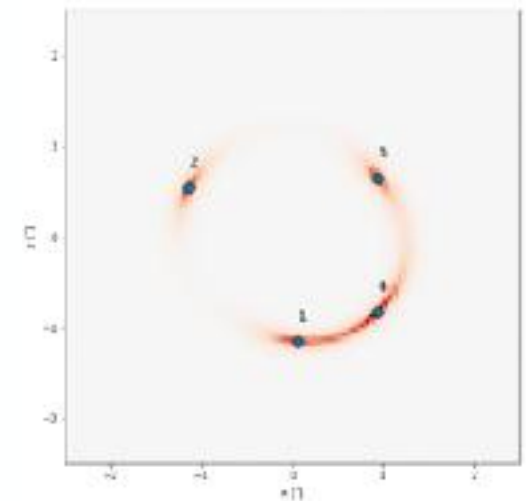
Siamak Ravanbakhsh is an assistant professor at McGill University's School of Computer Science and an expert in inference in combinatorial domains.



STRONG LENSING SIMULATION PIPELINE: CAUSTIC

A fast, AI-empowered, differentiable, extremely modular simulation pipeline for all your strong lensing needs.

- 1) Lens and source from analytic profiles or pixelated images/densities
- 2) Multiplane lensing
- 3) Line of sight mass distributions
- 4) Fast microlensing simulations
- 5) Time-delays



Connor
Stone



Adam
Coogan



Andi
Filipp



Alex
Adam



Misha
Barth

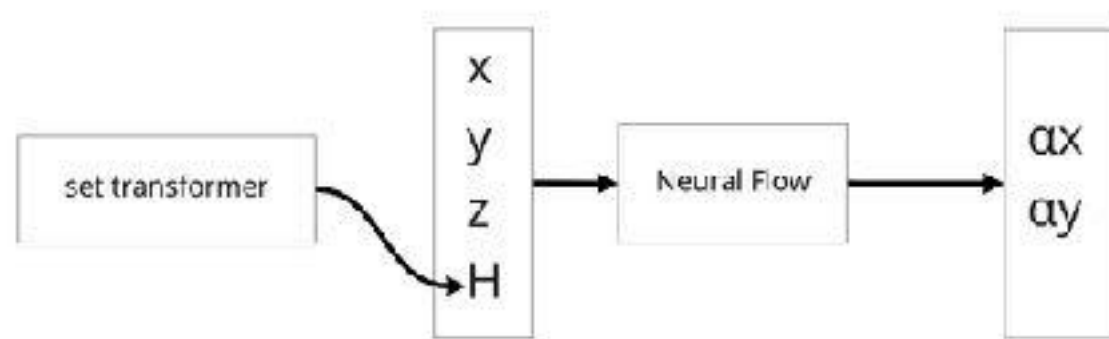
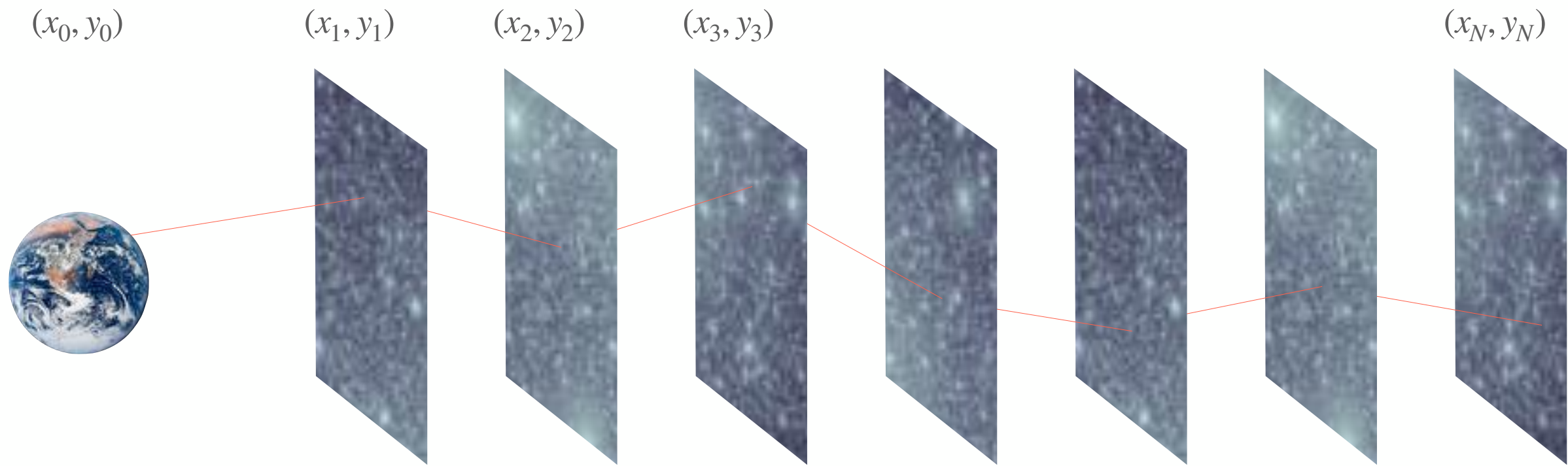


Charles
Wilson

<https://github.com/Ciela-Institute/caustic>

<https://github.com/Ciela-Institute/caustic-analyses>

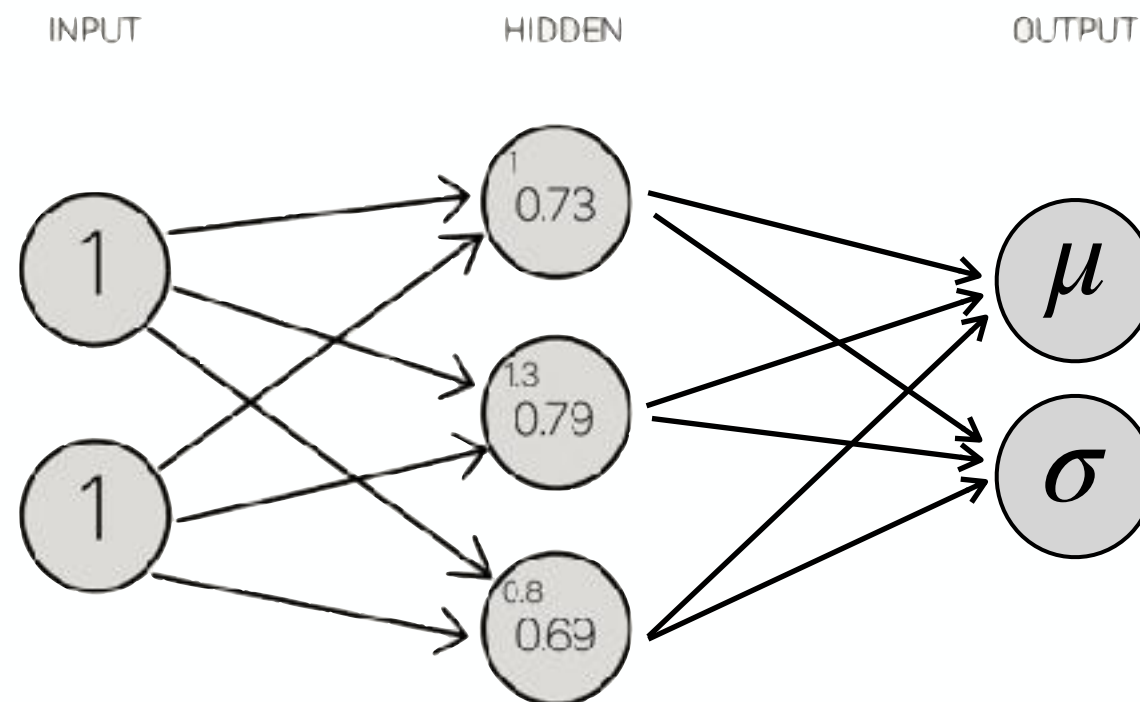
SPEEDING UP THE SIMULATIONS



Charles
Wilson

BAYESIAN NEURAL NETWORK (ALEATORIC UNCERTAINTIES)

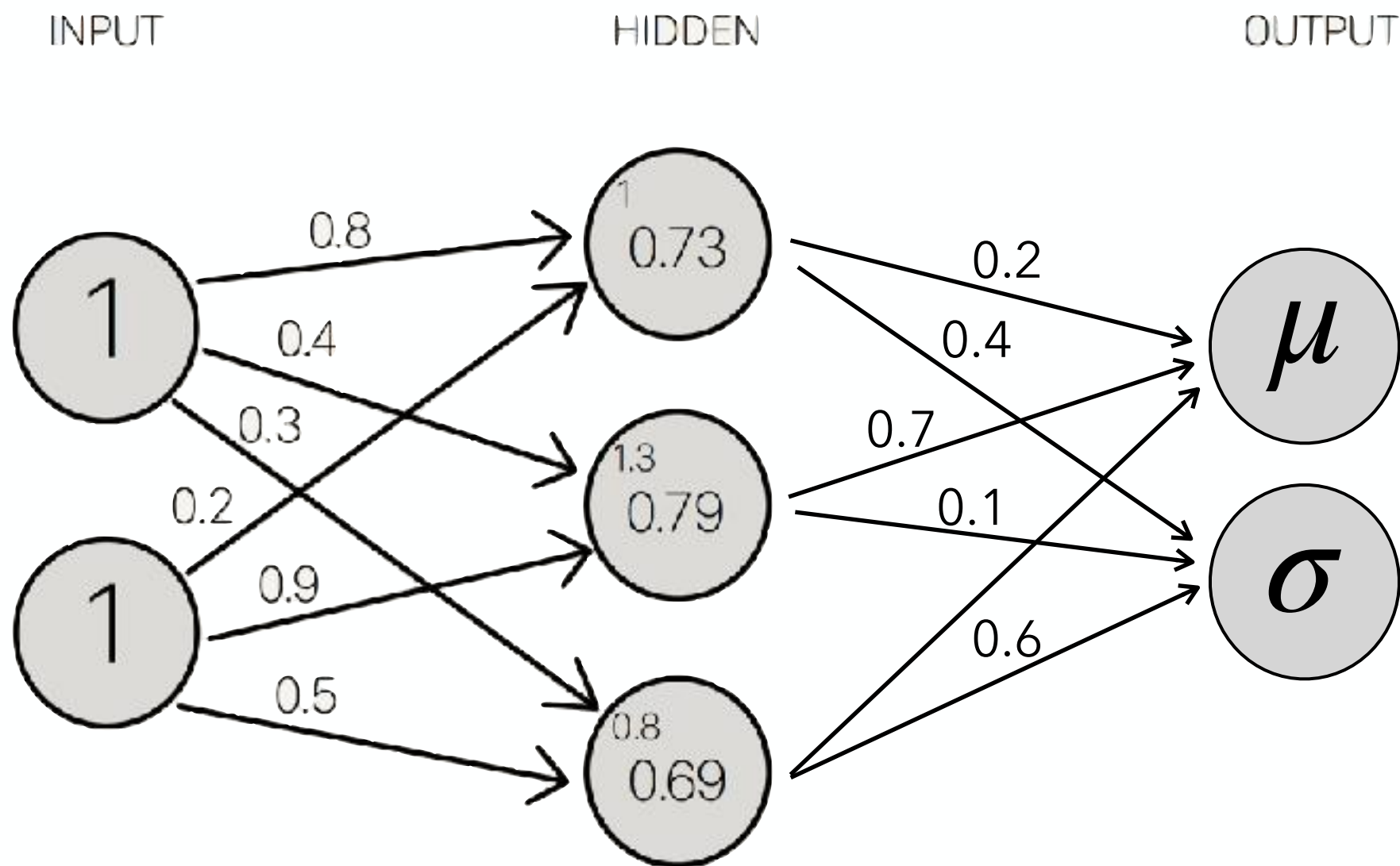
THE NEURAL NETWORK PREDICTS ITS OWN UNCERTAINTIES



$$\mathcal{L}(\mathbf{y}_n, \hat{\mathbf{y}}_n(\mathbf{x}_n, \omega)) \propto \sum_k \frac{-1}{2\sigma_k^2} \|\mathbf{y}_{n,k} - \hat{\mathbf{y}}_{n,k}(\mathbf{x}_n, \omega)\|^2 - \frac{1}{2} \log \sigma_k^2$$

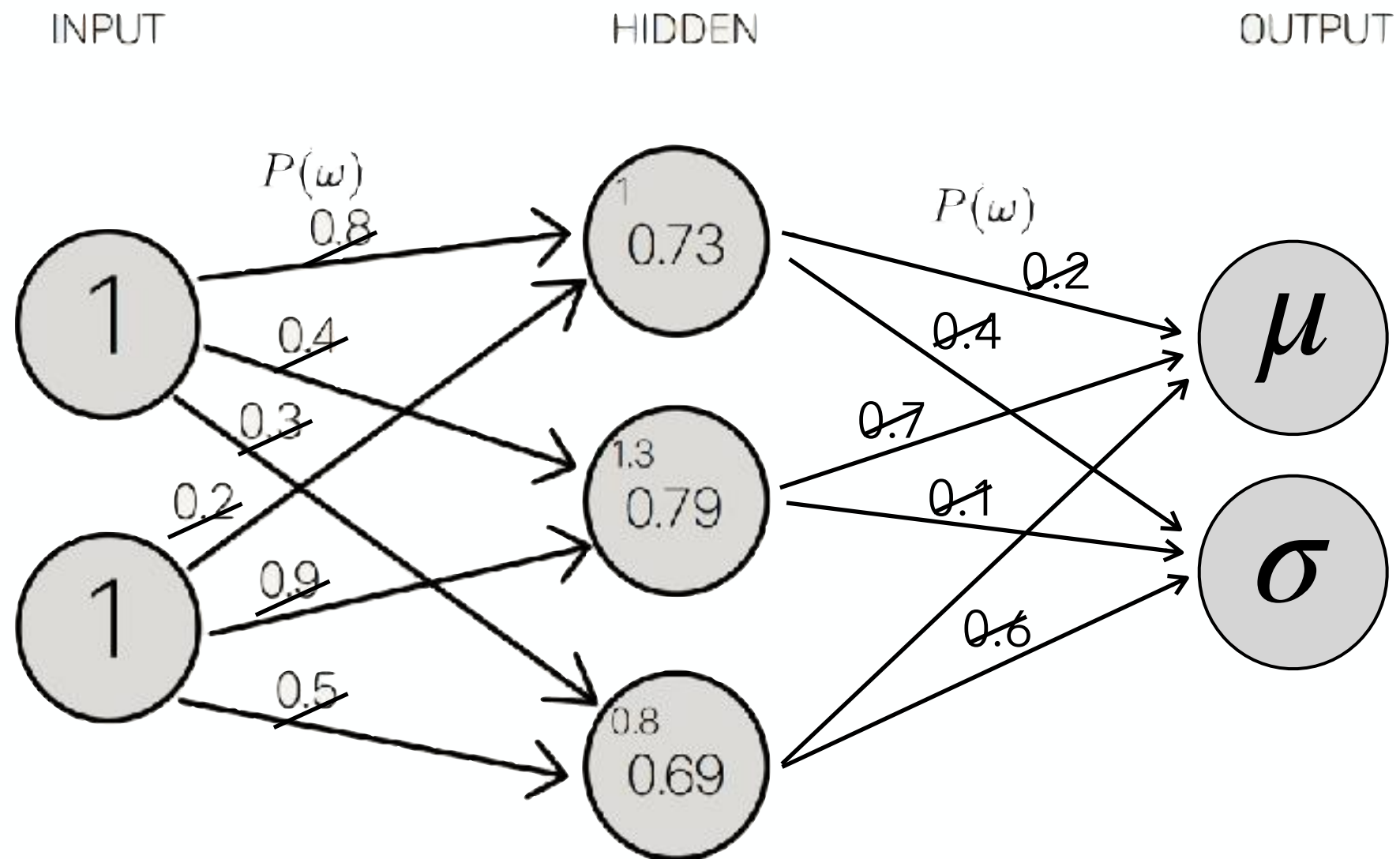
STANDARD NEURAL NETWORKS:

WEIGHT HAVE FIXED, DETERMINISTIC VALUES



BAYESIAN NEURAL NETWORKS:

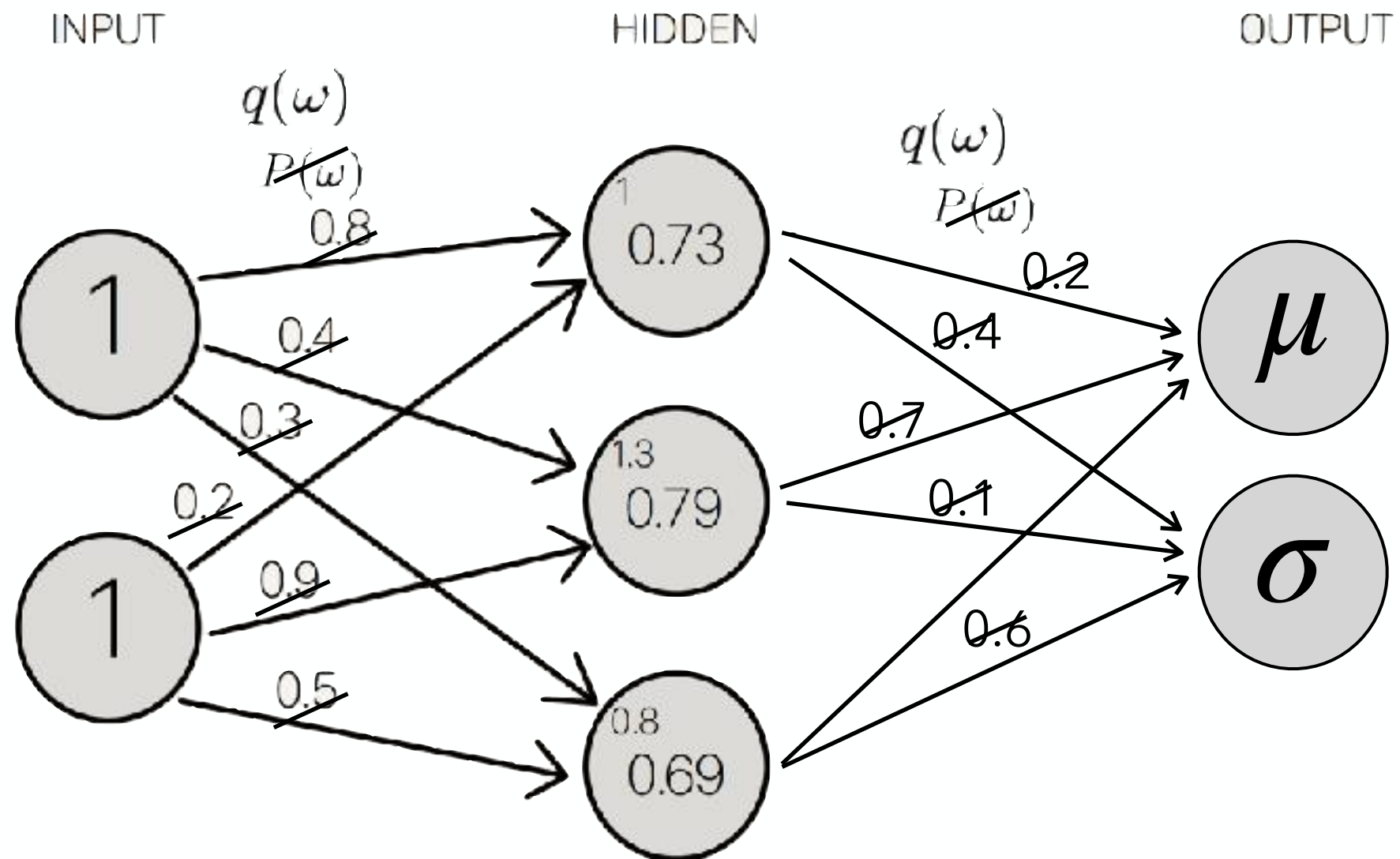
INSTEAD OF FIX VALUES, WEIGHTS ARE DEFINED BY PROBABILITY DISTRIBUTIONS



[USING VARIATIONAL INFERENCE]

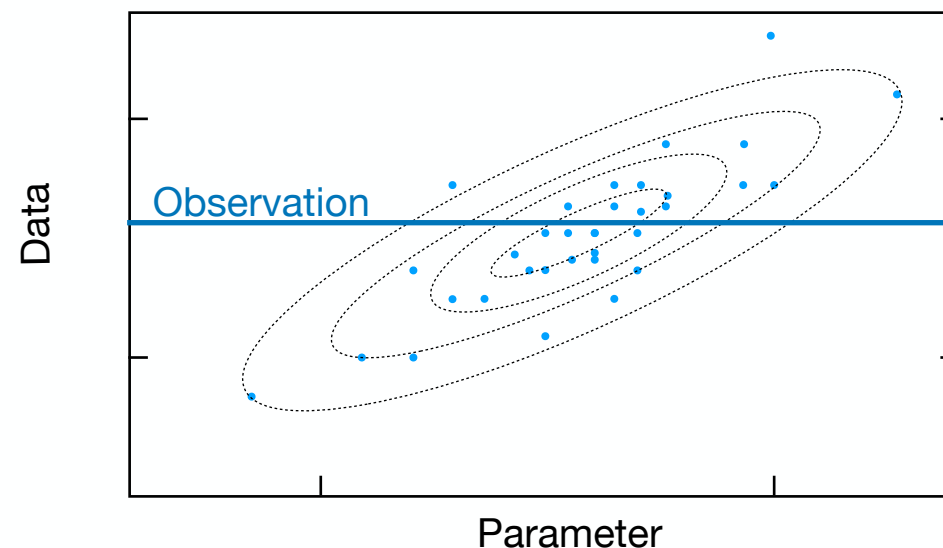
VARIATIONAL INFERENCE

REPLACE $P(\omega)$ BY A DISTRIBUTION WITH A SIMPLE ANALYTIC FORM, $q(\omega)$, (E.G., A GAUSSIAN).



LIKELIHOOD-FREE INFERENCE

Simulation-based inference: produce lots of simulations to populate a parameters-data graph, and at test time cut through that graph to get an accurate posterior



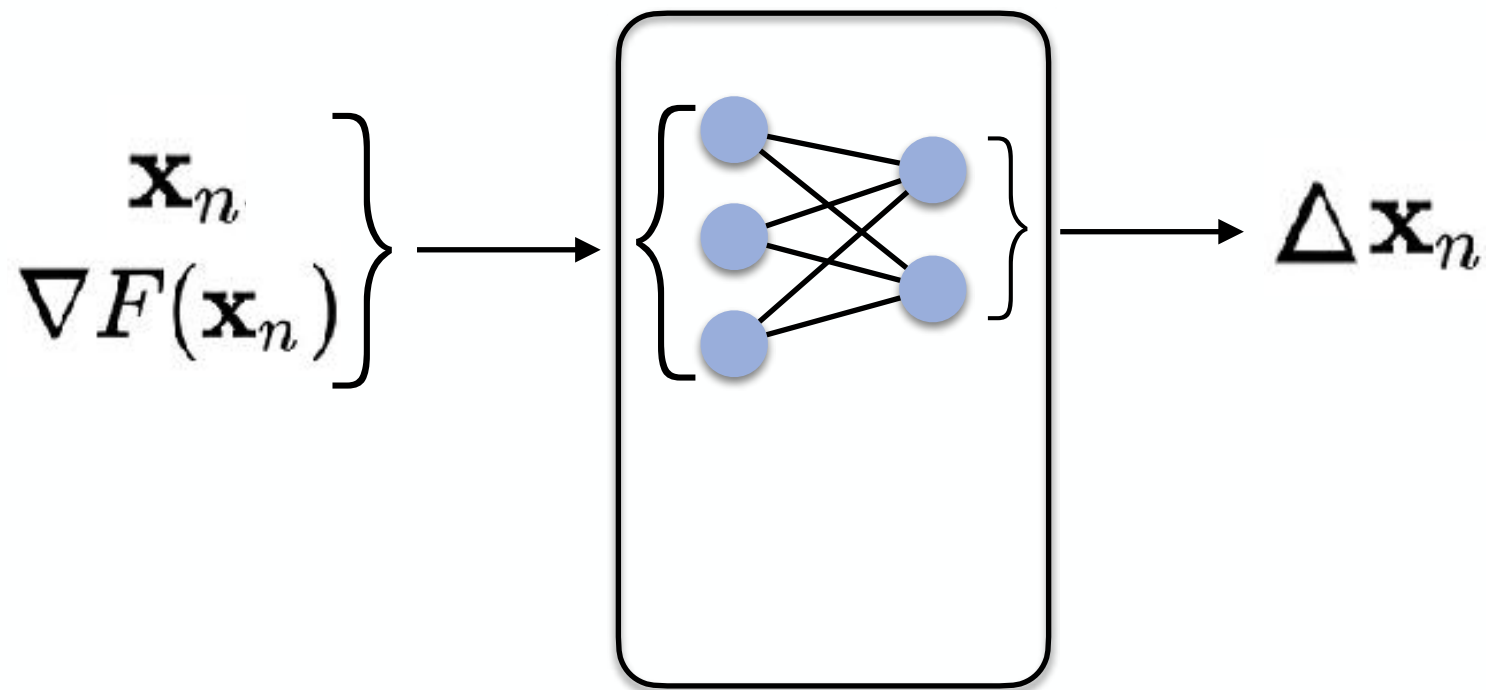
It's possible to use deep learning for automated feature extraction and data compression, and then run your preferred LFI framework.
=> Allows to both harness the power of NNs and be fully Bayesian, it's the best of both world!!

TRAIN A NEURAL NETWORK TO BE A GRADIENT DESCENT OPTIMIZER

$$\mathbf{x}_{n+1} = \mathbf{x}_n - \underbrace{\gamma_n \nabla F(\mathbf{x}_n)}_{\Delta \mathbf{x}_n}$$

TRAIN A NEURAL NETWORK TO BE A GRADIENT DESCENT OPTIMIZER

$$\mathbf{x}_{n+1} = \mathbf{x}_n - \underbrace{\gamma_n \nabla F(\mathbf{x}_n)}_{\Delta \mathbf{x}_n}$$



TRAIN A NEURAL NETWORK TO BE A GRADIENT DESCENT OPTIMIZER

$$\mathbf{x}_{n+1} = \mathbf{x}_n - \underbrace{\gamma_n \nabla F(\mathbf{x}_n)}_{\Delta \mathbf{x}_n}$$

